

# MUON MACHINES

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- ◆ OVERVIEW
- ◆ V-FACTORY
  - PERFORMANCE
  - OSCILLATION PHYSICS
  - OTHER POSSIBILITIES
- ◆ MUON COLLIDERS
- ◆ CONCLUSIONS

# HISTORY...

- Original concepts Budker (1969) Skrinsky (1971)  
KOSHKAREV (1974)  $\gamma$  SOURCE  
PARKHOMCHUK, SKRINSKY (1981) IONIZATION COOLING
- USA studies since 1992 (B. Palmer, Muon Collider Collaboration)  
MUON COLLIDER FEASIBILITY STUDY (1996)
- Study group at CERN (B. Autin) (1997)
- WORKSHOP ON "PHYSICS AT FIRST MUON COLLIDER AND FRONT-END"  
(FERMILAB, 1997)
- "OPTIONS FOR FUTURE COLLIDERS AT CERN"  
commanded by D.G. Ellis Keil Rolandi (Jan. 1998)
- ECFA Encourages "Prospective Study of MUON Storage rings at CERN"  
3 step Strategy (Autin/AB/Ellis) (June 1998)
- CERN report 99-02: Conclusions of prospective study  $\rightarrow$
- **V-FACT99, Lyon, July 99. (ICFA + ECFA)**
- 3 Step Strategy proposed for Fermilab (Geer)  
"a vision for the future of Fermilab"
- M.C.C. becomes "neutrino factory and Muon Collider Collaboration"
- 20 September 1999 Plenary meeting of European Study Group -
- 21 September 1999 Discussion at CERN SPC.

**The conclusions of the prospective study can be stated as follows**

- 1. The line of facilities using MUONbeams seems extremely interesting, providing a very rich physics programme for many years.**
- 2. We suggest to ECFA to recommend to the European particle physics community to take this option very seriously.**
- 3. We arrive at a point where detailed simulations and design become necessary, fault of which the feasibility and competitiveness of the project cannot be ascertained.**

**4. A series of**

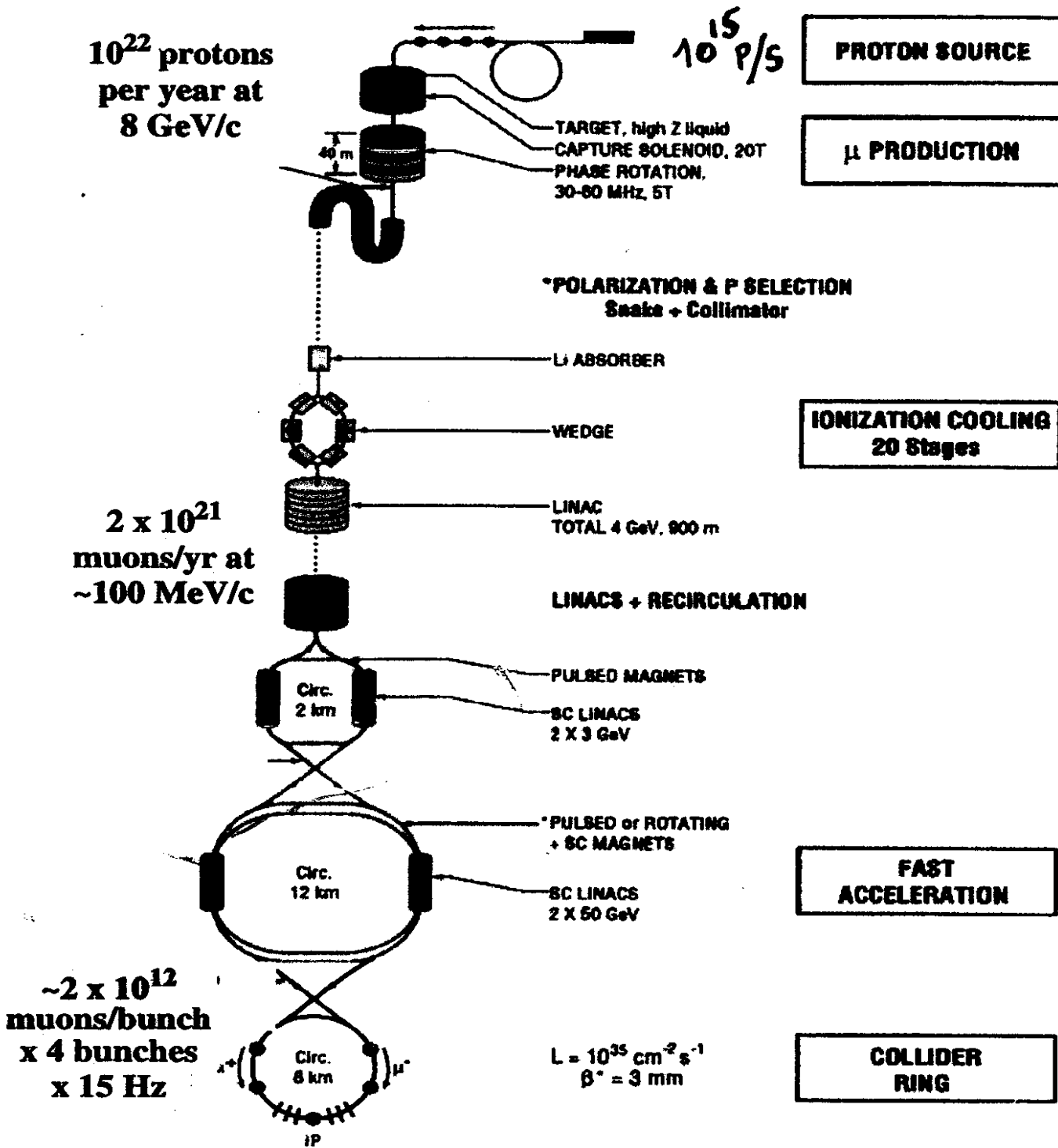
**ECFA-sponsored WORKshops**

**would be an adequate forum to undertake the detailed work that is necessary to design and evaluate more completely this project, with emphasis on the**

**NEUTRINO FACTORY**

**5. The design and even the construction of this line of machines could involve competences that are available throughout Europe. A dedicated collaboration involving european laboratories is necessary to go further, and could become extremely efficient.**

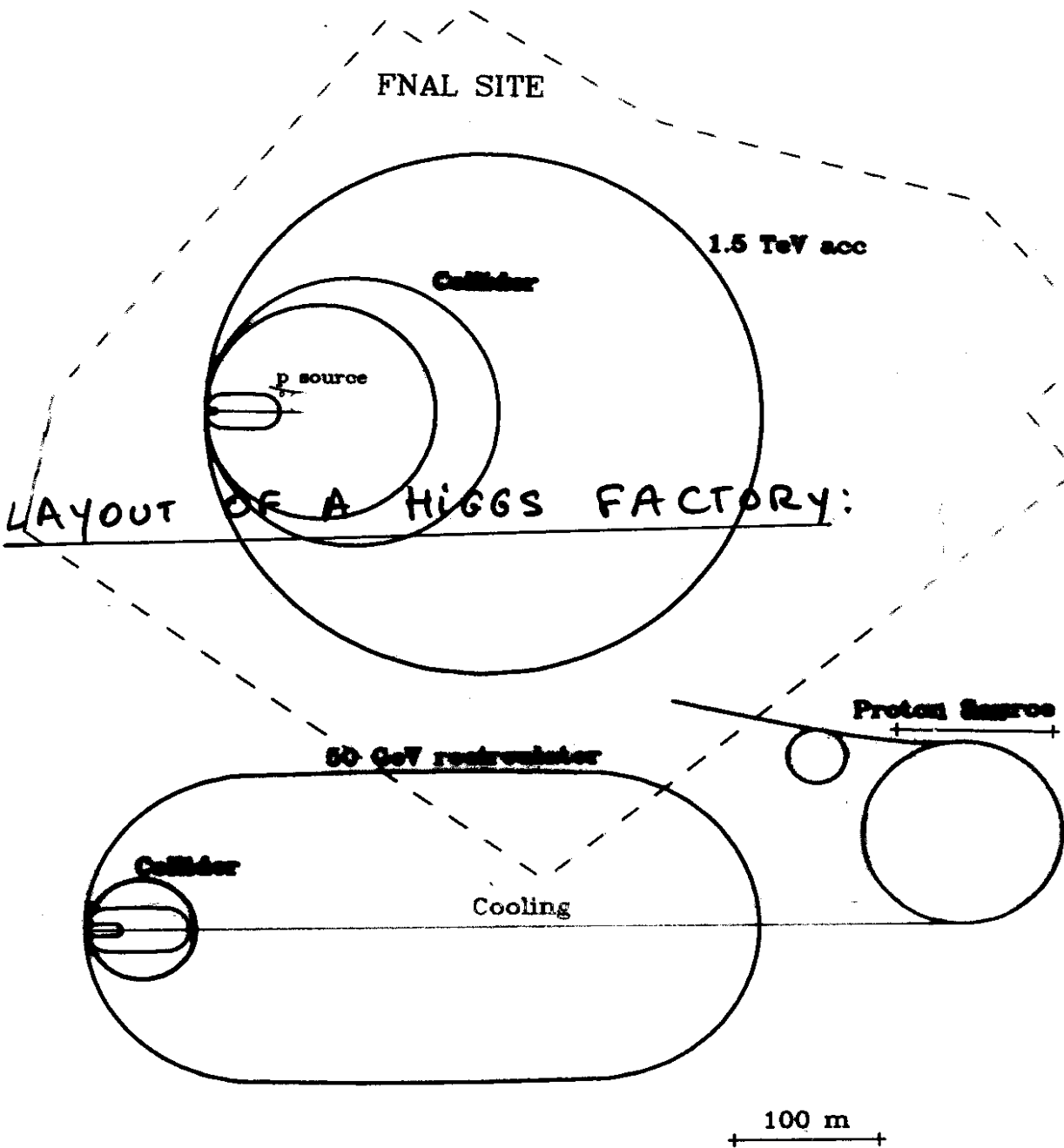
# 2 x 2 TeV Muon Collider Schematic



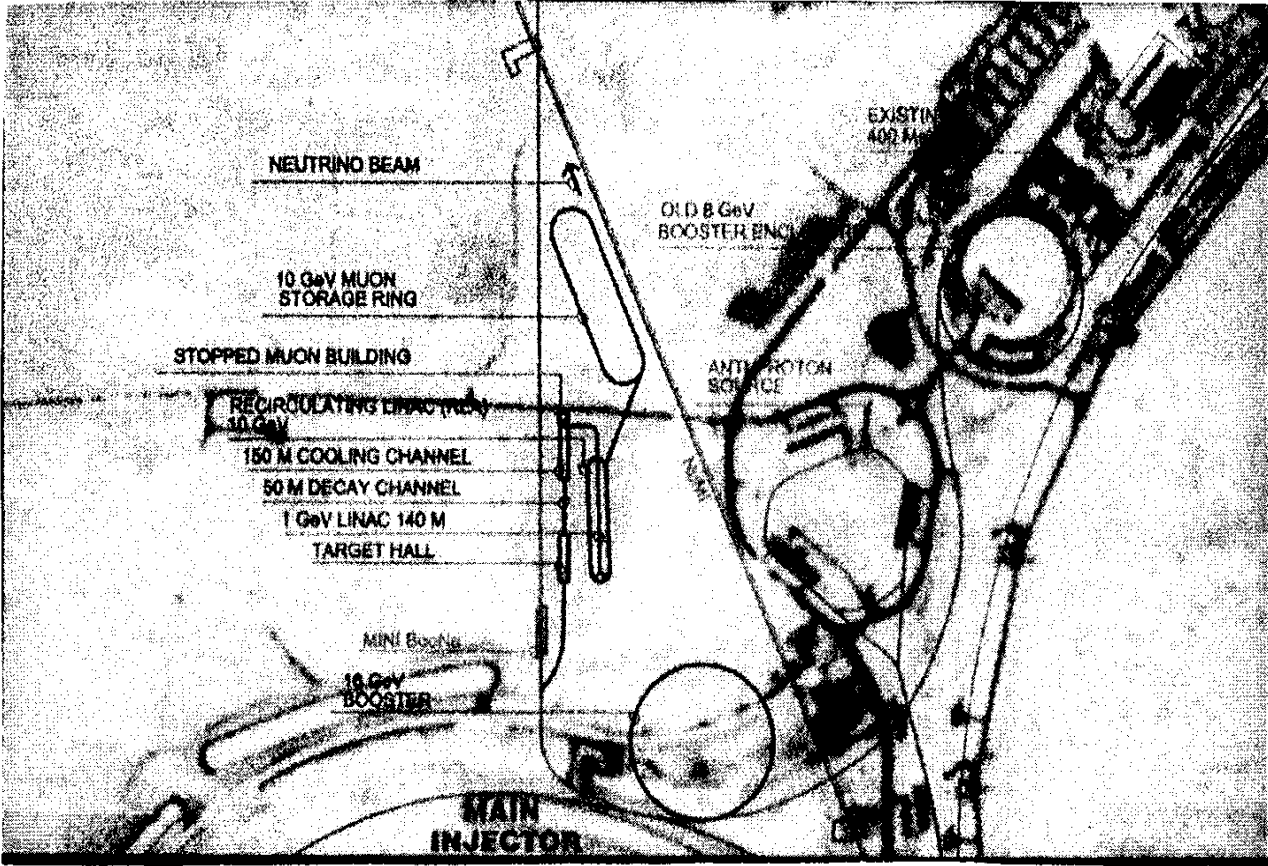
B. Palmer et al.

# LAYOUT OF A 3TeV ECM MUON COLLIDER:

6 km (11.5 km)



Photograph 1



Photograph 1 (Revised)

Photograph 2

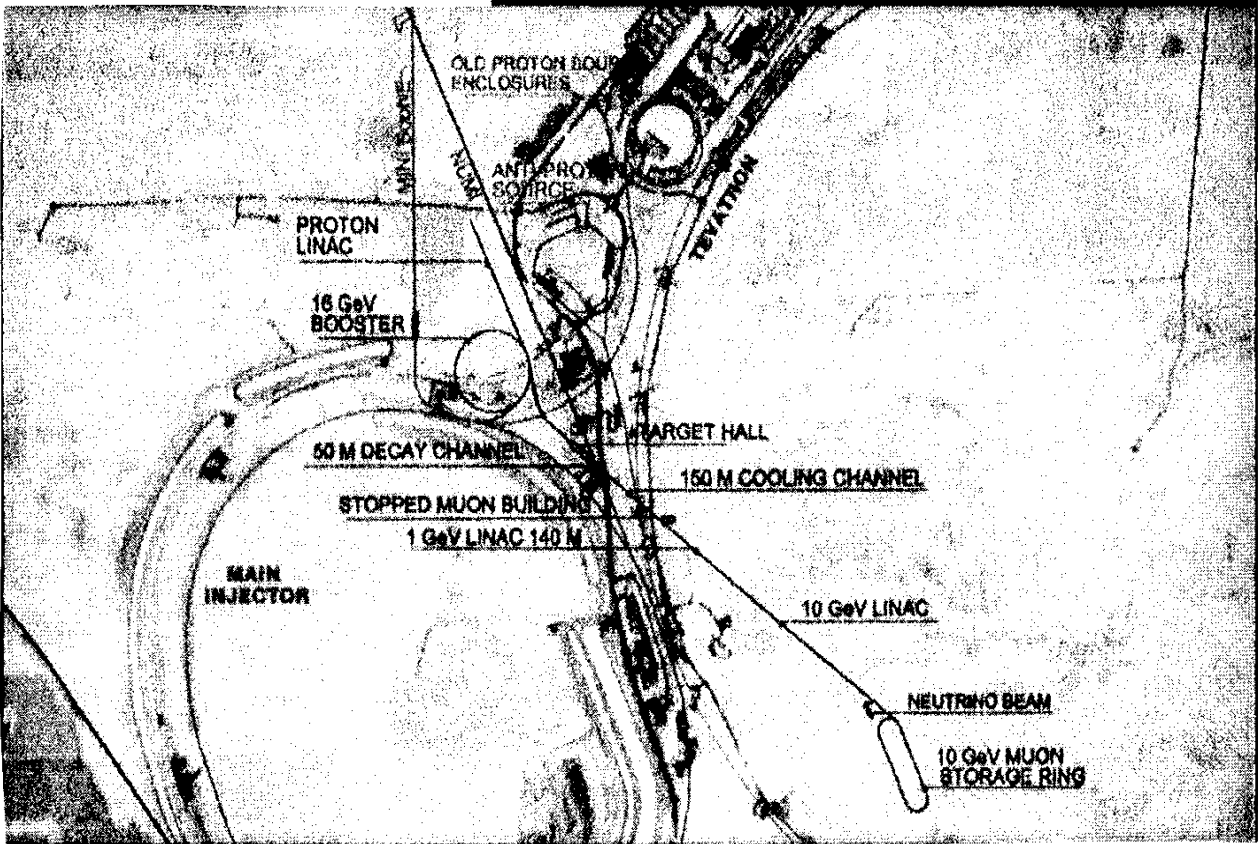
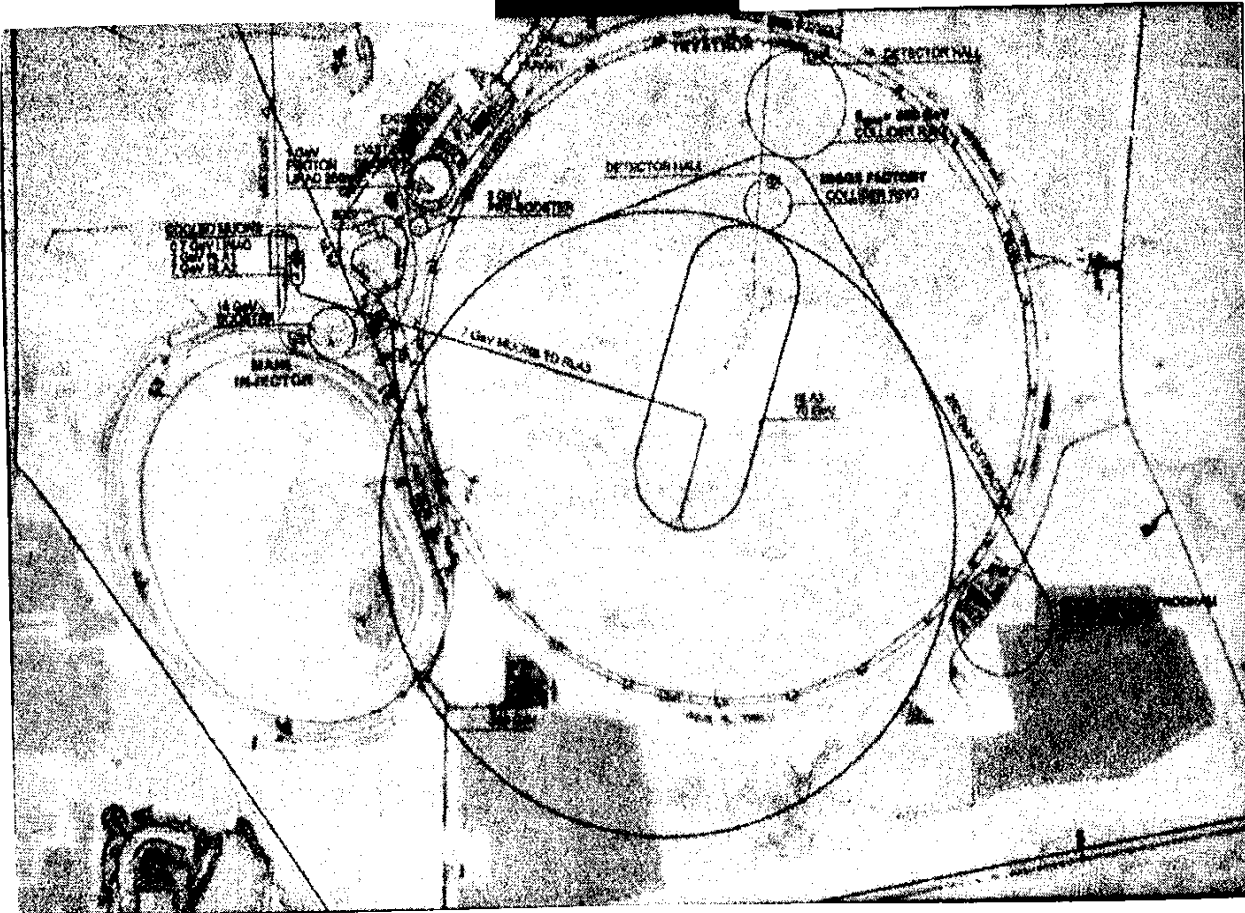


Diagram of the Tevatron

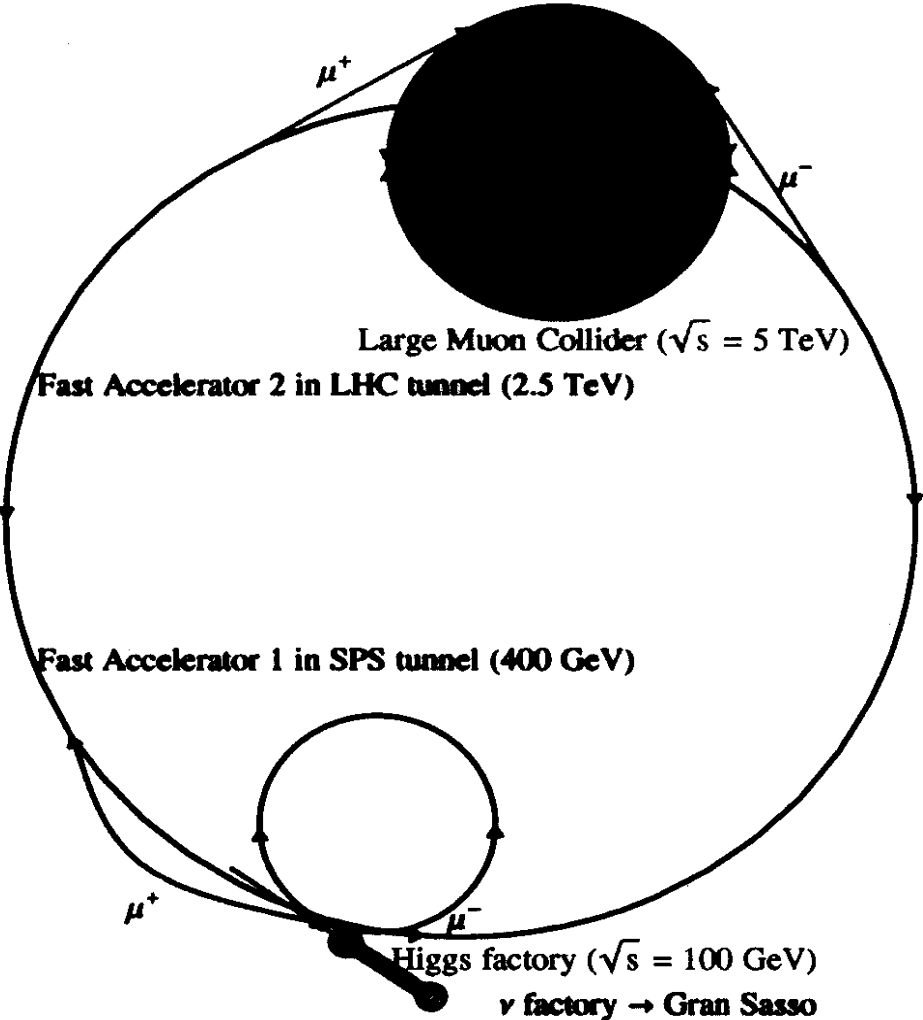
Photograph 3



U.S. DEPARTMENT OF ENERGY



**Possible layout of a MUON complex on the CERN site**



NOBODY HAS EVER BUILT A MUON MACHINE  
AND PROBLEMS SEEM OVERWHELMING  
IF ADDRESSED ALL AT ONCE.

