

STOPPED MUONS

WG

- BALDINI
 - BLONDEL
 - DE GOUVEA
 - ELLIS
 - GIUDICE
 - JUNGMANN
 - LOLA
 - PALLADINO
 - TOBE
 - VACCHI
 - VAN DER SCHAAF
 - ZUBER

At previous plenary meeting

talk by de Gouvea:

- precision measurement of $\mu \rightarrow e\nu\bar{\nu}$
(τ_μ , Michel parameters)
 - rare decays
 - model-independent approach
based on effective operators
 - CP violation in $\mu \rightarrow eeee$

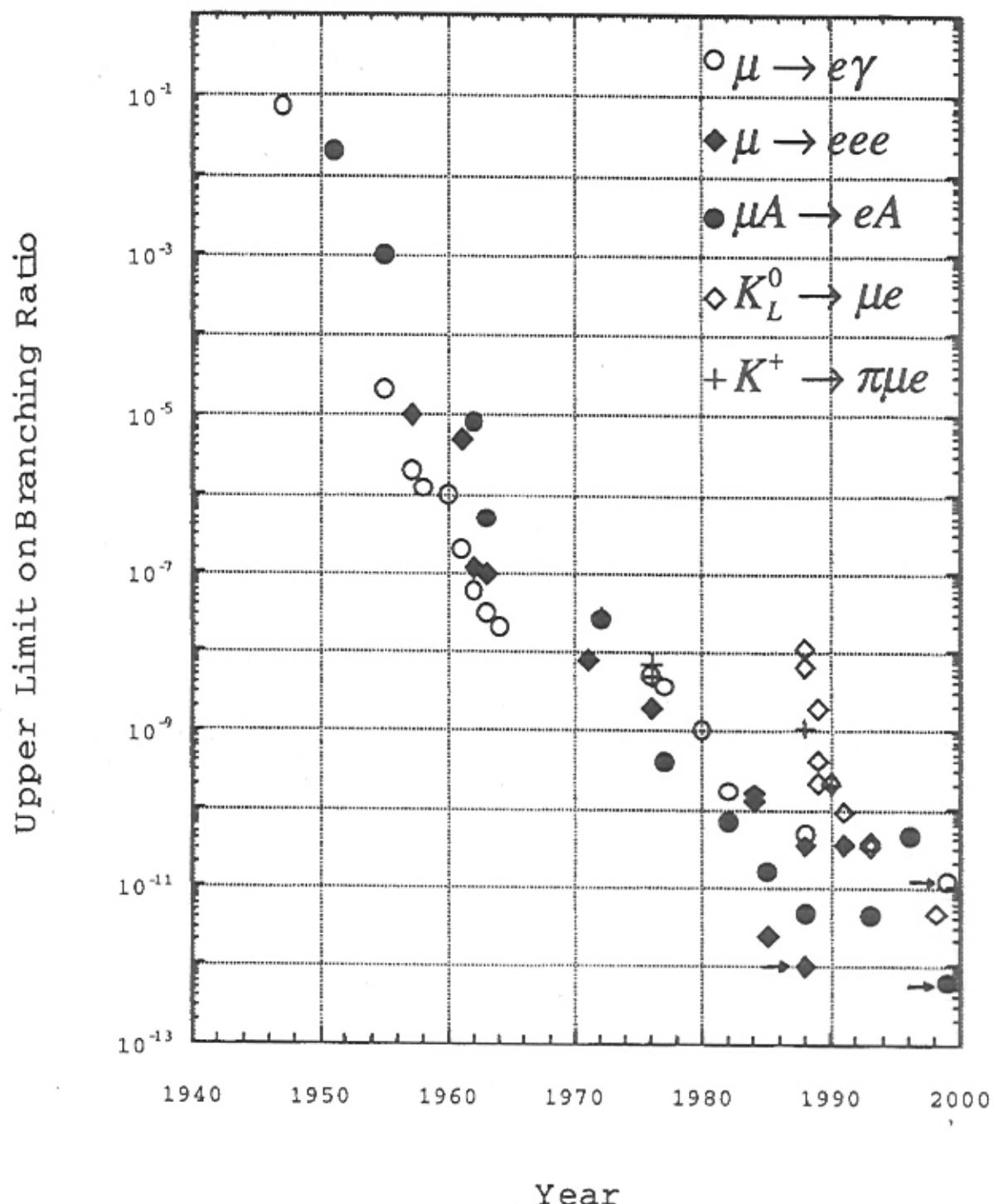
SUSY SCENARIOS

What do we learn from new experiments on rare μ decays?