### 3 POSSIBLE STEPS

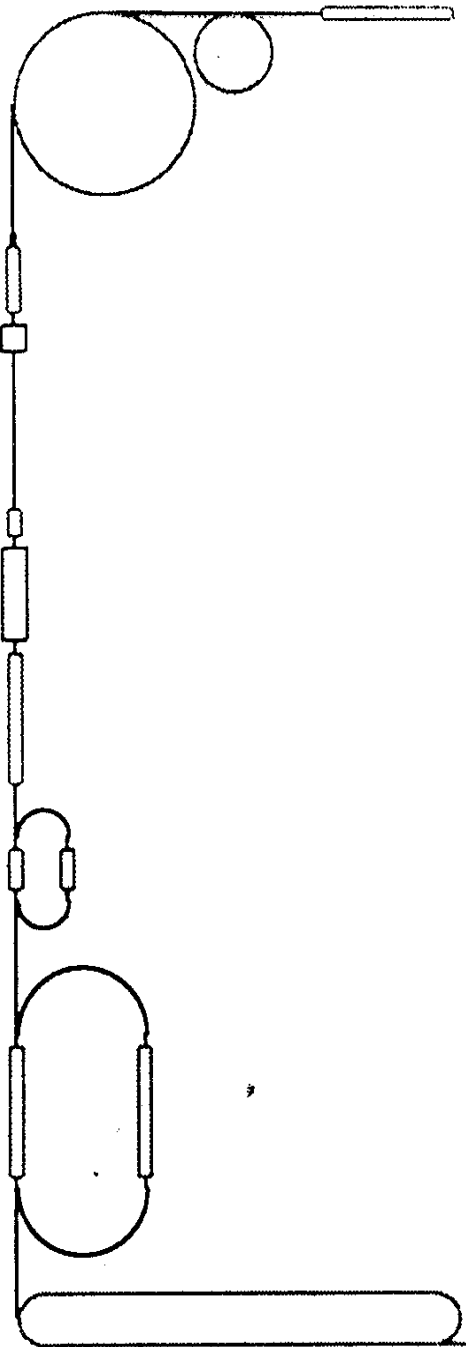
1. NEUTRINO FACTORY
  - high intensity protons  $\rightarrow$  target
  - Efficient capture + some cooling ( $1/30$ )
  - acceleration of MUONS
2. HIGGS FACTORIES
  - COOLING ( $1/10^6$ )
  - DETECTOR SHIELDING
3. HIGH ENERGY FRONTIER.
  - ACCELERATION  $\rightarrow$  2 TeV
  - NEUTRINO RADIATION

EACH OF THESE STEPS HAS A BEAUTIFUL PHYSICS  
PROGRAMME IN ITS OWN RIGHT !

# V-FACTORY

## MUON BUDGET

$1.5 \cdot 10^{15}$  p/s  
 $1.5 \cdot 10^{22}$  p/YR



Proton Driver

Target

Phase Rotate #1

Mini Cooling

Drift

Phase Rotate #2

Cooling

Linac

Recirc. Linac #1

Recirc. Linac #2

Storage Ring

Neutrino Beam 30%

ex 16 GeV/p H/P

( $\pi$  within acc) 0.44

(42 m rf)  $\mu$  0.2

(3.5 m H<sub>2</sub>) ↓

(160 m)

(10 m rf) 0.14

(80 m) 0.09

(2 GeV)

(2-8 GeV)

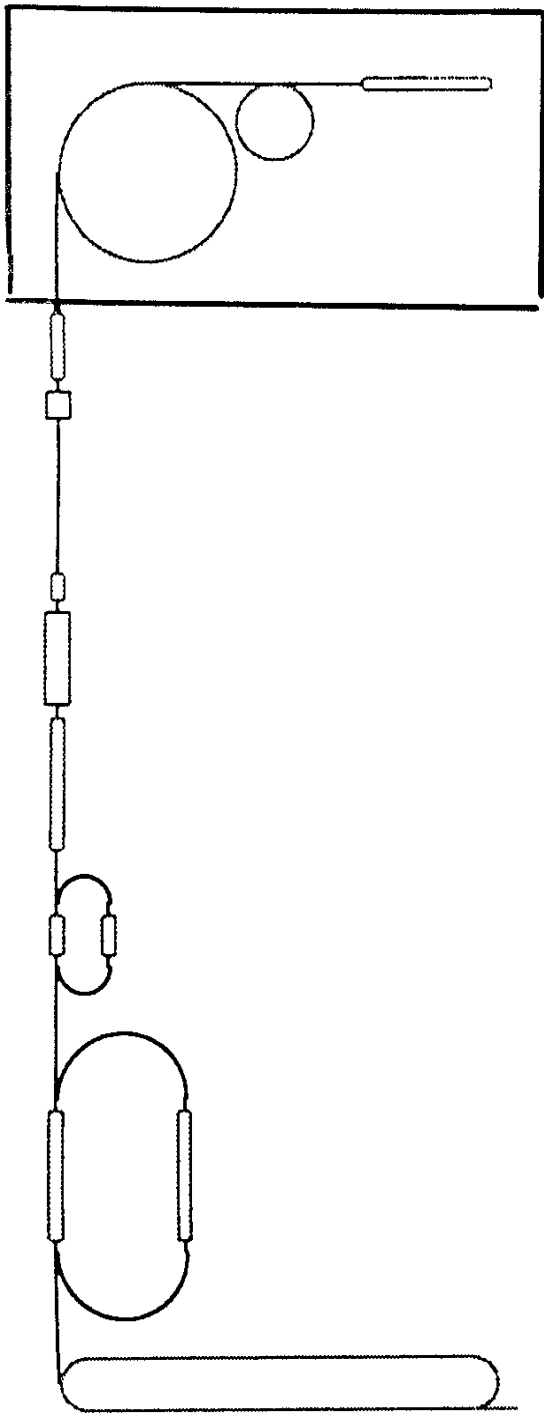
(8-50 GeV) 0.06  $\mu$ /l

(50 GeV 900m circ) 0.02  $\nu_{\mu}$

+ 0.02  $\nu_{e}$

$10^{21}$   $\mu$ /YR

$3 \cdot 10^{20}$   $\nu_e$ /YR +  $3 \cdot 10^{20}$   $\nu_{\mu}$ /YR



# PROTON DRIVER.

## MAIN OPTION

rapid cycling synchronous  
15 Hz

$$E = 16 - 30 \text{ GeV}$$

$$P \leq 4 \text{ MW}$$

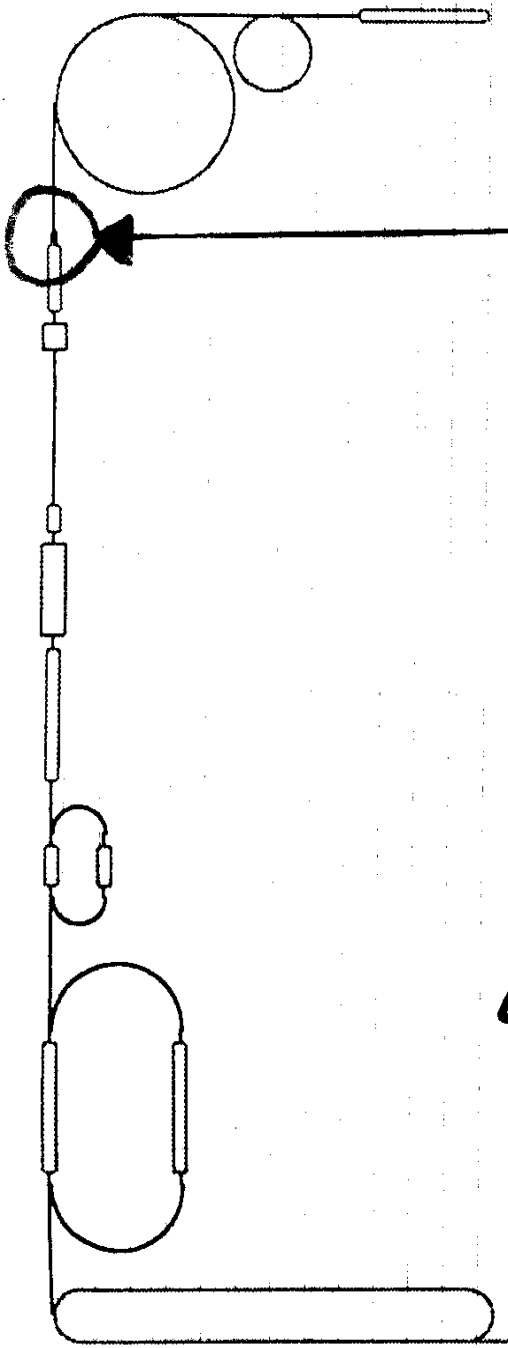
## OTHER OPTIONS

- High intensity Linac + ACCUMULATOR  
 $\Rightarrow \lesssim 50 \text{ Hz}$   
 $E = 2 \text{ GeV}$
- $\alpha$  beam for  $\mu\mu$ ?

## COMMENTS:

- low frequency important for  $\mu\mu$  colliders
- Pion production  $\propto E_p^{\text{kin}}$   
 $\Rightarrow$  Important parameter is: BEAM POWER
- Higher beam power seems easier to reach with LINAC
- $N_\nu$  prop. to Beam Power,  $L_{\mu\mu} \nearrow P \text{ or } P^2$   
 (?)

# TARGET AREA



## MAIN OPTION

- • Liquid MERCURY JET  
LIMITS BEAM POWER TO 4MW
- •  $B = 20\text{ T}$ ,  $R = 7.5\text{ cm}$   $L = 80\text{ cm}$   
SOLENOID

TAPERED TO  $1.25\text{ T}$ ,  $R = 40/140\text{ cm}$   
 $L = \approx 300\text{ m}$ !

- • MONOCHROMATOR =  
42k LINAC, 30-60 MHz, 5-8 MV/m  
PULSED COPPER RF, WARM

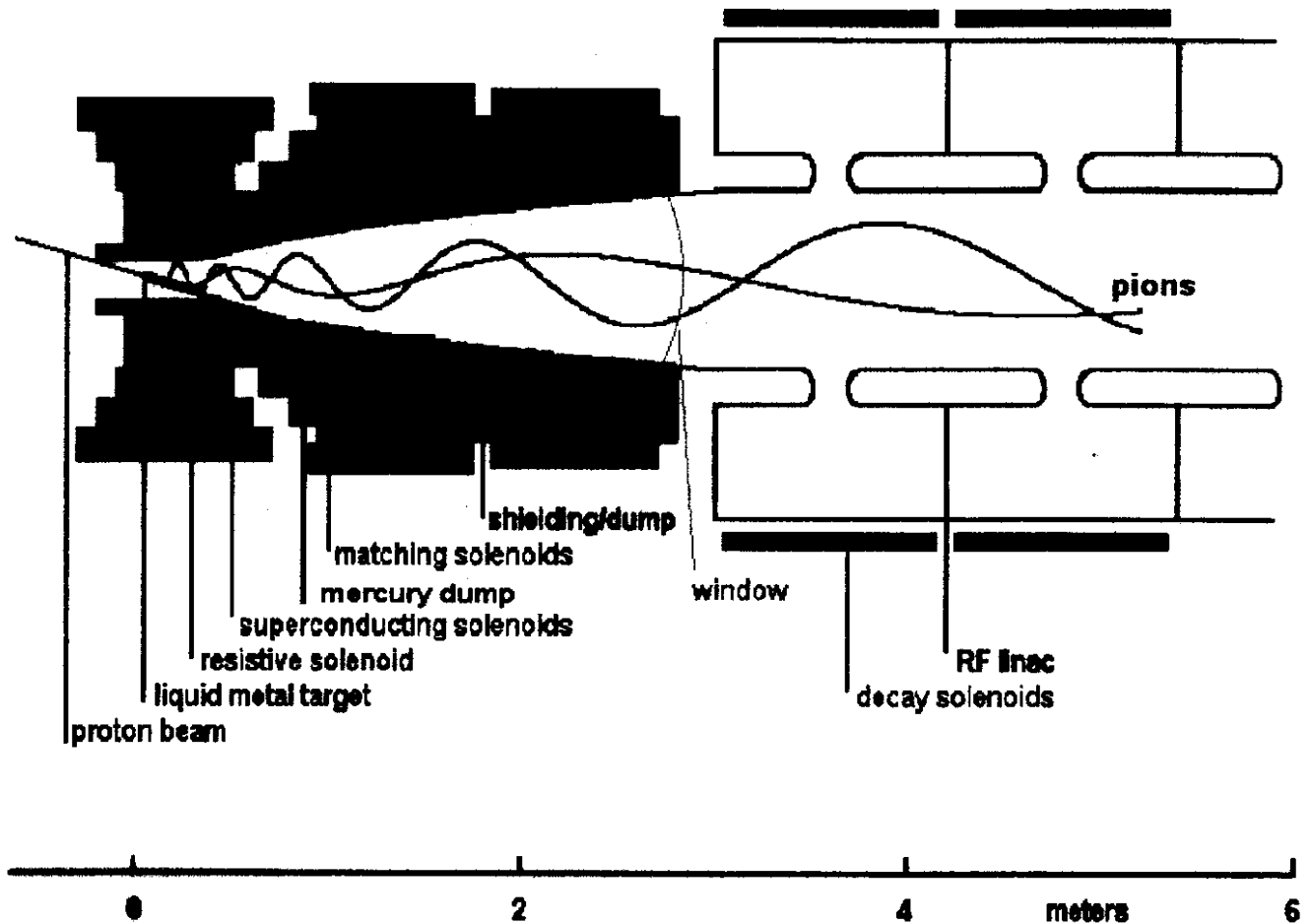


CAVITIES IN B-Field + Radiation

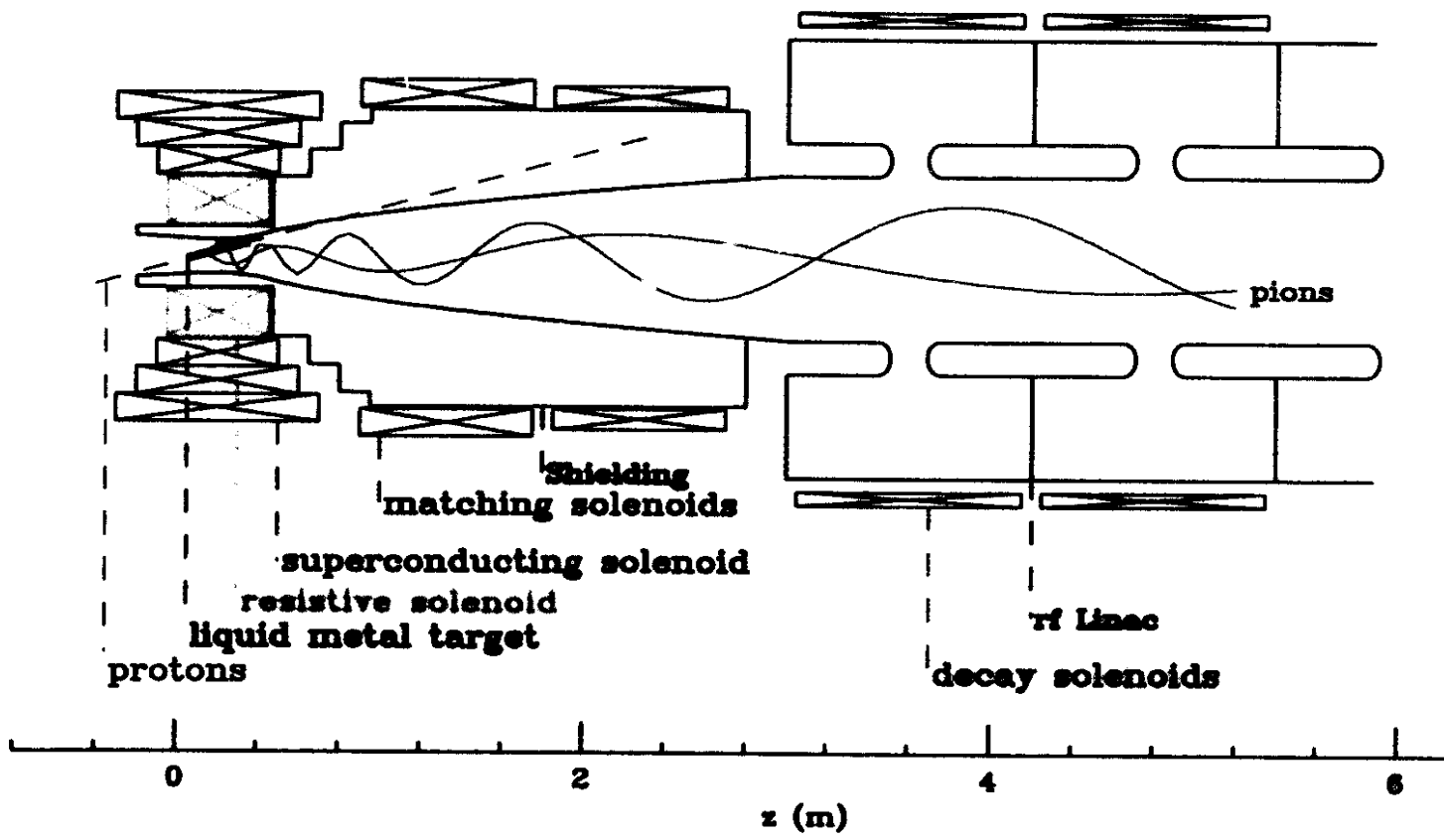
## OTHER OPTIONS

- ROTATING SOLIDS
- PULSED HORN? ONE SIGN  
SOLENOID REQUIRED FOR  $\mu^+\mu^-$
- REDUCES MOMENTUM SPREAD  
TO  $\pm 10\%$
- ESSENTIAL FOR  $\mu^+\mu^-$
- PROVIDES BETTER  
POLARIZATION FOR  
Y-FACTORY  
 $\langle P^2 \rangle$  from  $(0.28)^2$  to  $(0.4)^2$

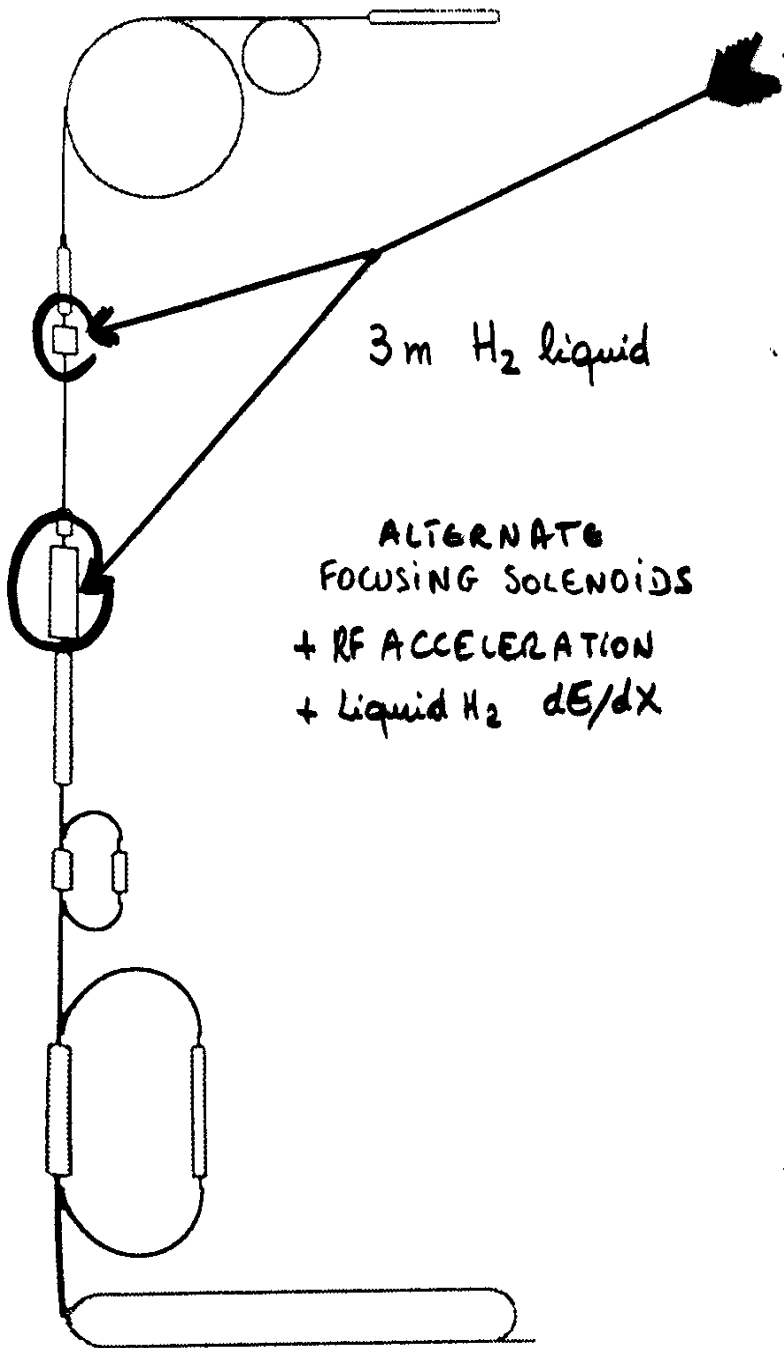
## Overview of Targetry for a Muon Collider



- $1.2 \times 10^{14} \mu^\pm/\text{s}$  via  $\pi$ -decay from a 4-MW proton beam.
- Proton pulse  $\approx 1$  ns rms for a muon collider.
- Mercury jet target.
- 20-T capture solenoid followed by a 1.25-T  $\pi$ -decay channel with phase-rotation via rf (to compress energy of the muon bunch).