STATUS AFTER LHC

- susy discovered
- many sparticle masses known

STATUS OF RARE MUON PROCESSES



PSI $\mu \rightarrow e\gamma$ 10^{-14}

SINDRUM II, PSI $\mu \rightarrow 3e$?

MECO, BNL $\mu^- Ti \rightarrow e^- Ti$ 10^{-16}

PRISM $\mu \rightarrow e\gamma : [10^{-15}]$ $\mu^- Ti \rightarrow e^- Ti : 10^{-18}$

IS IT USEFUL TO IMPROVE SEARCHES ?

Th : yes

- Source of lepton violation
not equal to ordinary ν oscillations
- In SUSY test of mixing angles
not accessible at high-energy colliders



susy masses

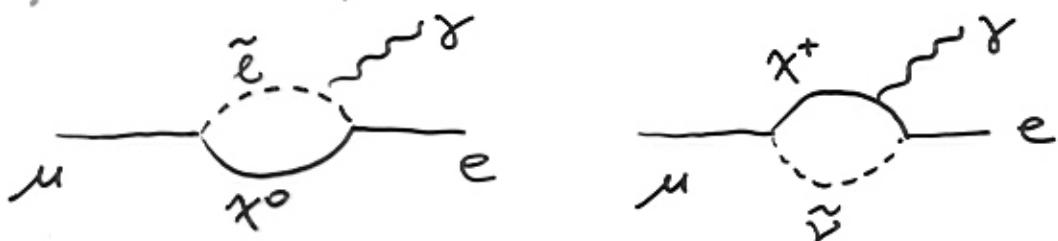
susy CKM angles and phases

RARE μ -decays in SUSY

susy $\left\{ \begin{array}{l} L \text{ violation in } \\ \text{slepton soft terms} \\ L \text{ violation from } R \end{array} \right\}$ $\left\{ \begin{array}{l} \text{from } \nu_R \\ \text{from GUT} \\ \text{effects} \end{array} \right\}$

$$\underline{\mu \rightarrow e\gamma}$$

\mathcal{L} in soft terms



$$BR(\mu \rightarrow e\gamma) \sim \frac{\alpha^3}{G_F^2} \frac{\tilde{\Theta}_{\mu e}^2}{\tilde{m}^4}$$

- \mathcal{L} in $\tilde{\Theta}_{\mu e}$
- Not suppressed by $1/M_{\nu_R}$ (as in SM)
- Enhanced by $\tan\beta$

(6)

To make predictions: how large is $\tilde{\theta}_{\mu e}$?

Most conservative estimate in supergravity:

- $\tilde{\theta}_{\mu e} = 0$ at M_{Pl}

$\tilde{\theta}_{\mu e}$ generated by quantum loops

- because of ν_R effects
- because of GUT effects

ν_R EFFECTS

$$\mathcal{L} = \lambda_\nu \bar{\ell}_L \nu_R H_u + \lambda_e \bar{\ell}_L e_R H_d + M_{\nu_R} \nu_R \nu_R$$

- Family L violated
(analogous to CKM in quark sector)
- induces non-diagonal $\tilde{\ell}_L$
mass-matrix elements