# IONIZATION COOLING



3m H<sub>2</sub> liquid

ALTERNATE  
FOCUSING SOLENOIDS  
+ RF ACCELERATION  
+ Liquid H<sub>2</sub> dE/dX

- NOT ABSOLUTELY NEEDED FOR V-FACTORY,  
ALLOWS MORE INTENSITY INTO MACHINES  
OF (REASONABLE) BEAM PIPE SIZE  
⇒ COOLING BY FACTOR  $\approx 30-100$

- CRITICAL ASPECT OF  $\mu\mu$  COLLIDER!  
cooling by FACTOR  $10^6$  required

- NEVER DONE BEFORE.

$\gamma$ -FACT = R & D FOR  $\mu$  COLLIDER



# MUON ACCELERATION [KEIL]

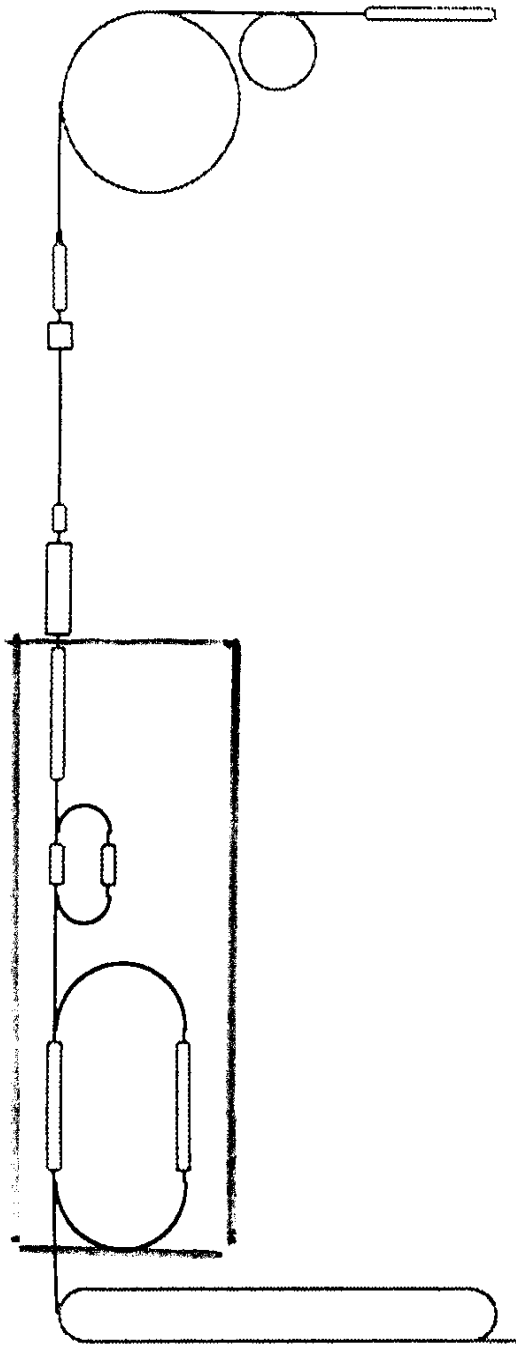
Linac  $\rightarrow$  2 GeV

Recirculating  $\rightarrow$  7.5 GeV

LINAC

[many arcs or  
FFAG?]  $\rightarrow$  50 GeV

heavy use of LEP SC RF cavities!



# ENVIRONMENTAL RADIATION ISSUES

[Mokhov, Dydak, Stevenson, Silari]

OK... **⚠ MUST BE TREATED VERY CAREFULLY!**

## \* AROUND TARGET:

[neutrons + photons]

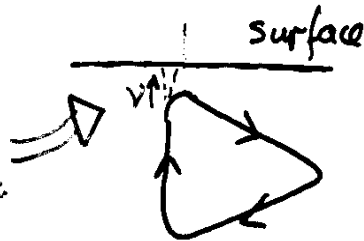
Requires •  $\geq 10$  m of Rock or CONCRETE

- AVOID AQUIFEROUS SUBSTRATE  
[T and Na<sub>22</sub> \* Water table]

## \* AROUND MUON STORAGE RING

[decay electrons  $\rightarrow$  photons]  
+ Stray muons?

THIS AREA MUST BE  
INSIDE SITE!



- SHIELDING OF BEAM PIPE
- HOW CLOSE CAN DETECTOR BE?
- RADIATION FROM NEUTRINOS\*

\* ISSUE FOR  $\mu$ -COLLIDER ABOVE  $E_{CM} = 4$  TeV

$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$$

$\nu$ -FACT  $\approx 100 \times$  conventional  $\pi \rightarrow \mu \nu$  beams  
 $E_\mu = 30 \text{ GeV}$   
 $\times 2$  FLAVOURS

- +
- well known flux, no high energy tail
  - $\nu / \bar{\nu}$  asymmetries easy ( $\mu^+ \rightarrow \mu^-$ )
  - $\bar{\nu}_\mu / \nu_e$  content depends on beam polarization

Physics:

- $\nu$  OSCILLATIONS  $\theta_{13}$ , matter effects,  $CP, \delta$
- very high flux  $\nu$  beam for DIS, NC/CC ....

$\nu$  FLUX CHARACTERISTICS:

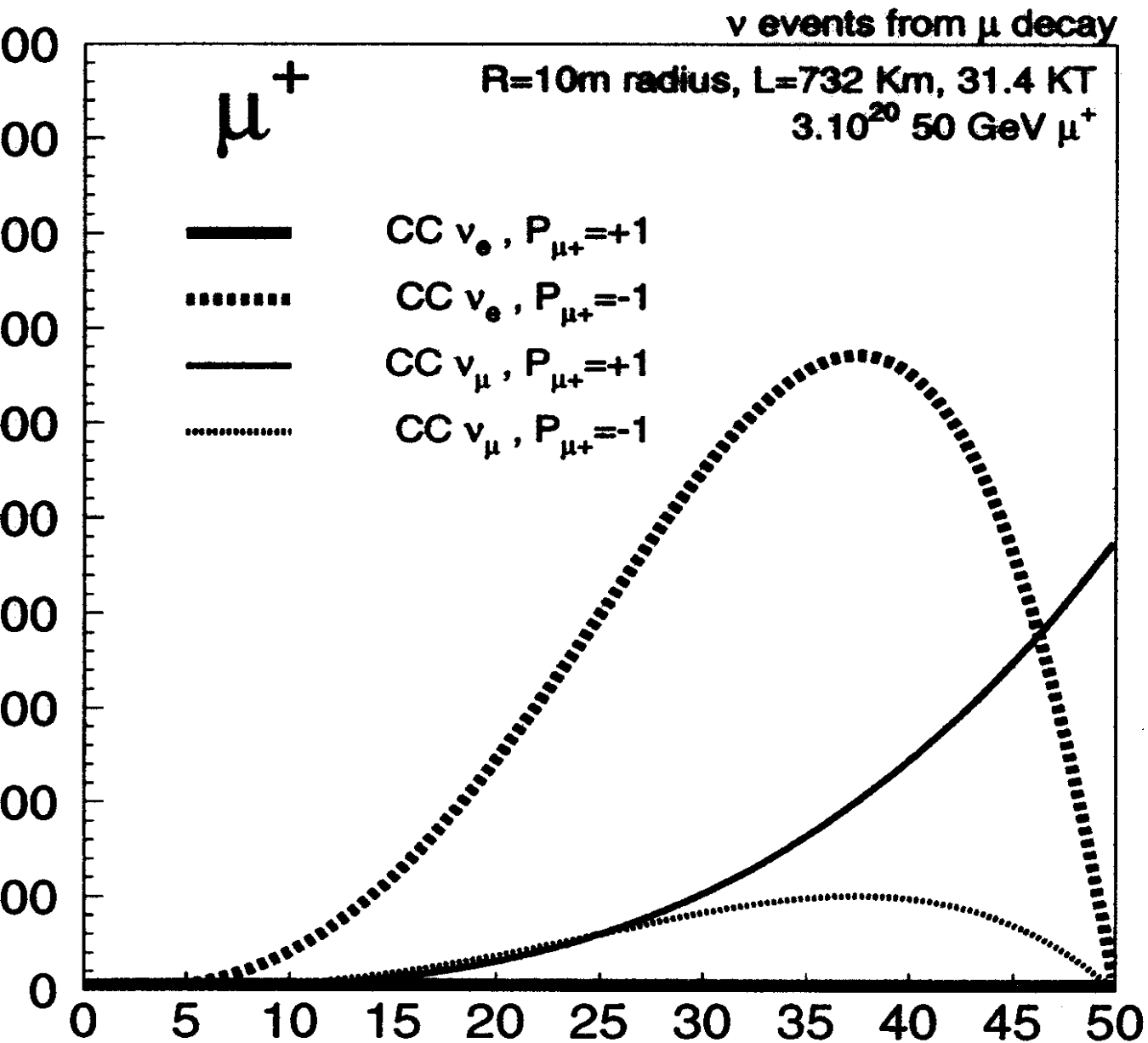
$\nu_e / \nu_\mu$  event ratio reversed by switching  $\mu^+ \rightarrow \mu^-$

$\vec{\mu}^+ \otimes \leftarrow \nu_e$  in Forward Direction

$\Rightarrow \mu$  POLARIZATION CONTROLS  $\nu_e$  flux [28%  $\rightarrow$  40%]

vents/0.25 GeV  
 $10^2$

$\nu_e / \nu_\mu$  flux shapes are different.



# NEUTRINO OSCILLATIONS

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

$\swarrow \theta_{12}$  (3 solutions)       $\nwarrow \theta_{13}$  (small)  
 $\swarrow \theta_{23}$  (large)

$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{j>i} U_{\alpha i} U_{\beta i} U_{\alpha j}^* U_{\beta j}^* \sin^2 \left[ k \Delta m_{ij}^2 \frac{L}{E} \right]$$

Each expt is sensitive to 3 angles and 3 mass differences + possibly 1 phase

FOR BASELINES OF EARTH SIZE  $E \rightarrow \Delta m_{23}^2 \theta_{13} \theta_{23}$   
 FOR SOLAR NEUTRINOS  $\Delta m_{12}^2 \theta_{12}$   
 $\nearrow \sim 10^{-5} - 10^{-4}$

ON EARTH:

$$\begin{aligned}
 P(\nu_e \rightarrow \nu_\mu) &= \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \left( k \frac{\Delta m_{23}^2 L}{E_\nu} \right) \\
 P(\nu_\mu \rightarrow \nu_\tau) &= \cos^4 \theta_{13} \sin^2 2\theta_{23} \sin^2 \left( k \frac{\Delta m_{23}^2 L}{E_\nu} \right) \\
 P(\nu_e \rightarrow \nu_\tau) &= \cos^2 \theta_{23} \sin^2 2\theta_{13} \sin^2 \left( k \frac{\Delta m_{23}^2 L}{E_\nu} \right)
 \end{aligned}$$

PROBABLE VALUES FROM SUPERK + AR fit.  
 ...

$$\begin{aligned}
 \Delta m_{23}^2 &\approx 3 \pm 1 \cdot 10^{-3} \\
 \theta_{23} &\approx 45^\circ \\
 \theta_{12} &\approx 0 - 45^\circ \text{ (best } = 8^\circ?)
 \end{aligned}$$

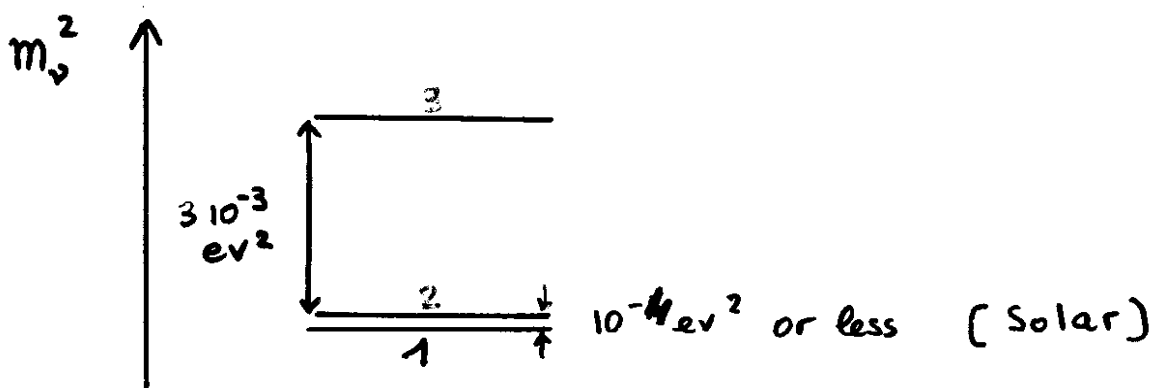
### 3 FAMILIES:

PROBABLE SPECTRUM (SMIRNOV, MORIOND '99)

$$\nu_1 = \nu_e + \epsilon_{1\mu} \nu_\mu + \epsilon_{1\tau} \nu_\tau$$

$$\nu_2 = \epsilon_{2e} \nu_e + \frac{1}{\sqrt{2}} (\nu_\mu + \nu_\tau)$$

$$\nu_3 = \epsilon_{3e} \nu_e + \frac{1}{\sqrt{2}} (\nu_\mu - \nu_\tau)$$



$$\Rightarrow \Delta m_{12}^2 \approx \Delta m_{23}^2 \approx 3 \cdot 10^{-3} \text{ eV}^2$$

$\Rightarrow$  THERE ARE TWO  $\Delta m_{ij} \approx 3 \cdot 10^{-3} \text{ eV}^2$   $\nabla$

$$\Delta m^2 = 3 \cdot 10^{-3} \Rightarrow L_{\min} = 400 \text{ km} \times E_\nu$$

= earth diameter for  $E = 30 \text{ GeV}$

### • 4 Families or Sterile $\nu$ (LSND true):

makes everything more complicated and interesting  
not considered here.

At High frequency (Large  $\Delta m^2$ ) ( $L/E \approx 500 \text{ km/GeV}$ )

$$\star P(\nu_e \rightarrow \nu_\mu) = \sin^2 \theta_{23} \sin^2 2\theta_{13} \sin^2(\kappa \Delta m^2 L/E)$$

$$\star P(\nu_\mu \rightarrow \nu_\tau) = \cos^4 \theta_{13} \sin^2 2\theta_{23} \sin^2(\kappa \Delta m^2 L/E)$$

$$\star P(\nu_e \rightarrow \nu_\tau) = \cos^2 \theta_{23} \sin^2 2\theta_{13} \sin^2(\kappa \Delta m^2 L/E)$$

$$\theta_{23} \approx 45^\circ \quad \theta_{13} = [0 \dots 13^\circ \dots 45^\circ]$$

$$\text{SUPERK} \Rightarrow \cos^4 \theta_{13} \cdot \sin^2 2\theta_{23} \approx 1 \pm 0.15$$

**\*  $\nu_e$  OSCILLATIONS IMPORTANT TO INVESTIGATE  $\nu$  MIXING MATRIX.**

# SIGNAL EVENTS [APPEARANCE EXPT]

$$\text{EVENTS} = N \cdot \sigma \cdot \phi \cdot \overbrace{V \cdot \rho}^{\text{AVOGADRO FUX } \nu/\text{cm}^2 \text{ MASS}}$$

$$E_\nu \cdot \frac{E_\nu^2}{L^2 \rho^2} = E_\nu^3 / L^2$$

$$\text{oscillated events: } \frac{E_\nu^3}{L^2} \times \sin^2\left(\kappa \frac{\Delta m^2 L}{E}\right) \propto E$$

$$\text{uncertainty on BKG} \sim \sqrt{E^3/L^2}$$

LOW BKG : SIGNAL  $\propto E$

HIGH BKG  $\sigma \propto \frac{1}{E}$   
a disappearance

# EXPERIMENTAL SIGNATURE OF $\bar{\nu}_e$ OSCILLATIONS:

## WRONG SIGN MUONS

$$\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu$$

NORMAL CC:

$$\nu_e + N \rightarrow e^- + X$$

$$\bar{\nu}_\mu + N \rightarrow \mu^+ + X$$

OSCILLATION

"EASY"!

$$\nu_e \rightarrow \nu_\mu + N \rightarrow \textcircled{\mu^-} + X$$

hard  $\mu^-$

$$\nu_e \rightarrow \nu_\tau + N \rightarrow \tau^- + X$$

$$\hookrightarrow \textcircled{\mu^-} \nu_e \bar{\nu}_\mu$$

softer  $\mu^-$   
+ missing  
 $E, P_\perp$

ALSO

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e + N \rightarrow \textcircled{e^+} + X$$

"IMPOSSIBLE" (?)

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_\tau + N \rightarrow \tau^+ + X$$

$$\hookrightarrow \textcircled{e^+} \bar{\nu}_e \nu_\mu$$

## ⇒ MAGNETIC DETECTORS

BACKGROUND IS  $\nu_\mu + N \rightarrow C \mu^-_{\text{slow}}$   
 $\hookrightarrow e^+ \nu_s \text{ or } \mu^+ \nu_s$



# BASELINE DETECTOR :

LARGE ( $\geq 10$  KT fid.)

MAGNETIZED IRON + SCINTILLATOR

$\sim$  few cm granularity.

• WRONG SIGN MUON APPEARANCE

• SOME  $e^\pm$  DETECTION

• NC/CC

most sensitivities calculated on this basis only.

## FURTHER CHALLENGES

$e^\pm$  appearance

[ICARUS

Companelli

$\tau^\pm$  appearance

" , OPERA]

Stolin

$e$  of wrong sign

(???)

D. Cline

$\mu^\pm$  Polarization influences  $\nu_e/\bar{\nu}_\mu$  ratio  
usefulness not quantified YET.

HIGH STATISTICS + WELL KNOWN FLUX

⇒ HIGH PRECISION MEASUREMENTS  
OF OSCILLATION PARAMETERS

e.g.  $\nu_\mu \rightarrow \nu_\tau$ :

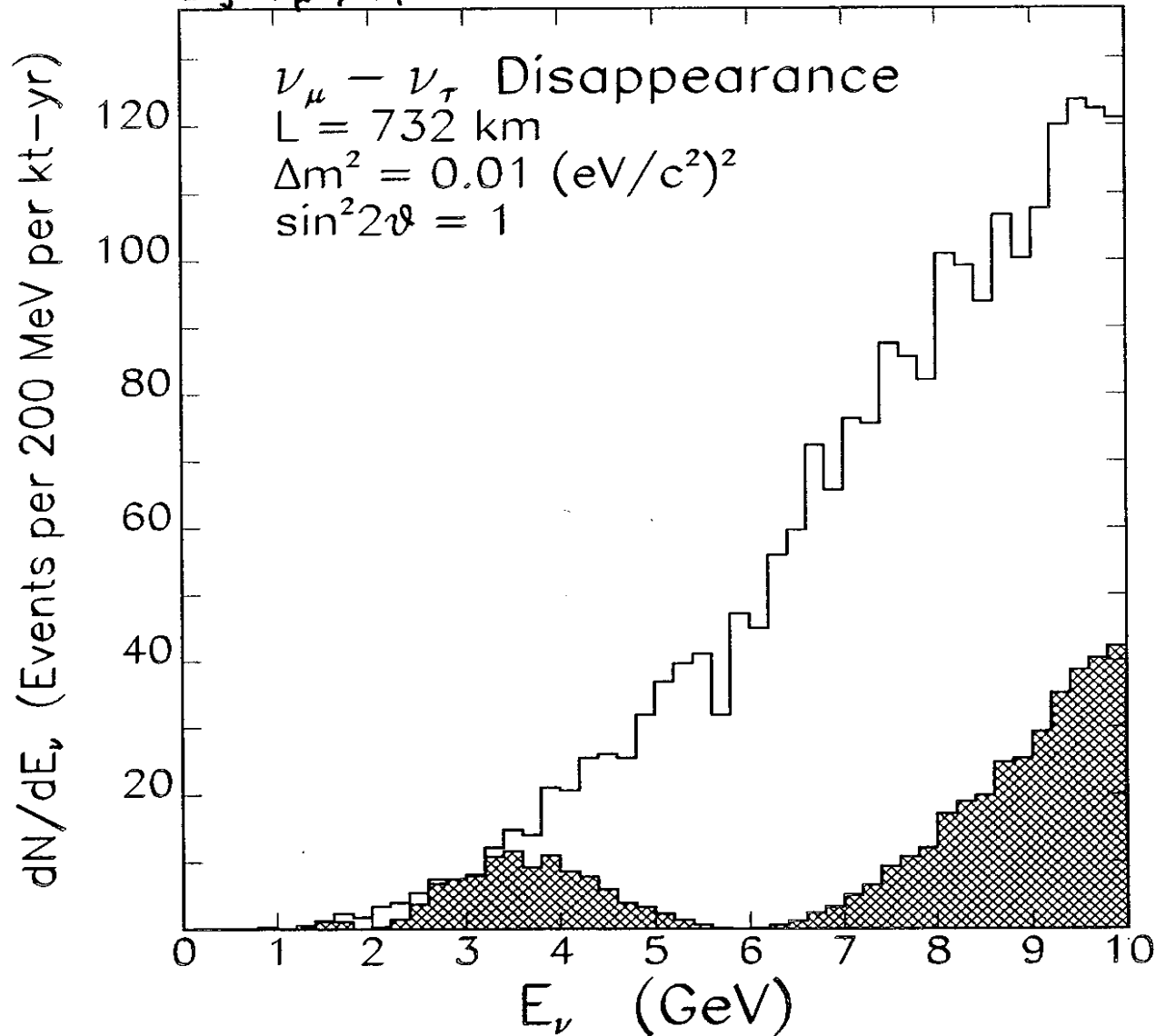


Figure 8 Predicted signal for  $\nu_\mu$  disappearance using a 10 GeV muon storage ring neutrino source at FNAL, pointed towards the Soudan mine in Minnesota. The open histogram is the prediction for the energy dependent CC interaction rate with no oscillations, and the shaded histogram is the prediction with oscillation parameters  $\Delta m^2 = .01 \text{eV}^2$  and  $\sin^2 2\theta = 1$ .

Full analysis with 3 FAMILIES OSCILLATIONS (Garcia Hernandez De RUIJLA)

$\mu^-$  beam 20 GeV  
 $3 \times 10^7$  of  $2.10^{20}$   $\mu/s$

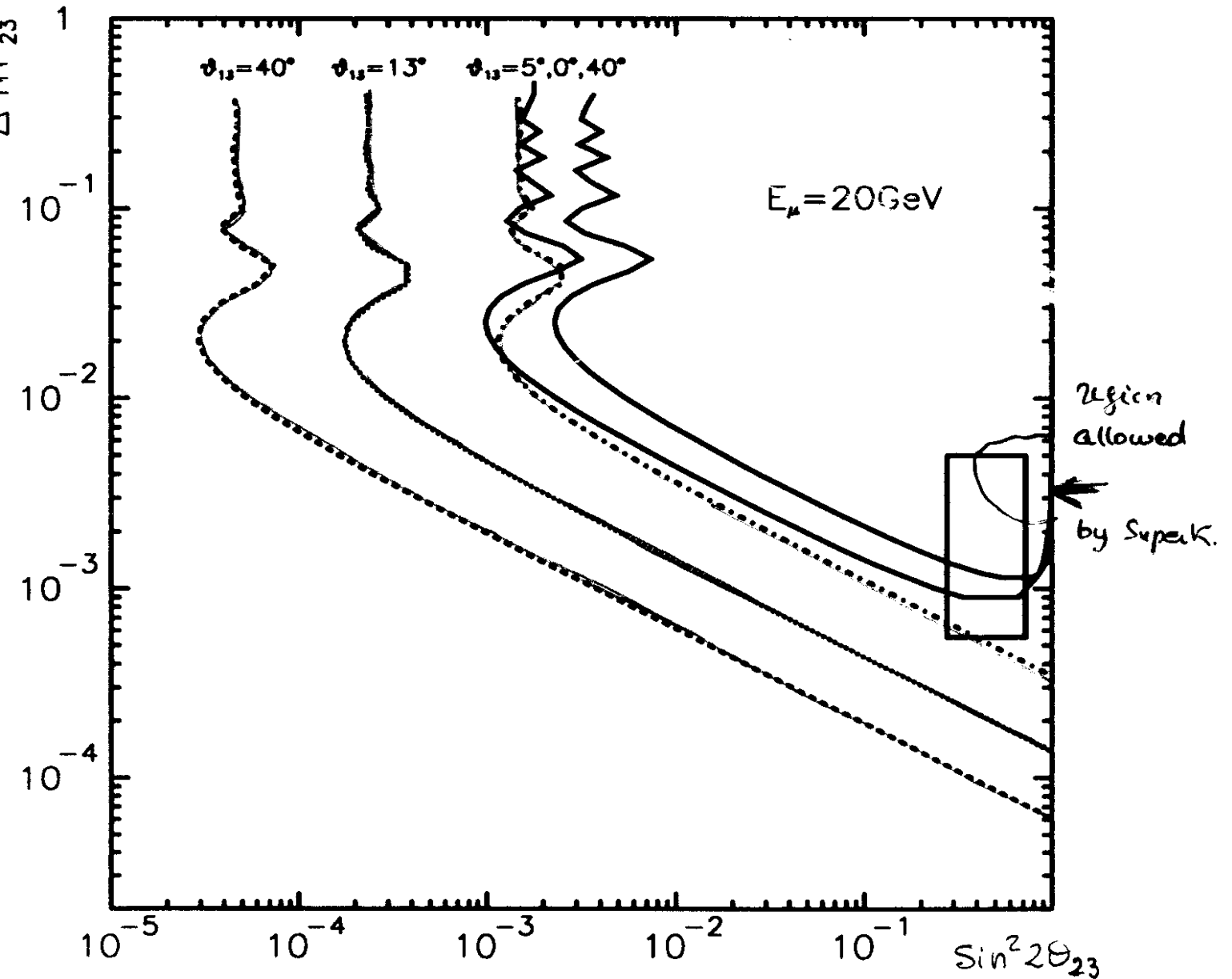
730 km

10 kT able to see  $\mu^+/\mu^-$

Compare:  $\mu^-$  Disappearance

$\theta_{23} / \Delta m_{23}^2$  à la SuperK  
 $\theta_{13} \in [0 - 45^\circ]$

$\mu^+$  (wrong sign) Appearance (from  $\bar{\nu}_e \rightarrow \bar{\nu}_\tau \rightarrow \tau^+$   
 $\nu_e \rightarrow \nu_\mu \rightarrow \mu^+$ )

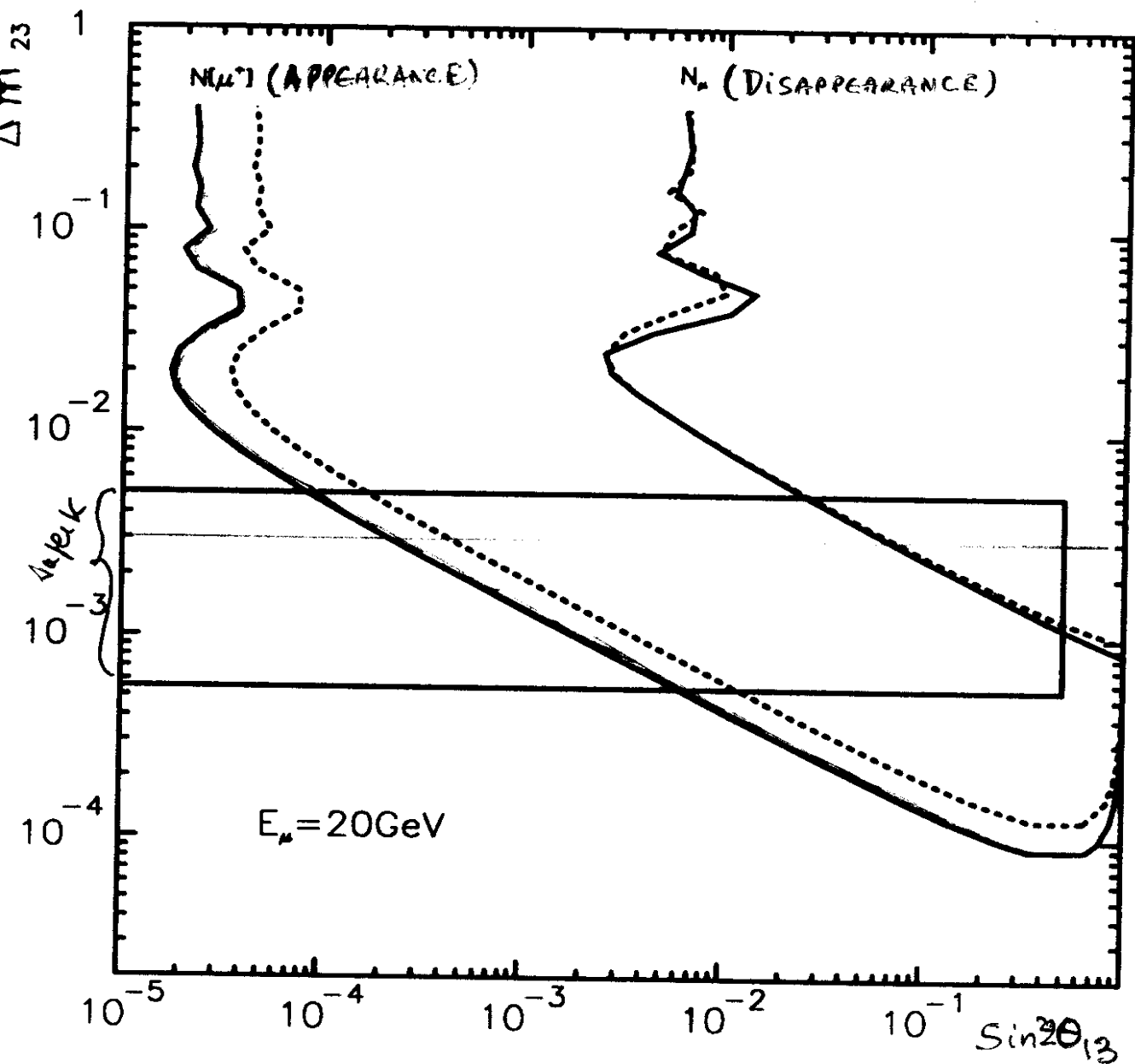


Same as  $\Delta m_{23}^2 / \sin^2 \theta_{13}$

APPEARANCE OF  $\mu^+$  in  
 BEAM FROM  $\mu^-$  decay  
 ( $\mu^+$  beam would be better here)

REACH  $\approx 10^{-4}$   
 $\sim$  precision

(cf Minos  $\sim 10^{-2}$ )



# CP or T VIOLATION

LIKE in the 3x3 QUARK MIXING MATRIX  
THERE ARE 4 DEGREES OF FREEDOM.

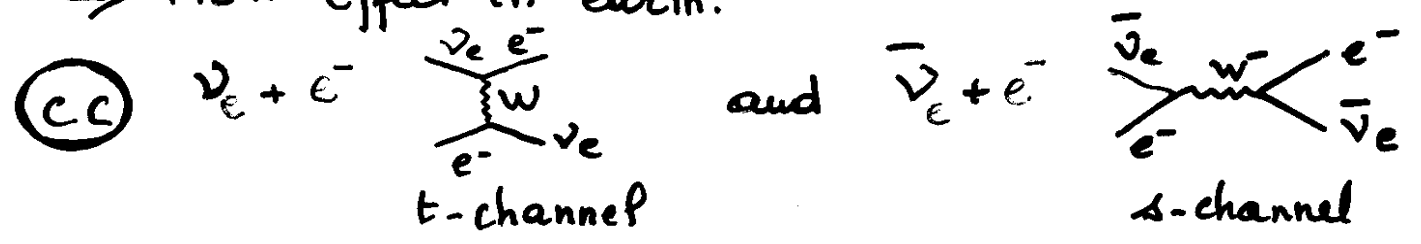
3 ANGLES

1 PHASE. → COMPLEX MATRIX

$$A_{CP} = \frac{P(\nu_e \rightarrow \nu_\mu) - P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)}{P(\nu_e \rightarrow \nu) + P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)} \approx 10^{-2} \pm 1$$

! HOWEVER! NEED LONG BASELINE THROUGH EARTH

⇒ MSW effect in earth.



→ OPPOSITE SIGN! ←

GENERATES FAKE CP-ASYMMETRY

$$A_T = \frac{P(\nu_e \rightarrow \nu_\mu) - P(\nu_\mu \rightarrow \nu_e)}{P(\nu_e \rightarrow \nu_\mu) + P(\nu_\mu \rightarrow \nu_e)}$$

$\mu^+$  beam                       $\mu^-$  beam

Requires sign id for  $e^\pm$ . "IMPOSSIBLE"...?

# T, CP Violation

Gavela Hernandez de Rujula; Donini  
Romanino, Rigolin...

Need large mixing angle MSW solution.

- $A_{CP}^{\nu_e \rightarrow \nu_\mu} \sim \frac{4 \sin 2\theta_{12} \cdot \sin \delta}{\sin \theta_{13}} \cdot \sin\left(\frac{2 \Delta m_{12}^2 L}{4\pi E}\right)$   
↑ goes as  $\frac{1}{E_{13}}$       ↑ scales as  $\frac{L}{E}$

- REQUIRES APPEARANCE EXPT ( $P(\nu_e \rightarrow \nu_e)$  is T symmetric!)  
⇒ not accessible to Reactor or solar expts.
- REQUIRES "SUPPRESSED"  $\nu_e \rightarrow \nu_\mu$  transition (does not work for  $\nu_\mu \rightarrow \nu_\tau$ )

- $A_{\text{matter}}^{\text{fake}} \sim 0.7 \cdot 10^{-6} \frac{L^2 (\text{km}^2)}{E (\text{GeV})}$  . for  $\Delta m_{23}^2 = 3 \cdot 10^{-3}$

- AT VERY LONG BASELINES MATTER EFFECTS CAN BE MEASURED  
(RESONANCE at  $E \sim 10 \text{ GeV}$  IN EARTH)  
AND SUBTRACTED FROM A SHORTER BASELINE EXPT. [Difference in composition of earth?]

(Gonzalez Garcia et al.)

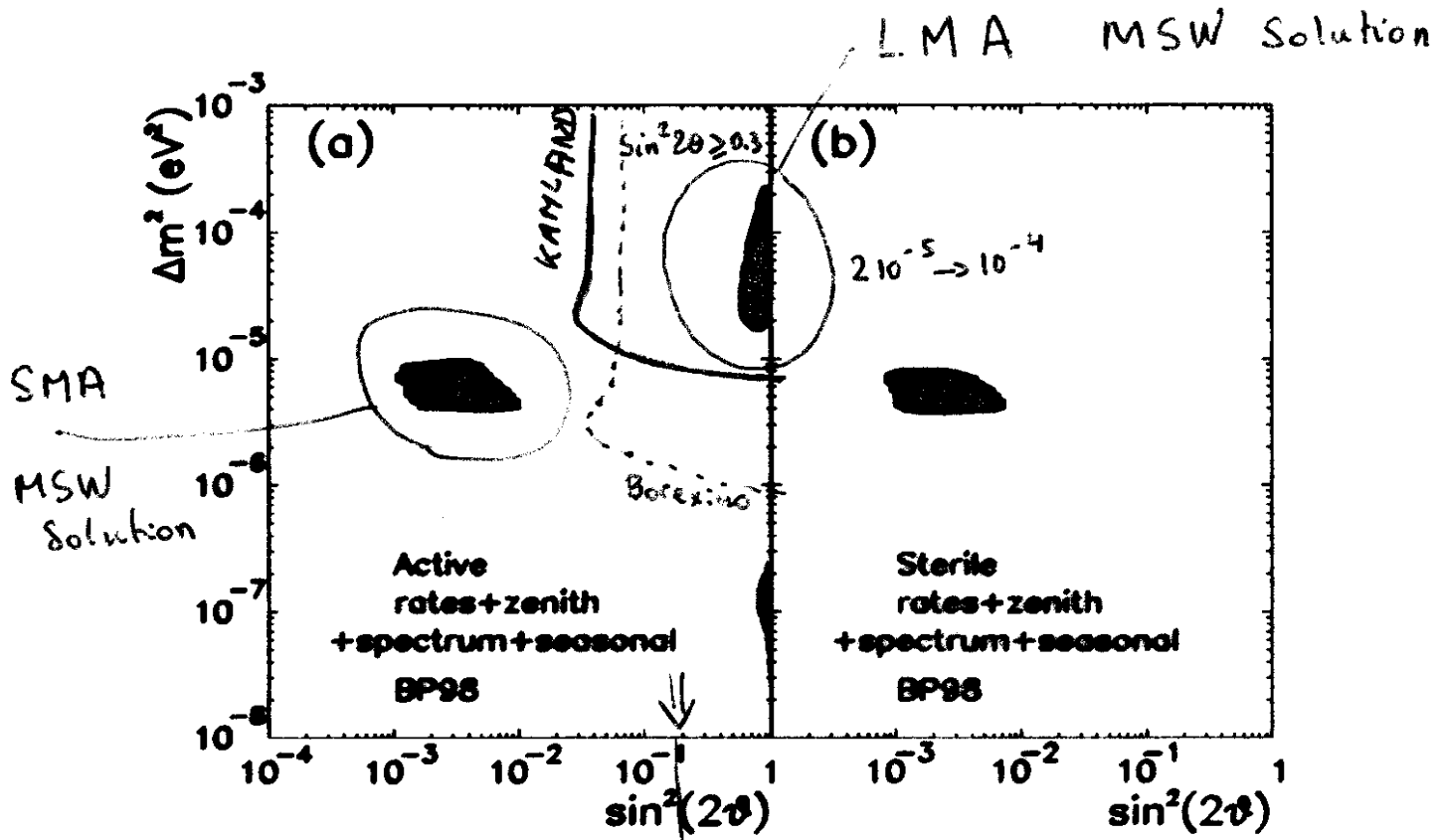


FIG. 8. Allowed regions in  $\Delta m^2$  and  $\sin^2 \theta$  from the measurements of the total event rates at the Chlorine, Gallium and Super-Kamiokande (708-day data sample) combined with the zenith angle distribution observed in Super-Kamiokande, the recoil energy spectrum and the seasonal dependence of the event rates, for active-active oscillations (a) and active-sterile oscillations (b). The darker (lighter) areas indicate 90% (99%) CL regions. Best-fit points in each region are indicated by a star.

MSW + LMA Solution → CP Violation at  $\nu$  FACT!

we will know in a few years from

- day-night effects in atm. neutrinos
- KAMLAND + BOREXINO (Reactor  $\bar{\nu}_e$ )

Donini et al. arXiv:1909.254

Baseline detector

$$\Delta m_{12}^2 = 10^{-4} \text{ eV}^2$$

$$E_\mu = 20 \text{ GeV}$$

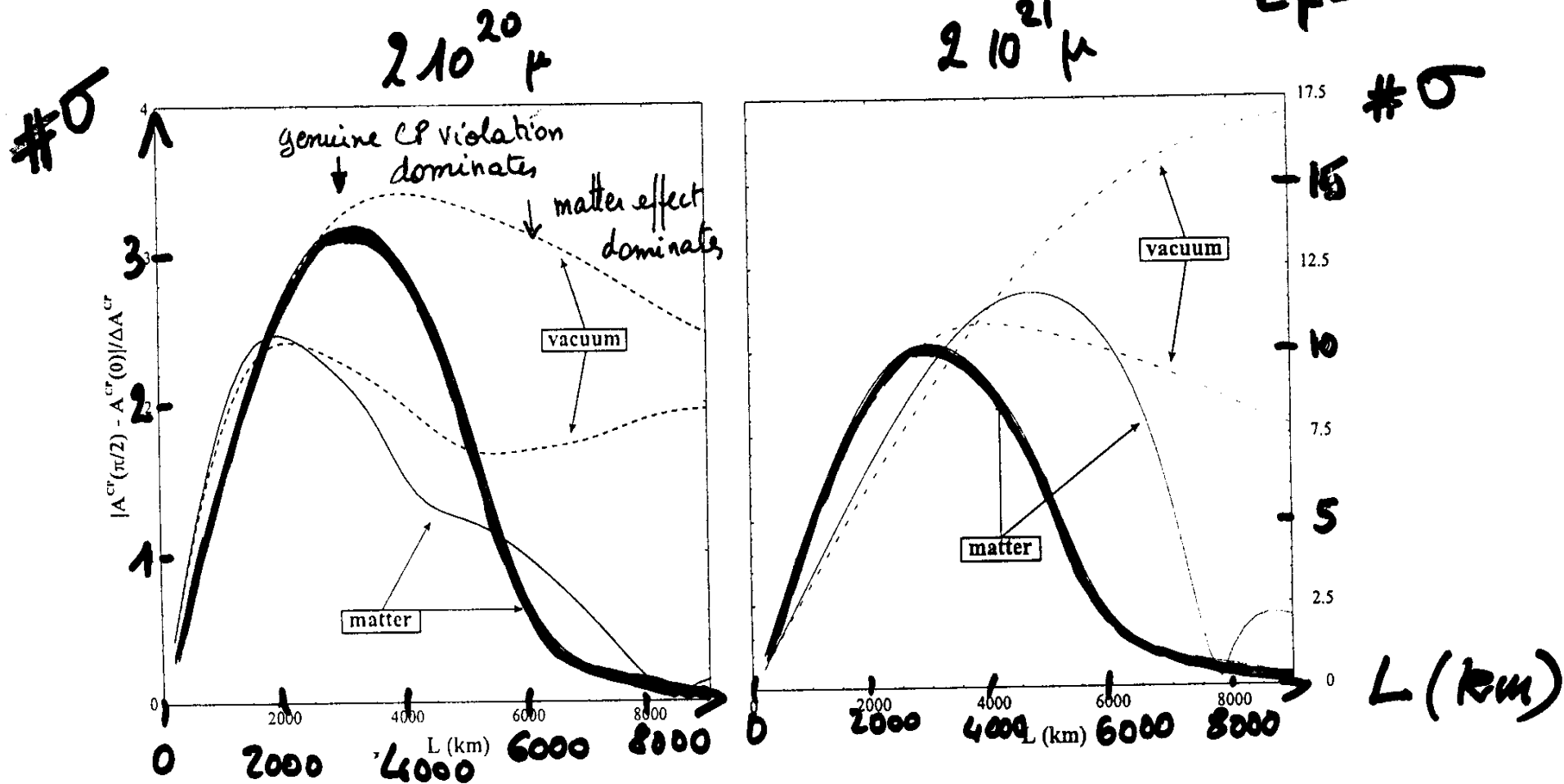


Figure 1: Signal over statistical uncertainty for  $|\bar{A}_{e\mu}^{CP}(\pi/2) - \bar{A}_{e\mu}^{CP}(0)|$  as a function of distance. Continuous (dashed) lines correspond to matter (vacuum) oscillations. In the left side, lower and upper curves correspond to  $E_\mu = 10, 20 \text{ GeV}$  for  $2 \times 10^{20}$  useful muons/year. In the right the same is depicted for  $E_\mu = 20, 50 \text{ GeV}$  and  $2 \times 10^{21}$  useful muons/year. The chosen CKM parameters are as described in the text.

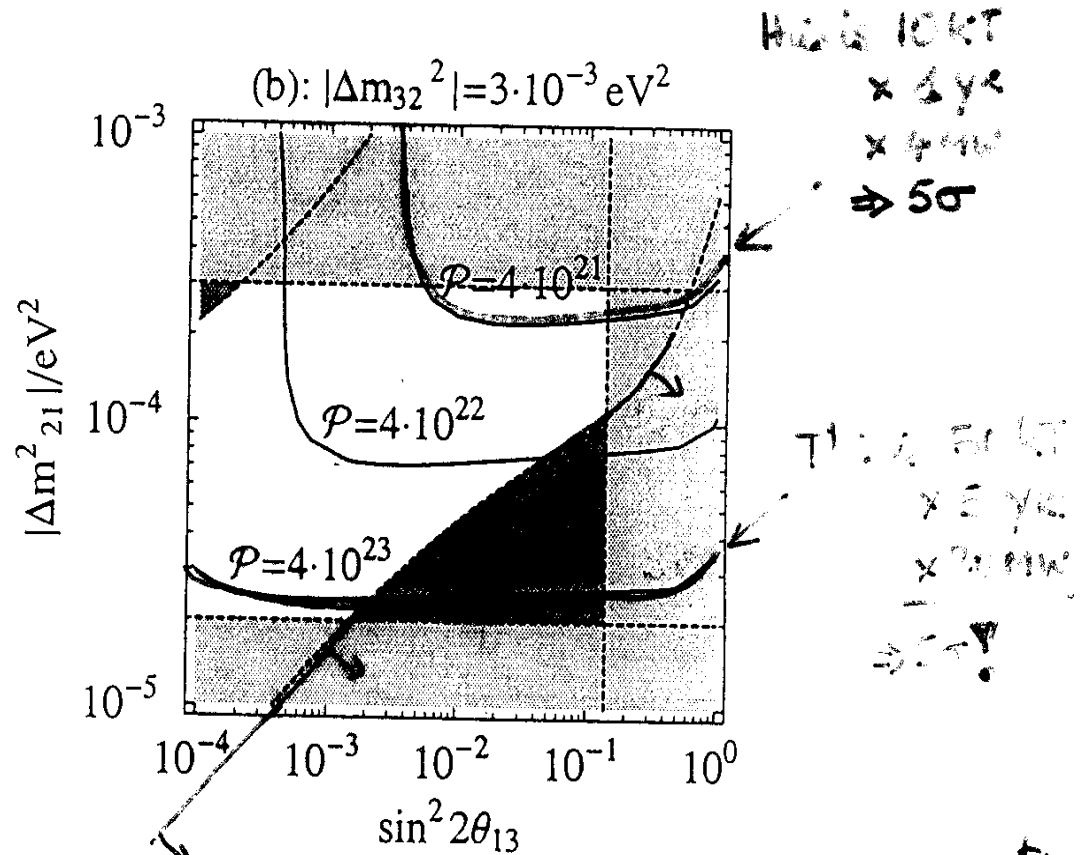
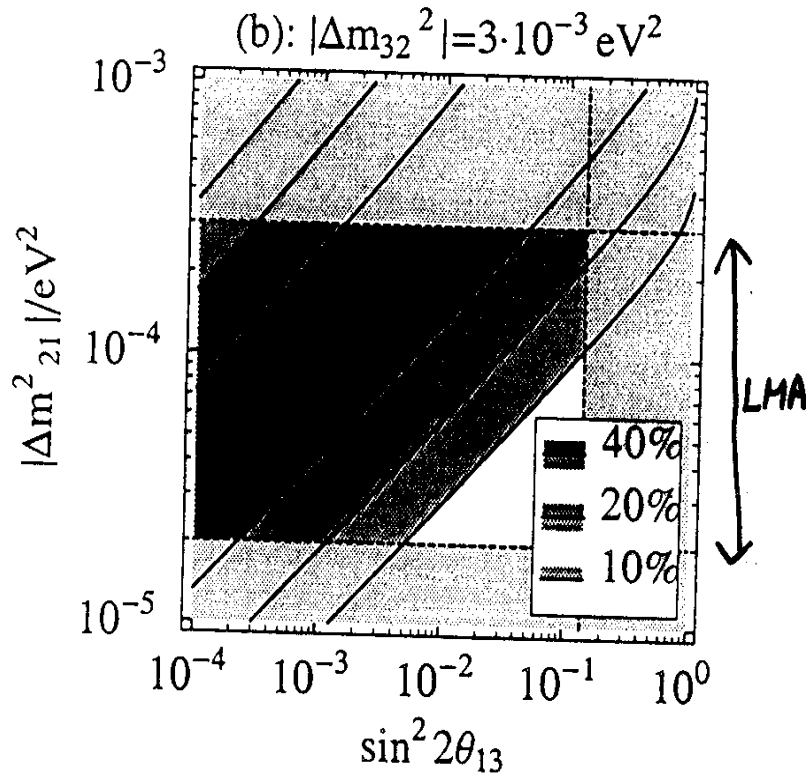


$P = N_p \cdot NKT \cdot \sin^2 \delta$  necessary to obtain  $5\sigma$   
 event counting, no use made of spectrum or polarization  
 no background.

MATTER ASYMMETRY HAS DIFFERENT  
 DEPENDENCE UPON DISTANCE  
 $\Rightarrow$  COMPARE TWO LONG BASELINES

$$A_{CP} = \frac{\nu_e \rightarrow \nu_\mu - \bar{\nu}_e \rightarrow \bar{\nu}_\mu}{\nu_e \rightarrow \nu_\mu + \bar{\nu}_e \rightarrow \bar{\nu}_\mu}$$

at 3000 km  $\downarrow$



below this line matter asymmetry  $>$  CP asymmetry  
 A. ROMANINO (after VFACT 99)

# MATTER EFFECTS

$$\nu + \textcircled{e, N} \xrightarrow{\text{matter}} \nu + \textcircled{e, X}$$



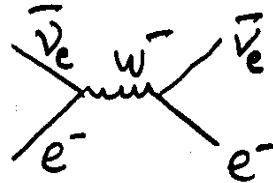
is the same for all neutrinos  $\rightarrow$  diagonal no effect

$$\nu_e + e^- \rightarrow \nu_e + e^-$$



add  $\nu_e \rightarrow \nu_e$  transition  
(forward Amplitude)

$$\bar{\nu}_e + e^- \rightarrow \bar{\nu}_e + e^-$$

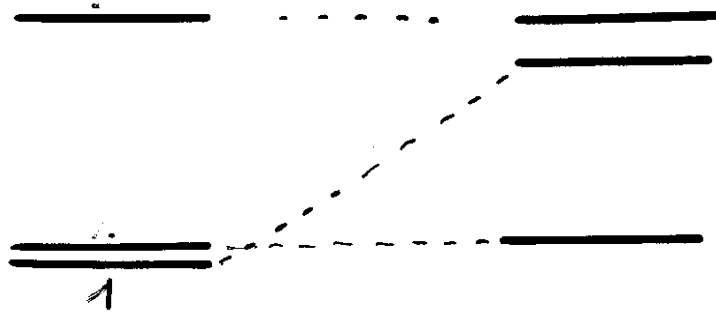


$$A = \pm G_F 2\sqrt{2} \cdot N_e \cdot E_\nu$$

$$H_{\nu_e \nu_e} = \frac{1}{2P_\nu} \left\{ U \begin{pmatrix} m_1^2 & & \\ & m_2^2 & \\ & & m_3^2 \end{pmatrix} U^\dagger + \begin{pmatrix} A & & \\ & 0 & \\ & & 0 \end{pmatrix} \right\}$$

$$H_{\bar{\nu}} = \frac{1}{2P_\nu} \left\{ U^* \begin{pmatrix} m & & \\ & m & \\ & & m \end{pmatrix} U^T - \begin{pmatrix} A & & \\ & 0 & \\ & & 0 \end{pmatrix} \right\}$$

⇒ New eigenstates, large modification of  $\Delta m^*$  and  $\theta^*$



LEVEL CROSSING (S)

+ POSSIBLE RESONANCE (S)

AT  $10 \text{ GeV} \approx E_\nu$  RESONANCE FOR

$$\Delta m^2 = 3 \cdot 10^{-3} \text{ eV}^2 !$$

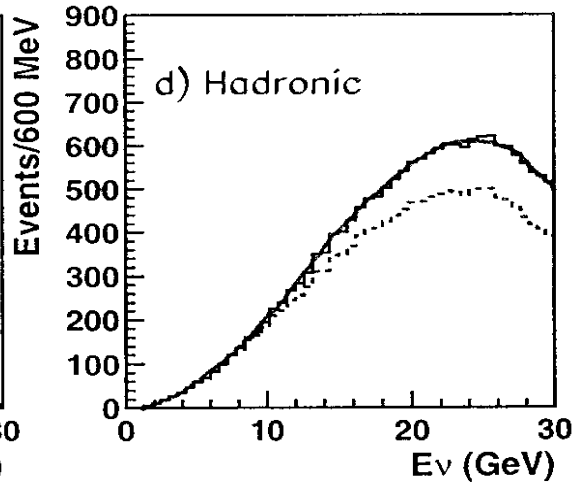
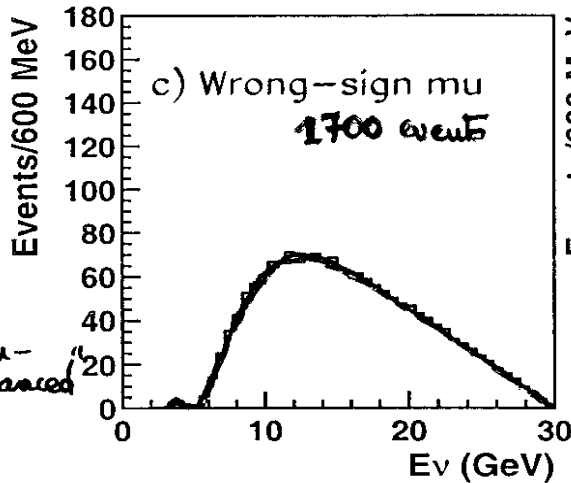
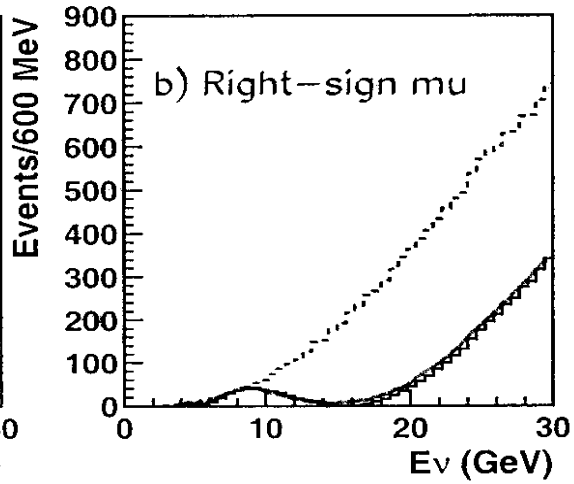
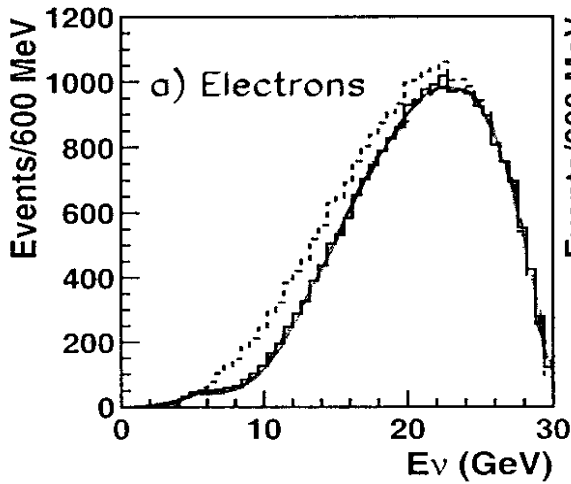
→ ENERGY AND DISTANCE - DEPENDENT  
MODIFICATION OF TRANSITIONS

→ FAKE CP ASYMMETRY  $\nu_e \rightarrow \nu_\mu \neq \bar{\nu}_e \rightarrow \bar{\nu}_\mu$

REQUIRES { DIFFERENT SIGNS  $\nu_e$  and  $\bar{\nu}_e$  (switch  $\mu^- \leftrightarrow \mu^+$ , easy)  
[ DIFFERENT LENGTHS

# Oscillated Spectra

$$\mu^+ \text{ beams} \rightarrow \nu_e \bar{\nu}_\mu$$



10 kT 500 km

$$\sin^2 \theta_{23} = 0.5$$

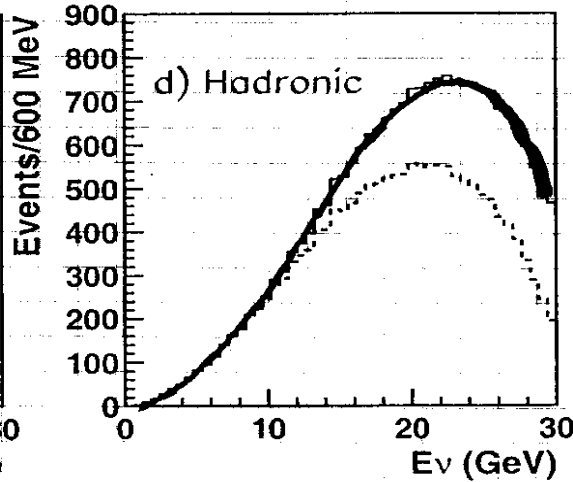
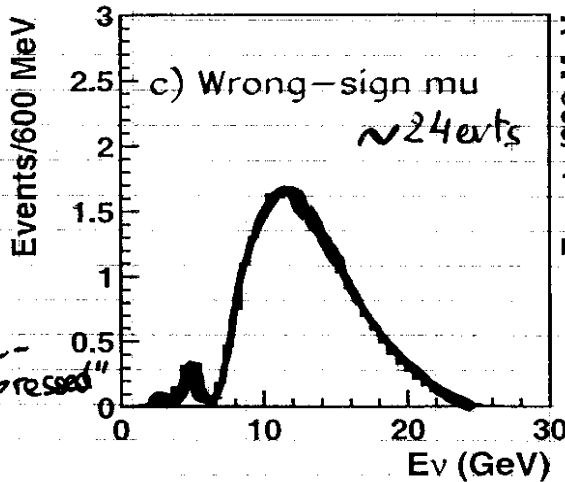
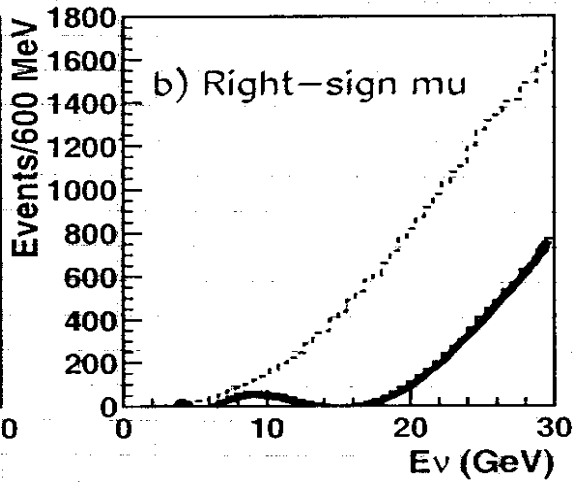
$$\sin^2 \theta_{13} = 0.025$$

Campanelli et al  
(FERMILAB)

# Oscillated Spectra

$\mu^-$  beams  $\rightarrow \bar{\nu}_e \nu_\mu$

--- no oscillations  
 — oscillations + matter effects



$\bar{\nu}_e \rightarrow \bar{\nu}_\mu$   
 is "matter-suppressed"

10 kT: 6500 km (BNL  $\rightarrow$  Gran Sasso)

$\sin^2 \theta_{23} = 0.5$  ( $\theta_{23} = 45^\circ$ )  
 $\sin^2 \theta_{13} = 0.025$  ( $\theta_{13} = 9^\circ$ )

companelli Bruno Rubbia  
 (ICARUS)

LONG BASELINE  $\sim 700 \text{ km}$



Very precise measurements of

- $\theta_{13}$  ( $\nu_e \rightarrow \nu_\mu$ )
- $\theta_{23}$  ( $\nu_\mu$  disappearance)
- $\Delta m_{23}^2$

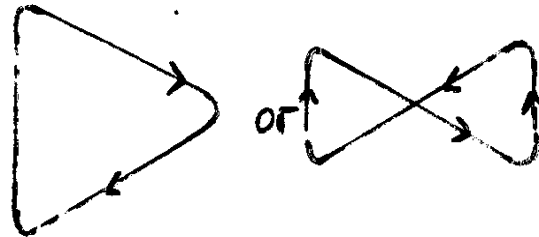
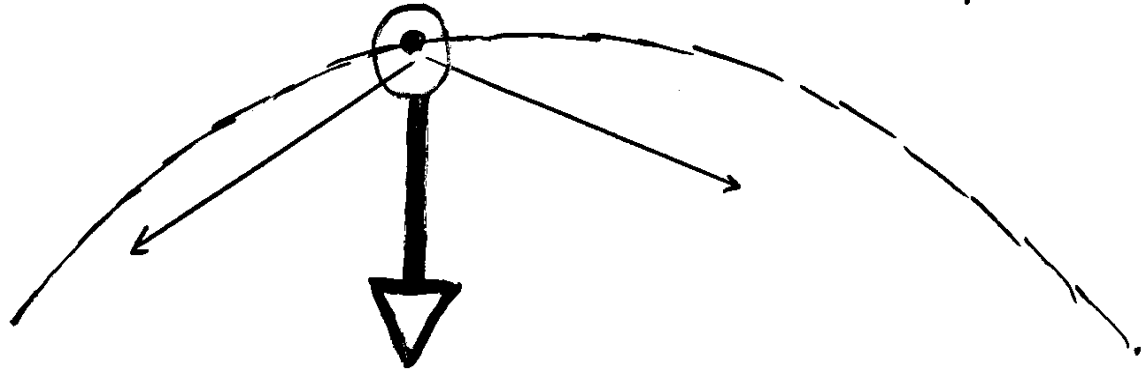
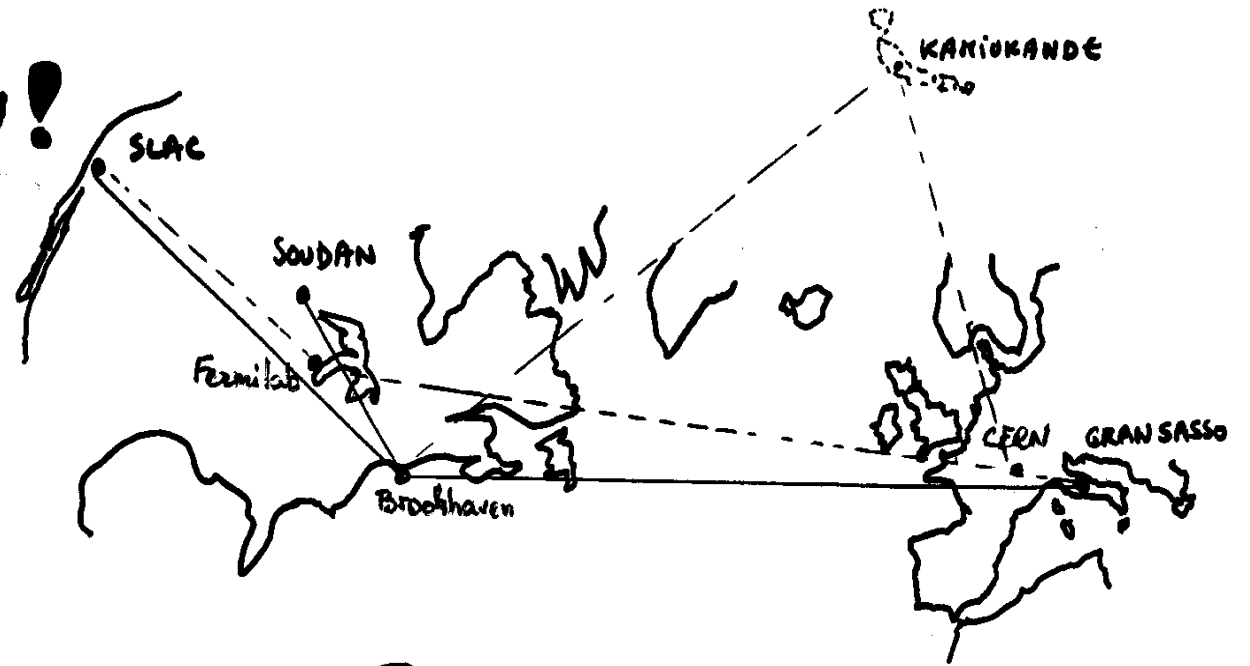
VERY LONG BASELINE ( $\geq 3000 \text{ km}$ )



matter oscillations (MSW)

CP, T violation!

# A WORLD MACHING!

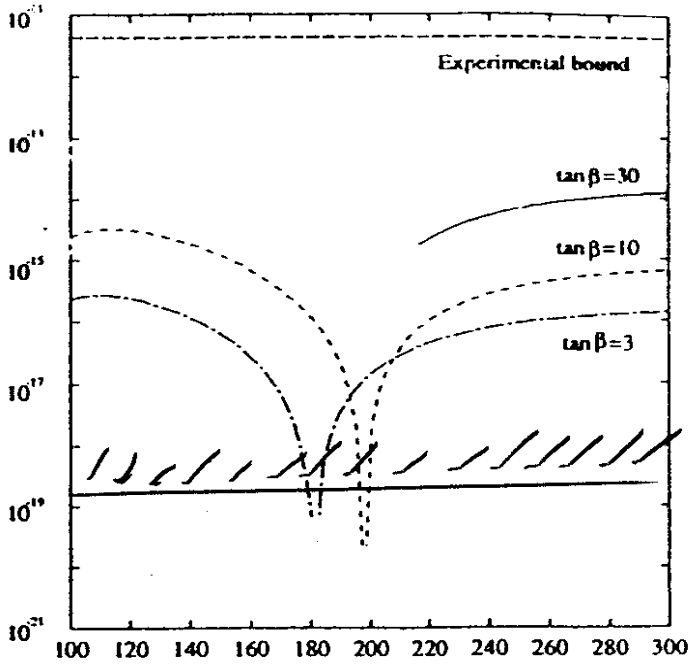
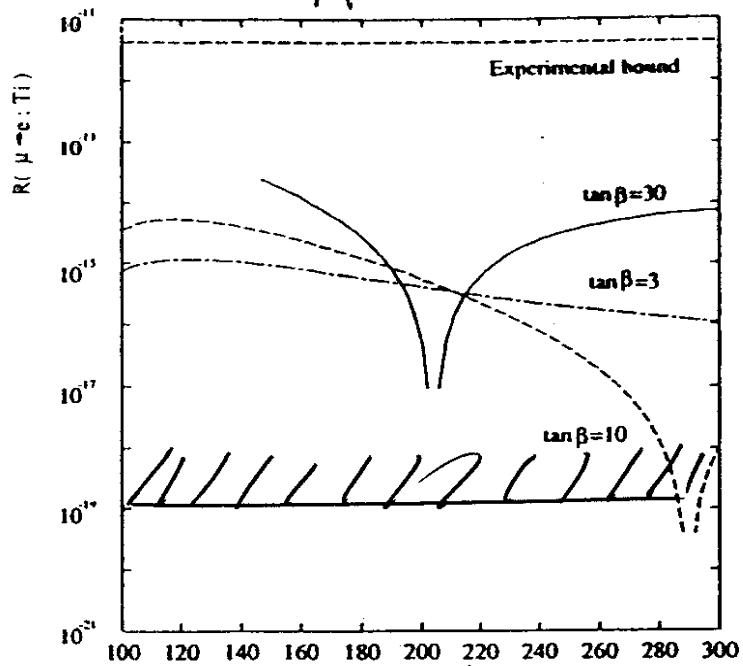


triangle or "Bowtie"

$\mu > 0$

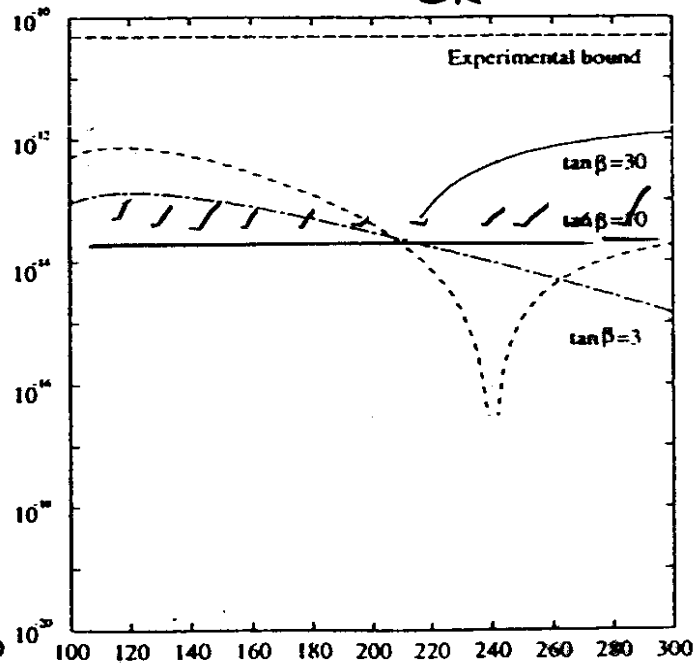
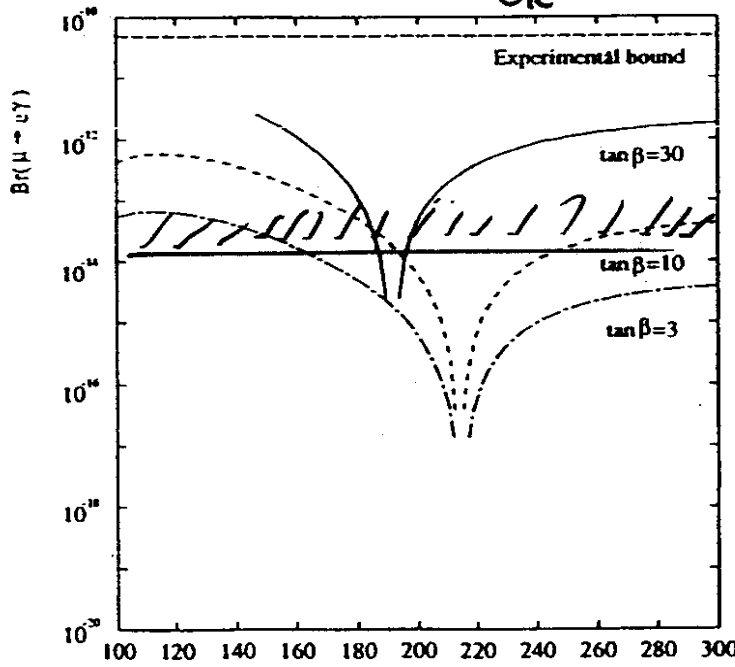
$\mu < 0$

$|\mu \tilde{\tau}_i \rightarrow e^- \tau_i|$



$m_{\tilde{e}_R}$  (GeV)

$m_{\tilde{e}_R}$  (GeV)



$m_{\tilde{\tau}_i}$  (GeV)

$m_{\tilde{\tau}_i}$  (GeV)

$|\mu^- \rightarrow e^- \gamma|$

$\mu \rightarrow e$  TRANSITIONS FROM SUSY LOOPS.

Hall, Barbieri, Hisano



# V-FACT UPGRADE TO PRECISION MUON COLLIDER

- more cooling
- $\mu^+$  and  $\mu^-$  SIMULTANEOUSLY  
(OR WITHIN  $\lesssim 1 \mu\text{s}$ )
- ONE BUNCH OF  $\mu^+$  and  $\mu^-$
- COLLIDER.

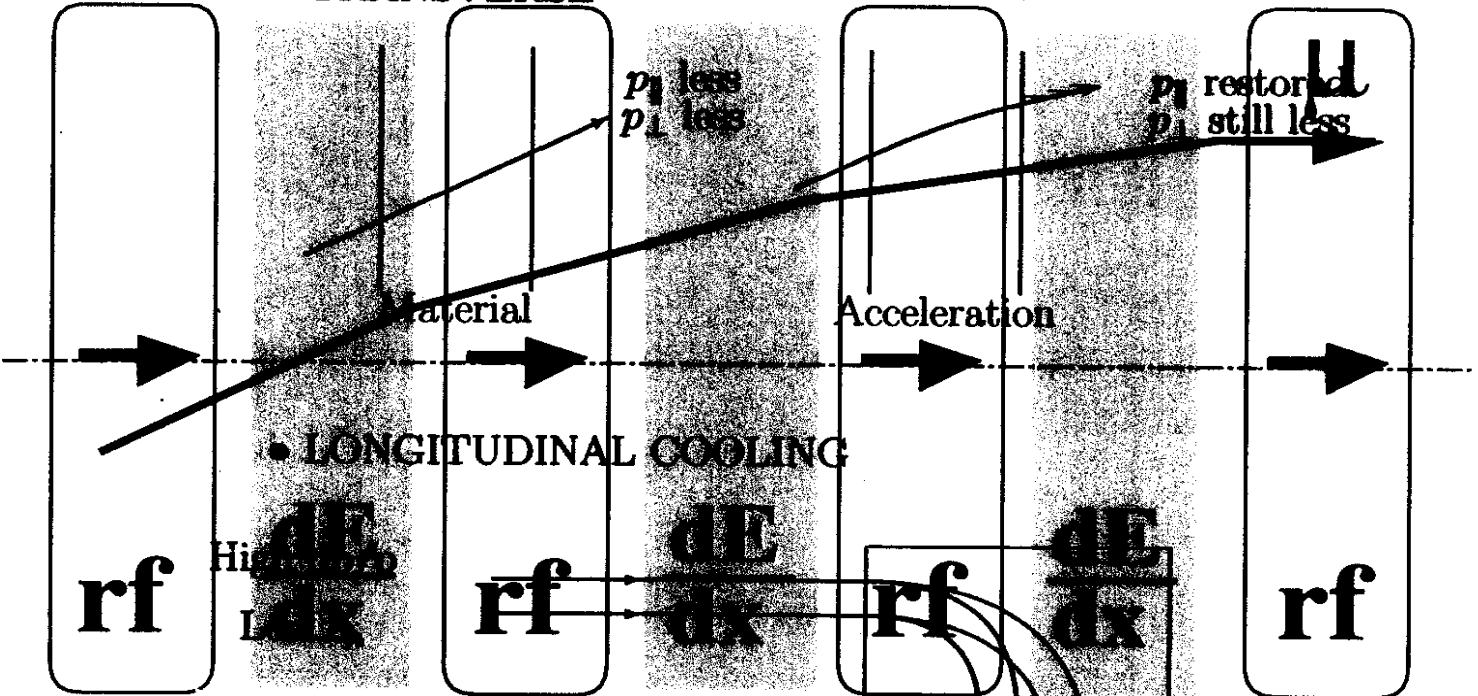
LIKE ALL lepton colliders in energy range  
100 - 1000 GeV, physics case very dependent  
ON FINDINGS FROM LHC

- HIGGS FACTORY  $E_{CM} = M_H \approx E [110 - 140 \text{ GeV}]$
- SUSY HIGGS FACTORY  $E_{CM} \approx M_A, M_H$

# Ionization Cooling

## IONIZATION COOLING

• TRANSVERSE



• LONGITUDINAL COOLING

Low  $dp/p$   
High  $\epsilon_n$

$$\frac{d\epsilon_n}{dx} = - \frac{1}{\beta^2} \frac{d\epsilon_p}{dx} \frac{\epsilon_n}{E_p} + \frac{\beta_{\perp} \cdot C}{\text{Magnet } E_p m_p \chi_0}$$

Reduce capacitance  $3 \cdot 10^{-5}$  !

but  $\beta_{\perp}$  = localisation au point de  $\frac{dE}{dx}$   
**INCREASE  $\sigma_x \sigma_y$  → decrease  $C$ .**

⇒ Luminosity  $\propto B^2$  at last cooling stage!

Baseline parameters for high- and low-energy muon colliders:  
Higgs/year assumes a cross section  $\sigma = 5 \times 10^4$  fb; a Higgs width  $\Gamma = 2.7$  MeV;  
1 year =  $10^7$  s. (From the muon collider collaboration)

CoM energy (TeV)	3	0.4		0.1	
$p$ energy (GeV)	16	16		16	
$p$ 's/bunch	$2.5 \times 10^{13}$	$2.5 \times 10^{13}$		$5 \times 10^{13}$	
Bunches/fill	4	4		2	
Rep. rate (Hz)	15	15		15	
$p$ power (MW)	4	4		4	
$\mu$ /bunch	$2 \times 10^{12}$	$2 \times 10^{12}$		$4 \times 10^{12}$	
$\mu$ power (MW)	28	4		1	
Wall power (MW)	204	120		81	
Collider circum. (m)	6000	1000		350	
$\langle B \rangle$ (T)	5.2	4.7		3	
$\delta p/p$ (%)	0.16	0.14	0.12	0.01	0.003
6-D $\epsilon_{6,N}$ ( $\pi\text{m}$ ) <sup>3</sup>	$1.7 \times 10^{-10}$	$1.7 \times 10^{-10}$	$1.7 \times 10^{-10}$	$1.7 \times 10^{-10}$	$1.7 \times 10^{-10}$
Rms $\epsilon_n$ ( $\pi$ mm-mrad)	50	50	85	195	290
$\beta^*$ (cm)	0.3	2.6	4.1	9.4	14.1
$\sigma_z$ (cm)	0.3	2.6	4.1	9.4	14.1
$\sigma_r$ spot ( $\mu\text{m}$ )	3.2	26	86	196	294
$\sigma_\theta$ IP (mrad)	1.1	1.0	2.1	2.1	2.1
Tune shift	0.044	0.044	0.051	0.022	0.015
$n_{\text{turns}}^{\text{effective}}$	785	700	450	450	450
Luminosity ( $\text{cm}^{-2}\text{s}^{-1}$ )	$7 \times 10^{34}$	$10^{33}$	$1.2 \times 10^{32}$	$2.2 \times 10^{31}$	$10^{31}$
Higgs/year			$1.9 \times 10^3$	$4 \times 10^3$	$3.9 \times 10^3$

# LUMINOSITY CONSIDERATIONS

$$\mathcal{L} = f \cdot \frac{N_{\mu^+} \cdot N_{\mu^-}}{4\pi \sigma_x \sigma_y}$$

$$\sigma_x = \sqrt{\epsilon_x \beta_x^*}$$

- $\beta^*$  cannot usefully be smaller than BUNCH LENGTH.
- $f = \# \text{ collisions / second}$

$$= \left( \frac{\tau_{\mu} \cdot \beta \gamma c}{2\pi \langle R \rangle} \right) \times \# \text{ fills / second.}$$

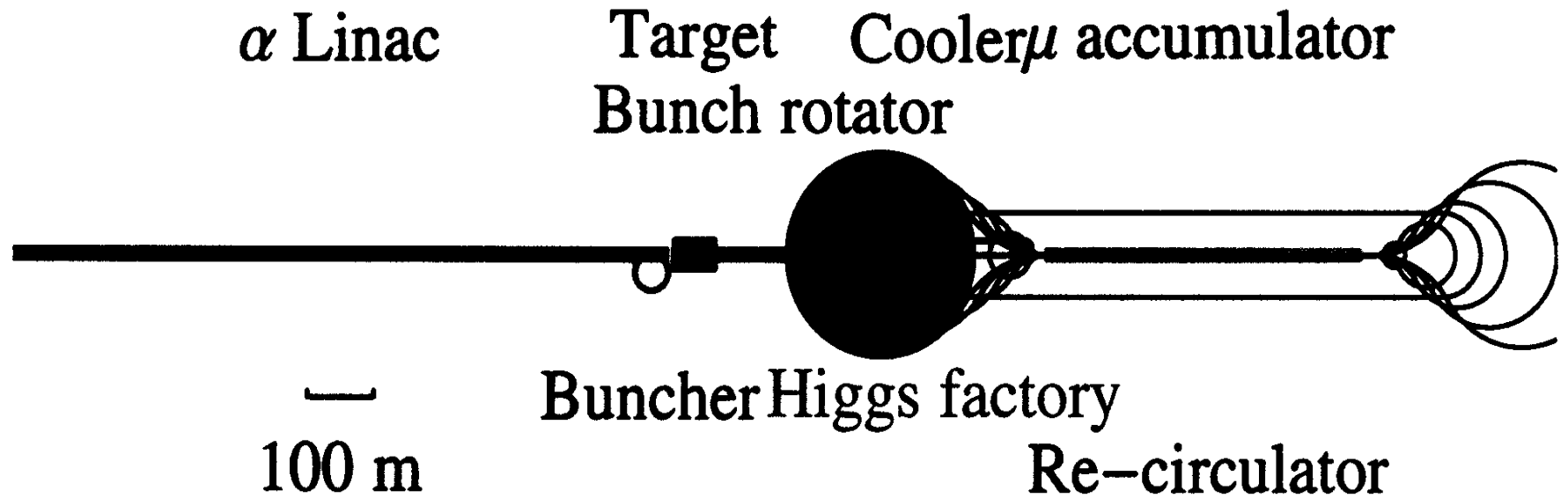
lifetime expressed  
in # turns in collider  
 $\Rightarrow$  Strong B field wiring.

$\Rightarrow$  For given  $\# \mu^\pm / \text{second}$ , optimise  $\mathcal{L}$ , without  
reaching beam-beam limit [WHICH MIGHT BE  
MUCH HIGHER THAN  
IN  $e^+e^-$  RINGS]  
(then beams blow up and luminosity  $\downarrow$ .)


$\Rightarrow$  more  $\mu$ /bunch at lower frequency

typical 15 Hz  $4 \cdot 10^{12}$   $\mu$ /bunch

$\rightarrow$  NEED BOTH SIGNS EQUALLY  
[ $\alpha$  instead of  $p$ ?]



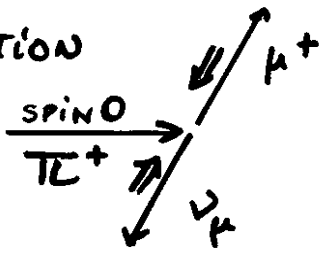
Tentative layout of a Higgs factory

BEWARE: MARYEL! 

# ENERGY CALIBRATION

1. MUON, are naturally POLARIZED

PARITY VIOLATION



SPINO  
 $\pi^+$

$\mu^+$   
 $\mu^-$

$\Rightarrow$  100% LEFT-HANDED  $\mu^+$   $\pi^+$   $\pi^0$

BOOST  $\rightarrow P_L^{\mu^+} = -28\%$  LAB

[MOMENTUM SELECTION  $\rightarrow P_L^{\mu^+} \approx -70\%$

2. POLARIZATION IS HARD TO DESTROY

3. POLARIZATION PRECESSES IN STORAGE RING

$$\# \text{ PRECESSIONS/TURN} = \nu_s = \frac{E_\mu}{m_\mu} \cdot \frac{g-2}{2} = \frac{E(\text{GeV})}{90.6223(6)}$$

200 times slower than  $e^+$ !  $\leftarrow$   $m_\mu$   $\nearrow \sim \frac{\alpha}{2\pi}$

SLOW, EXPLAINS 2

4.  $\mu^+ \rightarrow e^+ \nu \bar{\nu}$  (PARITY VIOLATION, AGAIN)

GIVE NATURAL POLARIMETER  
 $\hookrightarrow E_\mu$

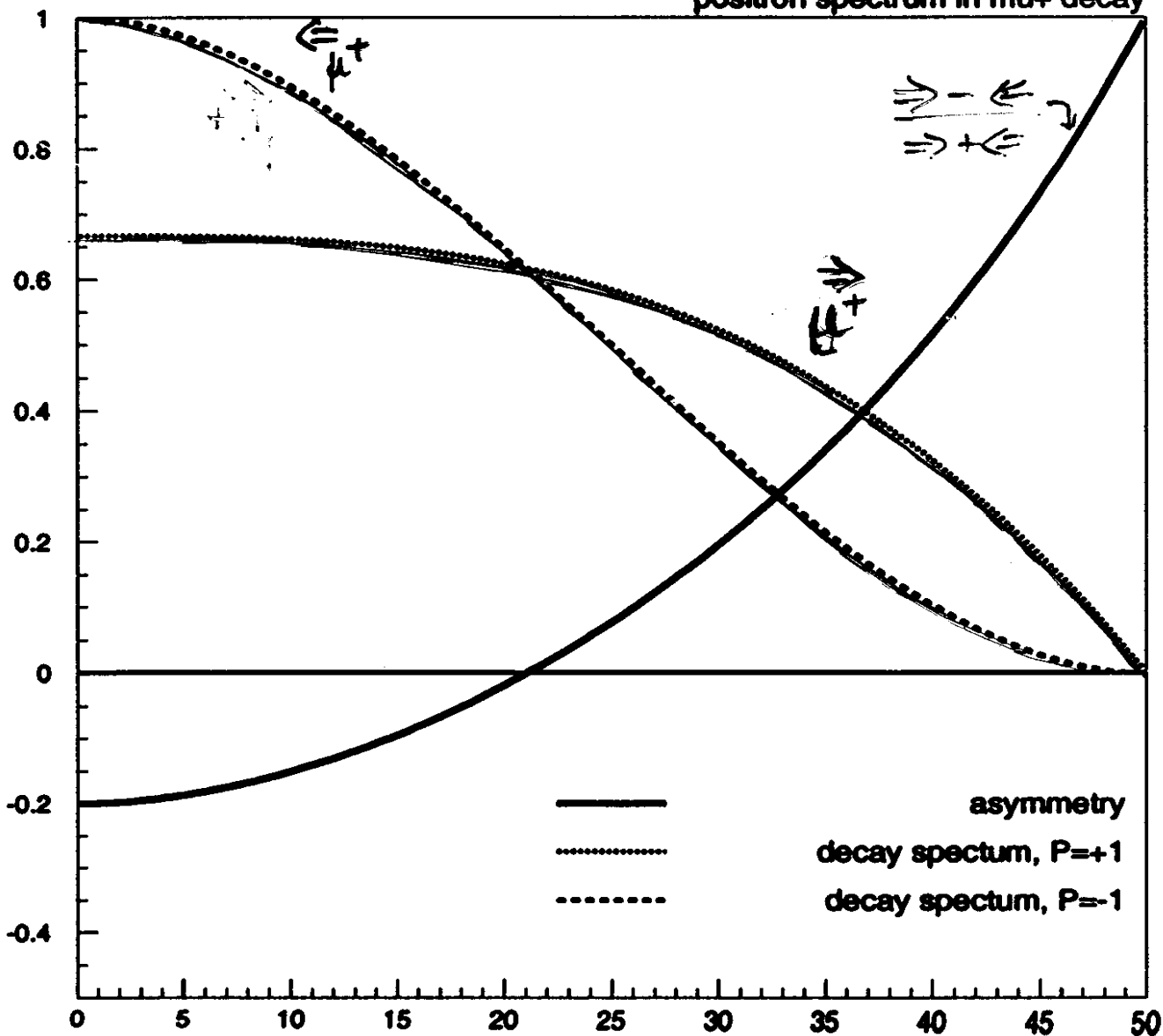
$$4 \cdot 10^{12} \mu^+ \rightarrow 4 \cdot 10^3 e^+ / \text{turn}$$

$$\rightarrow \frac{2 \cdot 10^6}{\text{turn}} e^+ \text{ in } \begin{cases} 1 \text{ m decay length} \\ 30.40 \text{ GeV} \end{cases}$$

$$\gamma = \frac{E_\mu}{m_\mu} \times \frac{g-2}{2} = 0.5 @ 45 \text{ GeV}$$

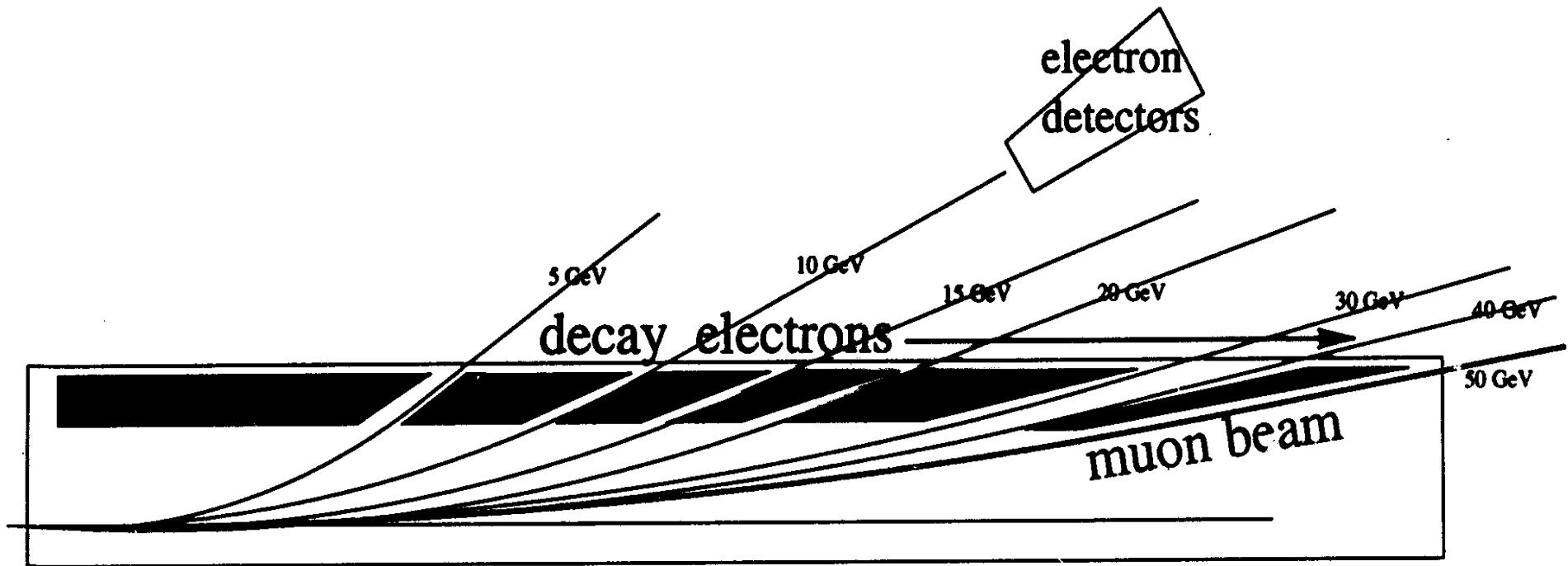
50 GeV MUONS

positron spectrum in  $\mu^+$  decay



$P_{e^+}$

# muon polarimeter



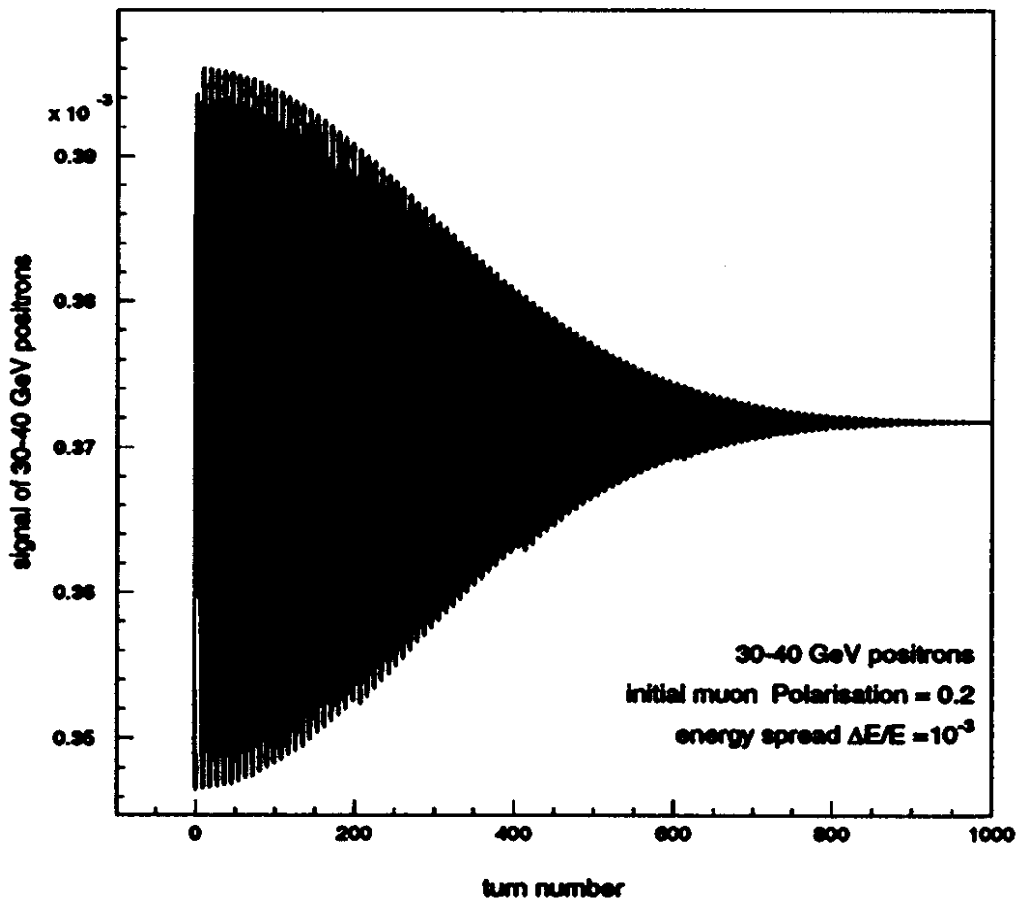
First magnet after straight section



Oscillation by turn provide

Fourier Transform of energy distribution:

$$\frac{N(T)[30,40 \text{ GeV}]}{N_p(T)}:$$



amplitude	→	beam polarisation
frequency	→	beam energy
decrease with time	→	energy spread

→ By fitting the polarisation precession as function of turn number, one can extract the beam energy with a precision of a few  $10^{-6}$  for each MUON fill! (limited by present precision on  $g - 2$ !)

→ can also extract energy spread to similar precision (Important for extraction of width and cross-section) from decrease of polarisation with turn number.

→ since there are  $10^8$  fills per year, energy spectrum is exceedingly well known

(systematics remain to be studied) MUON collider is a perfect machine for study of narrow resonances, and thresholds.

# COLLIDER PARAMETERS

AMERICAN  
MUON  
COLLABORATION

c of m Energy	GeV	3000	400	100		
p Energy	GeV	16	16	<u>16</u>		
p's/bunch	$10^{13}$	2.5	2.5	5		
bunches/fill		4	4	2		
rep rate	Hz	15	15	<u>15</u>		
p power	MW	4	4	4		
$\mu$ /bunch	$10^{12}$	2	2	4		
$\mu$ power	MW	28	4	1		
wall power	MW	204	120	81		
collider circ	m	6000	1000	<u>300</u>		
min depth ( $\nu$ )	m	300	.7	.01		
rms dp/p	%	.16	.14	.12	.01	.003
rms $\epsilon_n$	$\pi$ mm mrad	50	50	85	195	280
$\beta^*$	cm	0.3	2.3	4	9	13
$\sigma_z$	cm	0.3	2.3	4	9	13
$\sigma_r$ spot	$\mu m$	3.2	24	82	187	270
tune shift		0.043	0.043	0.05	0.02	.015
luminosity	$cm^{-2} sec^{-1}$	$5 \cdot 10^{34}$	$10^{33}$	$1.2 \cdot 10^{32}$	$2 \cdot 10^{31}$	$10^{31}$
c of m dE/E	$10^{-5}$	80	80	80	7	2
Higgs/year	$10^3 year^{-1}$			1.6	4	4

cf TESLA

$2 \cdot 10^{34}$

cf LEP

$2 \cdot 10^{30}$

cf CLIC

$10^{35}$

# PHYSICS WITH MUON COLLIDERS

1. MUON COLLIDER CAN DO <sup>(ALMOST)</sup> EVERYTHING  
AN  $e^+e^-$  COLLIDER CAN DO.

- ⊖ LUMINOSITY IN PRESENT DESIGNS  
IS LOWER BY FACTOR  $\approx 10$ .  
more luminosity welcome.
- ⊖ NO  $\gamma$ - $\gamma$  COLLISIONS
- ⊖ BACKGROUNDS FROM DECAY ELECTRONS  
AND STRAY MUONS ARE MORE  
DIFFICULT TO HANDLE.  
BUT LESS THAN LHC, ACCORDING TO  
AMERICAN MUON COLLABORATOR J. STUMER.
- ⊖ NEUTRINO RADIATION
- ⊖ POLARIZATION IS  $\sim 20\%$  FOR BOTH BEAMS  
VS  $80\%$  FOR  $e^-$   
difficult for  $e^+$

2. MUON COLLIDER CAN DO THINGS  
AN  $e^+e^-$  COLLIDER CANNOT DO

+

COUPLING TO HIGGS  $\approx m_\mu$  vs  $m_e$

$$\Rightarrow \sigma(\mu^+\mu^- \rightarrow H) = 40000 \sigma(e^+e^- \rightarrow H)$$

USABLE IF  $M_H \lesssim 2M_W$  (likely, not certain)

+

ENERGY RESOLUTION CAN BE

EXCELLENT  $\sigma_E/E \approx 10^{-3}$   
NO BEAMSTRAHLUNG  $\rightarrow 3 \cdot 10^{-5} \text{ ?}$

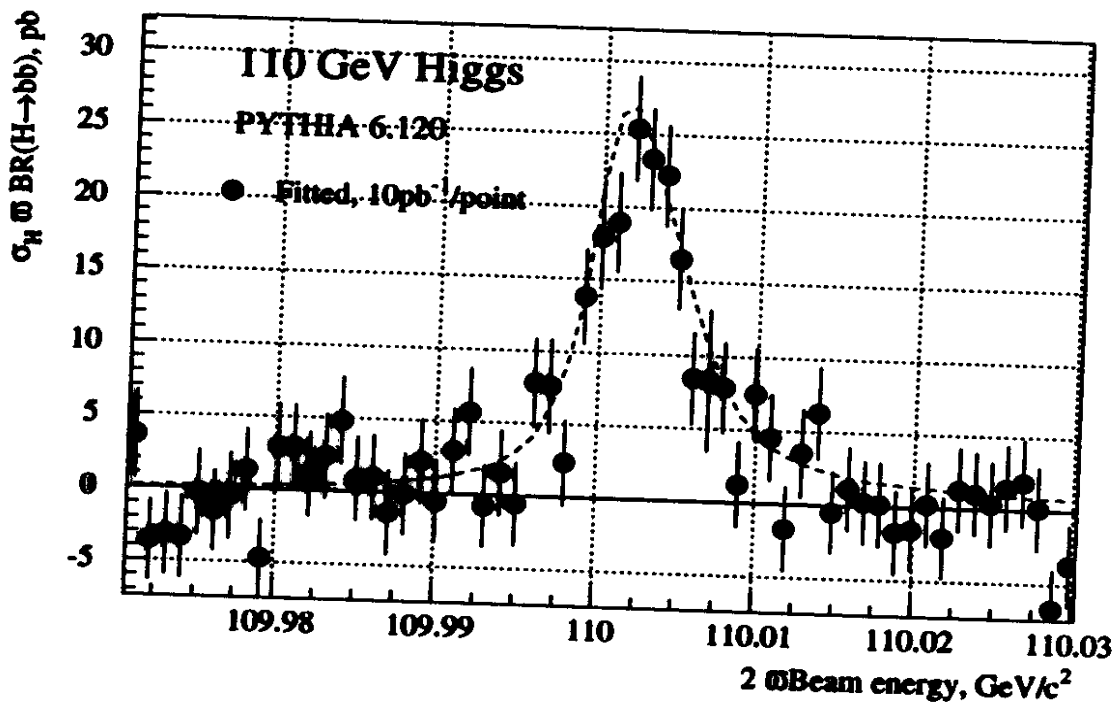
+

ENERGY CALIBRATION  $\approx$  INFINITELY  
PRECISE.

$\sim$

$\mu \neq e \rightarrow$  of course better for  $\tilde{\mu}, \tilde{\mu}^*$

FOR LIGHT HIGGS ( $m_H \lesssim 140 \text{ GeV}$ )  
 DIRECT  $\mu^+ \mu^- \rightarrow H$  production



measurements of Higgs  
 mass  $\pm 0.1 \text{ MeV}$   
 Width  $\pm 0.3 \text{ MeV}$   
 cross-section  $\pm 1\%$

}

FOR SM HIGGS.  
 $\sim 4000 \mu\mu \rightarrow H \rightarrow b\bar{b}$  / year  
 more for MSSM.

$\rightarrow$  VERY STRONG CONSTRAINTS on Higgs couplings, SUSY phase space.

# PRECISION MEASUREMENTS OF HIGGS BOSON PROPERTIES

WOULD ALLOW

- TEST OF HIGGS MECHANISM
- TEST OF EXISTENCE OF OTHER HIGGS:

ex. in SUPER SYMMETRY,  $\exists$   $h$ ,  $A$ ,  $H$   
 $m_h \leq 130$  GeV      CP odd scalar      CP even scalar

$\Rightarrow$  Pin down predictions for masses and couplings of  $H$  and  $A$ .

STEP 2'

BUILD

PRECISION MUON COLLIDER 2

$$\sqrt{s} \gtrsim m_A.$$



- use polarization  $\leftarrow \Rightarrow$  vs  $\Rightarrow \Rightarrow$  to identify particles as scalars

- identify A and H as CP odd / CP even (KRAMLETal)

if eg  $\tilde{\nu}, \tilde{E}_1$  vs  $\tilde{E}_1, \tilde{E}_2$  production available

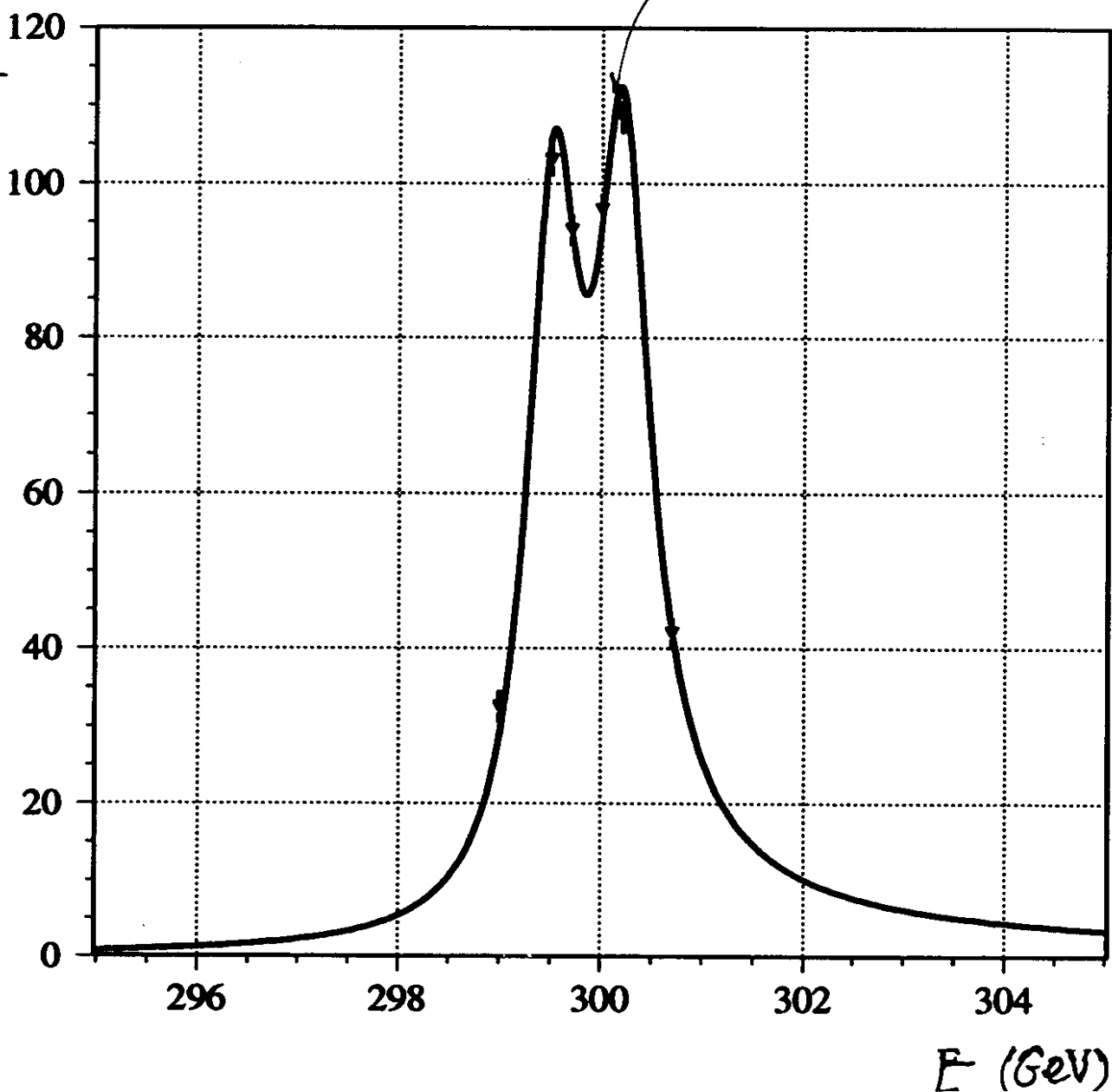
measure  $\Delta m_H \sim \Delta m_A \sim 20 \text{ GeV}$

$\Delta \Gamma_H \Delta \Gamma_A \simeq 100 \text{ GeV}$

- interference between H/A (C.P violation in Higgs sector)  $\sigma_{\text{peak}} \text{ to } \pm 1\%$

$m_A^{\text{Pole}} = 299.500$

$m_H^{\text{Pole}} = 300.193$

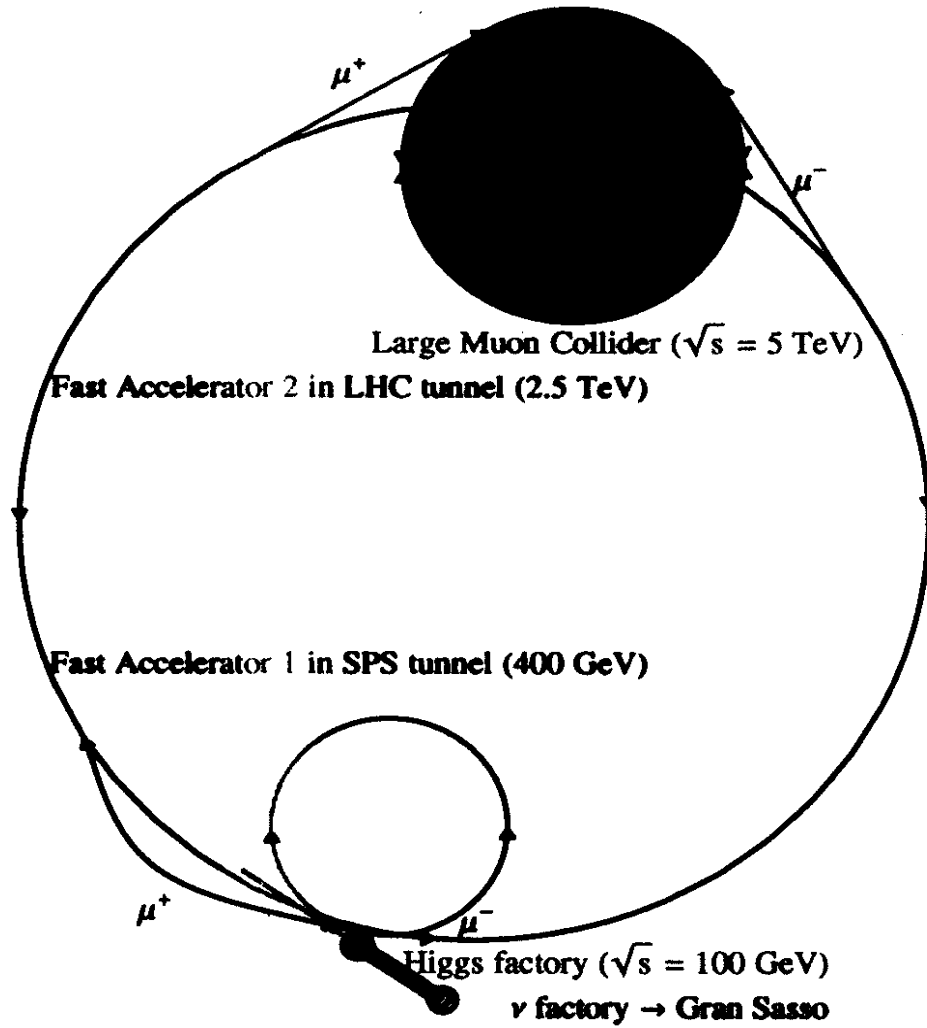


# **A THREE STEP SCENARIO**

## **3. High energy Frontier**

- aim: lepton collider at highest energies (7 TeV Ecm in LHC tunnel!)**
- strong points: rather straightforward after PMC, same virtues.**
- problems: neutrino radiation.**

# Possible layout of a MUON complex on the CERN site



# NEUTRINO RADIATION

# Particles produced by  $\nu$  interactions  $\propto E$

$\gamma$  cross-section  $\propto E$

$N(\text{beam size}) \approx \text{area reached} \propto E$

$\Rightarrow$  RADIATION  $\nearrow$  Like  $E^3!$   
 $\searrow$  like  $R^2$

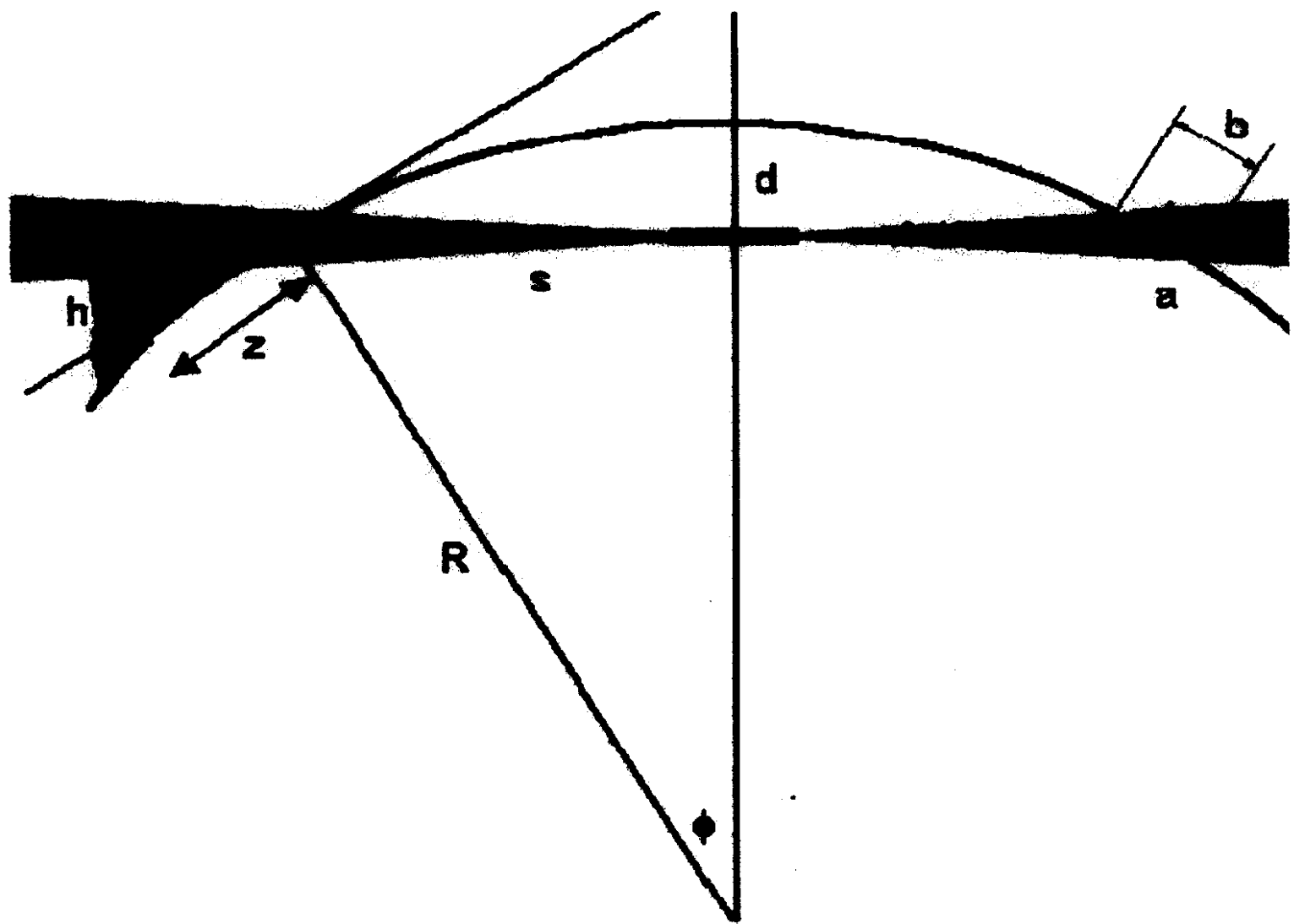
YES : RADIATION FROM NEUTRINO INT. PRODUCTS  
MUST BE TAKEN INTO ACCOUNT.

$\rightarrow$  Johnson / Rolandi / Silari.  
have verified and CONFIRMED  
AMERICAN STUDY.

FOR THE MOMENT  $\rightarrow$  LIMIT AT 4 TEV  
ECM

+ BUY LAND AT EXIT OF EARTH  
IN LINE WITH STRAIGHT SECTIONS

$E^4!$



$$s^2 = 2Rd - d^2$$

$$\sin \phi = s/R$$

$$h \cong z \tan \phi$$

$$\theta \sim 1/\gamma$$

$$a \cong 2 \theta s$$

$$b \cong e / \phi$$

E CoM	d (m)	s (km)	$\phi$	z (km)	h (m)	$\theta$	a (m)	b (m)
0.5 TeV	100	35	$5.6 \cdot 10^{-3}$	10	56	$424 \cdot 10^{-6}$	30	5300
4.0 TeV	500	80	$12.5 \cdot 10^{-3}$	10	125	$53 \cdot 10^{-6}$	8.5	680

Some typical geometrical features of the neutrino

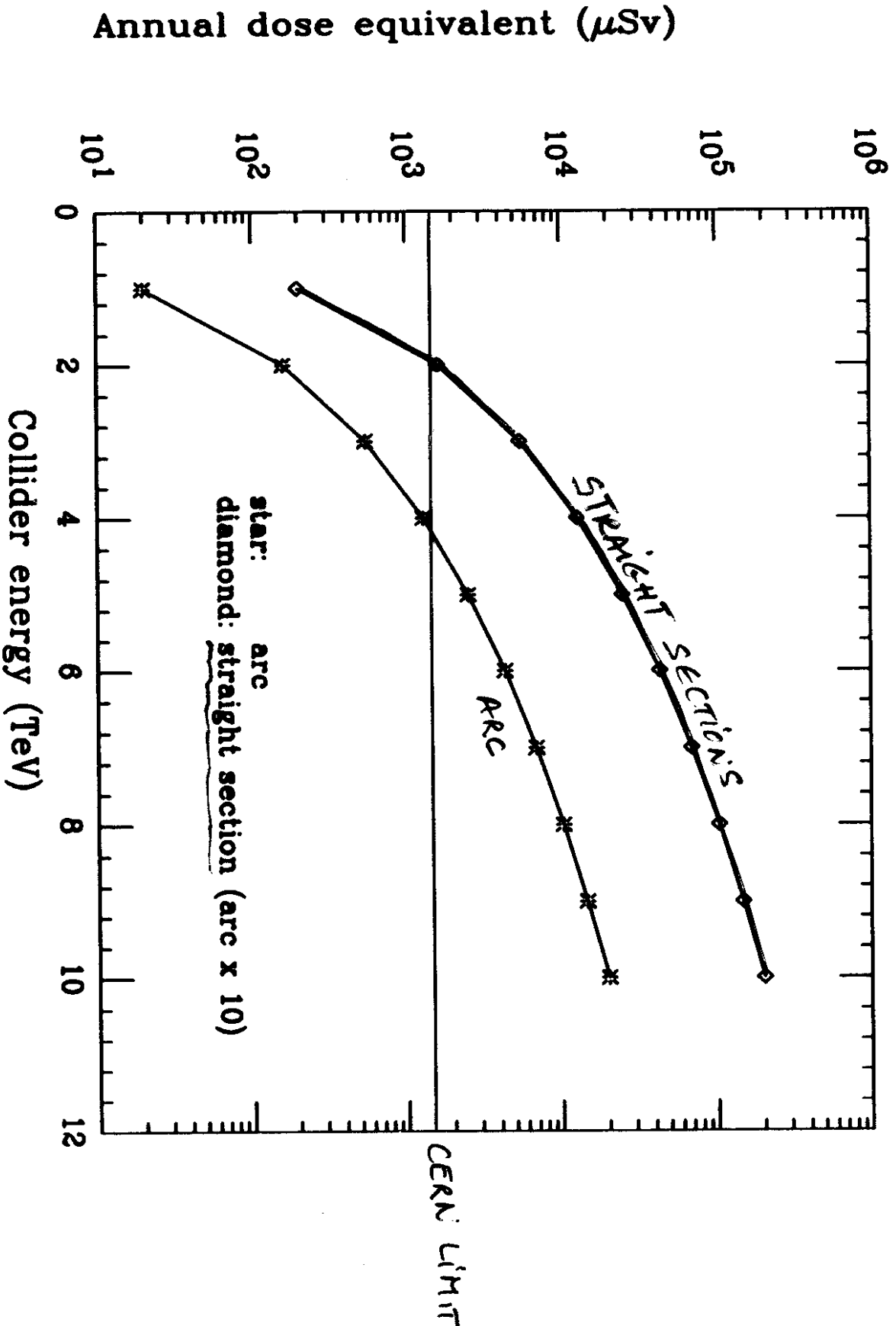


Fig. 1. Dose equivalent due to neutrino radiation at 36 km distance (collider at 100 m depth)

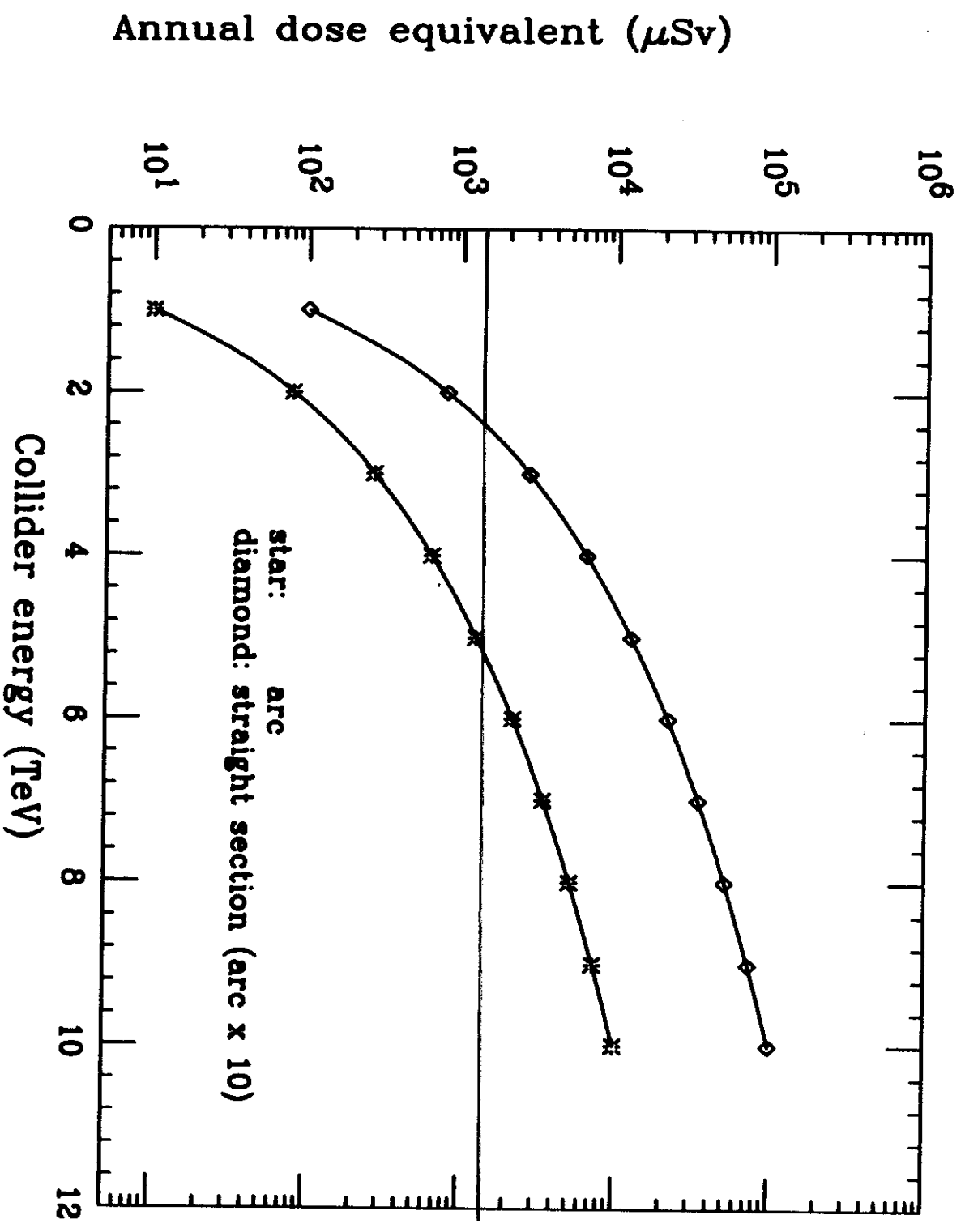


Fig. 2. Dose equivalent due to neutrino radiation at 51 km distance (collider at 200 m depth)

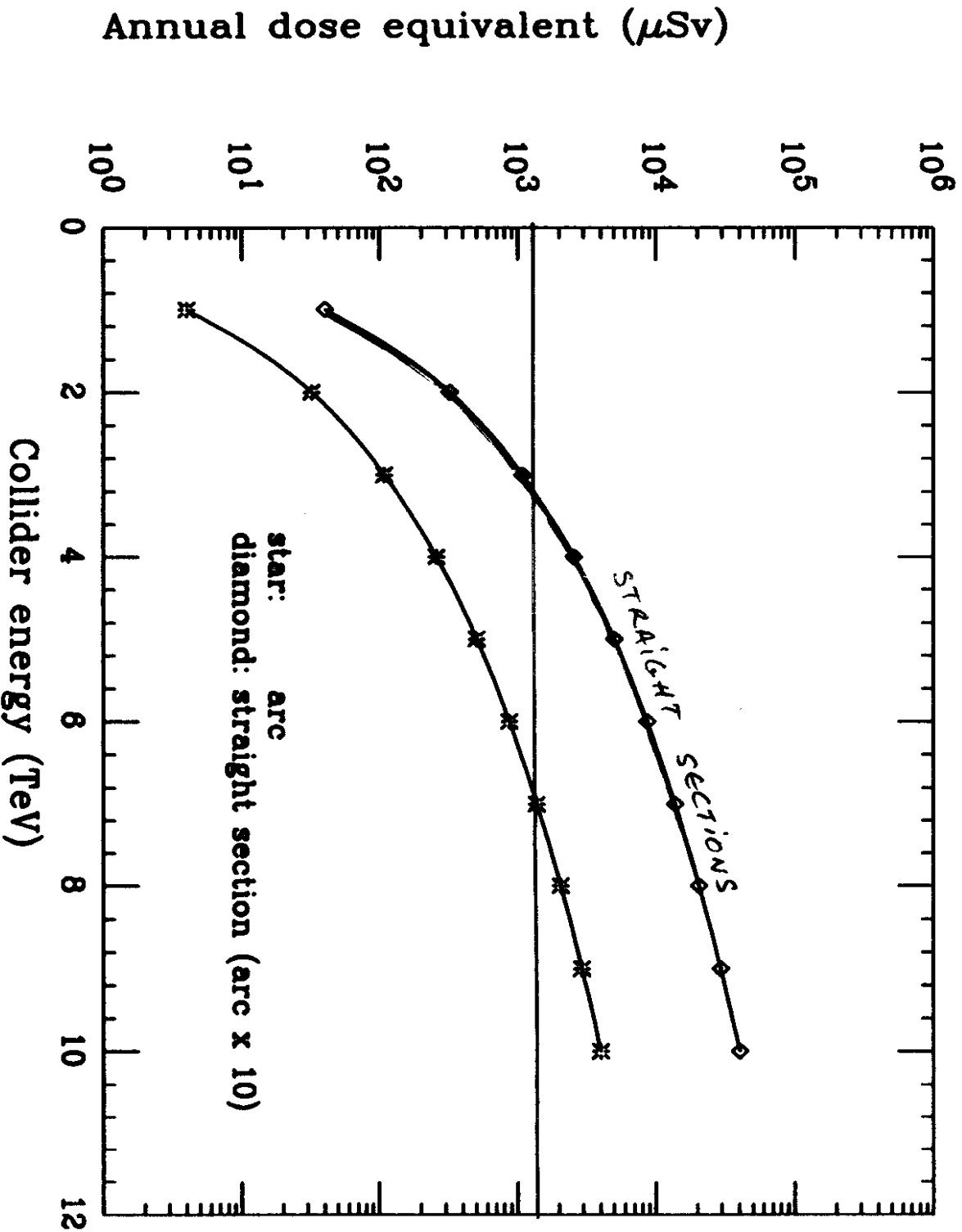


Fig. 3. Dose equivalent due to neutrino radiation at 80.5 km distance (collider at 500 m depth)



# NEUTRINO RADIATION

## LINES OF THOUGHT FOR SOLUTIONS:

- x ACCEPT REDUCTION IN INTENSITY  
BUT NOT IN LUMINOSITY
  - ⇒ IMPROVE COOLING → HIGHER  $\beta$
  - NEW METHODS
  - ⇒ COMPENSATE BEAM BEAM TUNE-SHIFT
  - ⇒ MODIFY FREQUENCY / INTENSITY
  - ⇒ ALL OF ABOVE.
  
- x ARRANGE COLLIDER GEOMETRY  
CAREFULLY: BUY EXIT POINTS  
FACING STRAIGHT SECTION
  
- x SITUATE MACHINE DEEP UNDER GROUND.

## in the US

- V-FACT99 has given MCC tremendous boost !
- MCC → V-FACT + MC Collaboration !
- BNL (UPGRADED AGS) or FERMILAB (Pre Injector)?
- TARGET EXPERIMENT GIVEN A BIG KICK ↑
- NSF "CONSIDERING" 500 M \$ SUPPORT FOR CORNELL + BNL PROJECT

? ↘ { FEASIBILITY STUDY SOON  
PROPOSAL IN 1-2 YEARS  
MACHINE COULD BE THERE IN 7-8 YEARS  
[H. KIRK, BNL]

--- THINGS ARE MOVING FAST ---

## WORKING GROUPS IN EUROPE:

- **NFWG** appointed 3/5/99 (H. Haseroth)  
brief report 9/99  
more detailed report 3/00

"To study the accelerator aspects of a possible neutrino factory" DCEB

- **BEAM & DETECTORS** (F. DYDAK + J. GOMEZ)  
continues from  $\nu$ FACT 99

- **INTENSE MUONS & NEUTRINOS** (J. ELLIS NEW)

- **Higgs FACTORY & HIGH ENERGIES** (P. JANOT)

+

- **High Intensity Proton Source** (R. GAROBY, Linac  
H. SCHÖNAUER, Synch.,  
+ accum.)

Plenary meetings  $\approx$  3 MONTH



$\gamma$ -FACT $\emptyset\emptyset$

May 22-26 2000  
MONTEREY Ca

ENCOURAGEMENTS + GUIDELINES FROM SPC  
WOULD BE VERY BENEFICIAL!

# ACTIVITIES TOWARDS $\gamma$ -FACTORY and $\mu\mu$ COLLIDER.

- ASCERTAIN #  $\mu/p$  BY RELIABLE CALCULATIONS (AKA. "Full simulation")
  - develop tools to track  $\mu$  from target to accelerator, through • Production models

Combines tools from  
accelerator phys.  
+ experimental phys.

- magnetic field
- RF cavities
- $DE/DX$ , multiple scattering, straggling and secondary interaction
- decay

→ 1 month workshop in BERKELEY 10 October → 10 NOVEMBER  
Participation from CERN: 3 people. (2 PS + 1 EP)

- UNDERSTAND WHICH PART OF THE CHAIN REQUIRES EXPERIMENT
  - TARGET EXPERIMENT in BNL given high priority
  - AT CERN, UNDER CONSIDERATION:
    - TARGET TESTS (liquid Hg)
    - RF IRRADIATION EXPT
    - $\pi$  production expt.

# ACTIVITIES TOWARDS $\gamma$ -FACTORY and $\mu\mu$ COLLIDER

## • REFINE PHYSICS PERFORMANCE EVALUATION

- oscillations • more realistic detectors
  - " sophisticated, powerful detectors
- use of polarisation and sensitivity to beam parameters

## low energy $\mu$ and $\gamma$

- stopped  $\mu$  identical
- $\mu$ -induced fusion?
- physics use of high intensity proton machine
- nearby  $\gamma$  physics

## muon colliders

- comparison with TESLA, NLC, CLIC
- benefits of high precision measurements of  
 $m_h, m_A, m_H, m_{Susy}, \dots$

• ....

MUON machines can offer a very rich physics programme for many years.

$\nu$ -FACTORY  $\rightarrow$   $\nu$  mixing matrix ( $\theta_{13}$ !) + matter effects + CP violation  
(if LMA is correct)

$\rightarrow$  A WORLD MACHINE WITH TREMENDOUS LOCAL BY-PRODUCTS  
• High intensity  $\nu$  beams, stopped muons etc....

$\rightarrow$  FIRST STEP FOR HIGGS FACTORY (IES)  
FRONTIER COLLIDER.

EUROPE SHOULD CONSIDER THIS OPTION

VERY SERIOUSLY