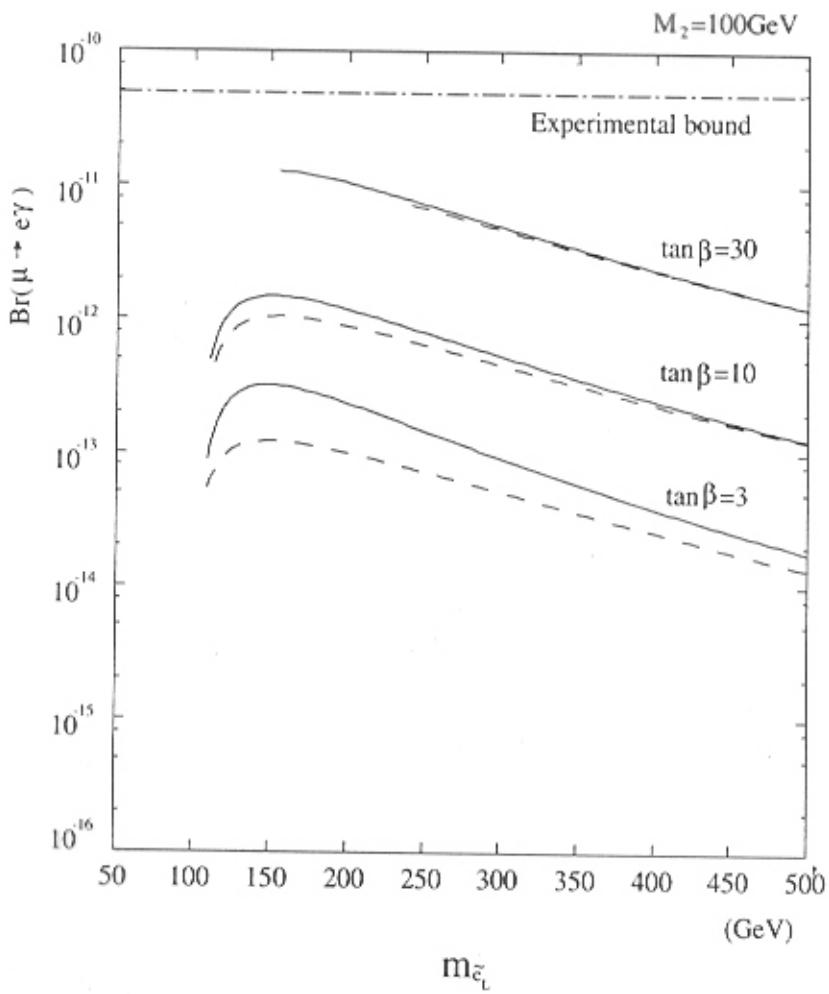
$$\delta \tilde{m}_e^2 \sim \frac{1}{16\pi^2} (3 \tilde{m}^2 + A^2) \lambda_\nu^+ \lambda_\nu^- \log \frac{M_{Pe}^2}{M_{\nu_R}^2}$$

Predictions depend on V_ν^{KM} assumptions

Examples:

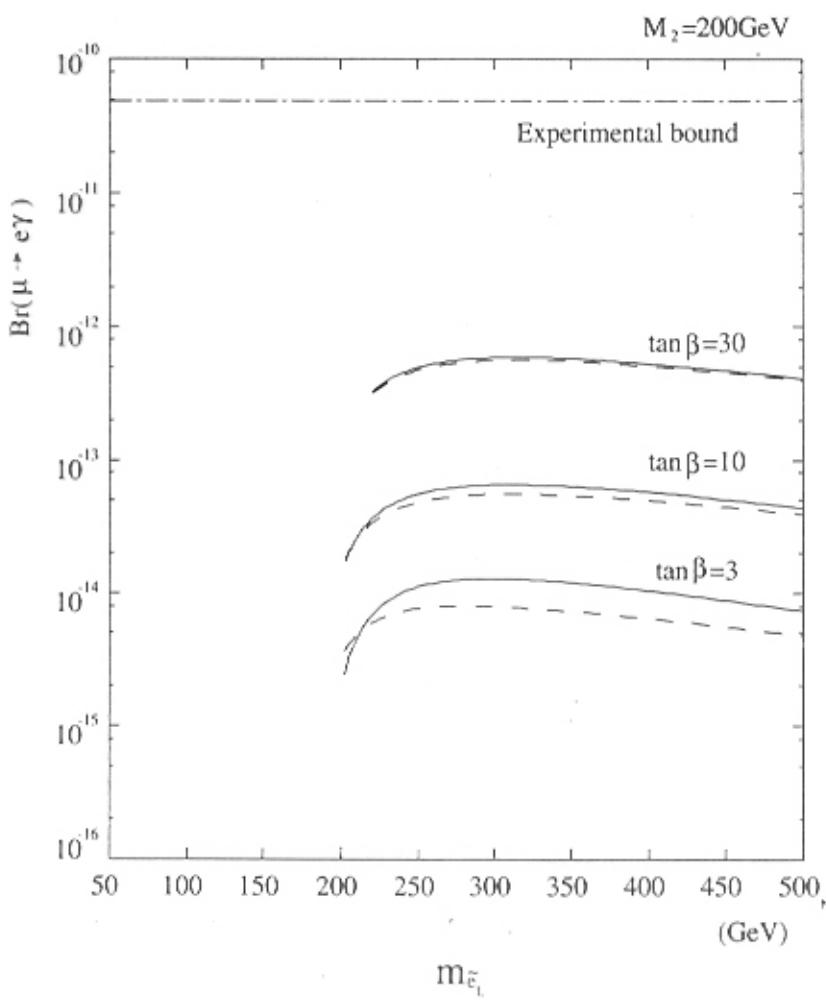
$$1) V_\nu^{KM} = V_q^{KM}$$

$$2) V_\nu^{KM} \text{ ansatz fitting } \nu \text{ oscillation data}$$



γ_R effect
with
 $V_\gamma^{kn} = V_q^{km}$

HISANO
HOROI
TOBE
YAMAGUCHI



ν_R effect
with V_{ν}^{KM}
from
 ν -oscillation
data

ELLIS
GOMEZ
LEONTARIS
LOLA
NANOPOULOS

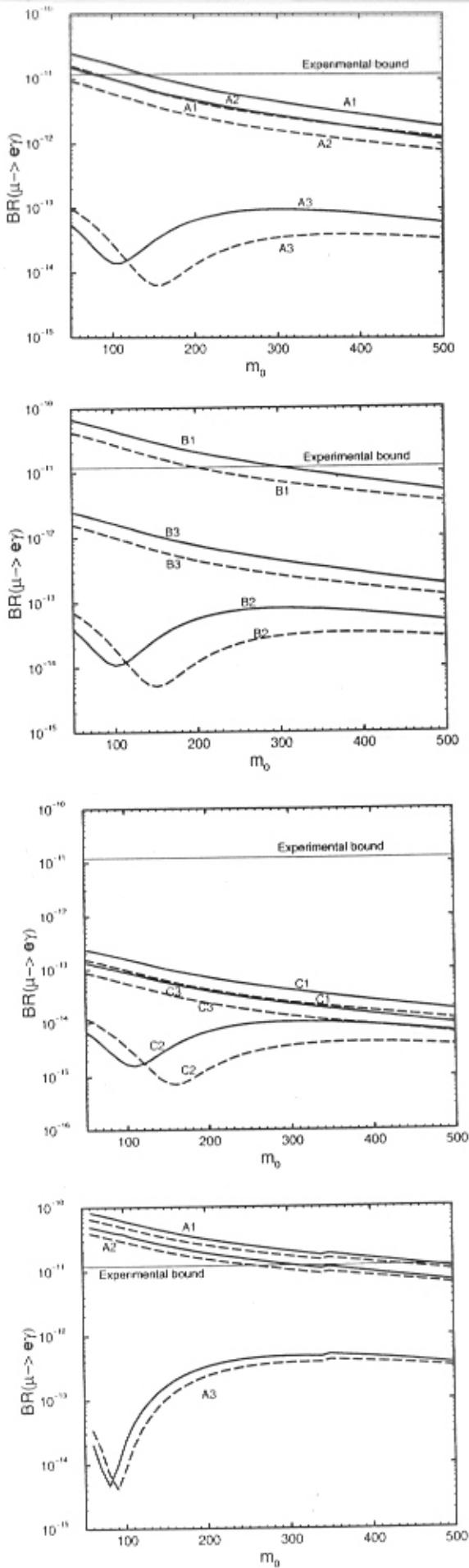


Figure 2: Predictions for $BR(\mu \rightarrow e\gamma)$ and $BR(\tau \rightarrow \mu\gamma)$ for texture A of Section 4, assuming the values $m_{1/2} = 250$ GeV, $\tan \beta = 3$ and $A_0 = -m_{1/2}$. The solid lines correspond to positive μ , and the dashed ones to $\mu < 0$. The results are for the three specific choice of the undetermined numerical coefficients c_{ij} shown in the text. We see that, for fixed m_0 , the $\mu \rightarrow e\gamma$ curves are more sensitive to the c_{ij} than are those for $\tau \rightarrow \mu\gamma$.

GUT effects

Above SU_5 GUT threshold

e_R and U_R in same multiplet.

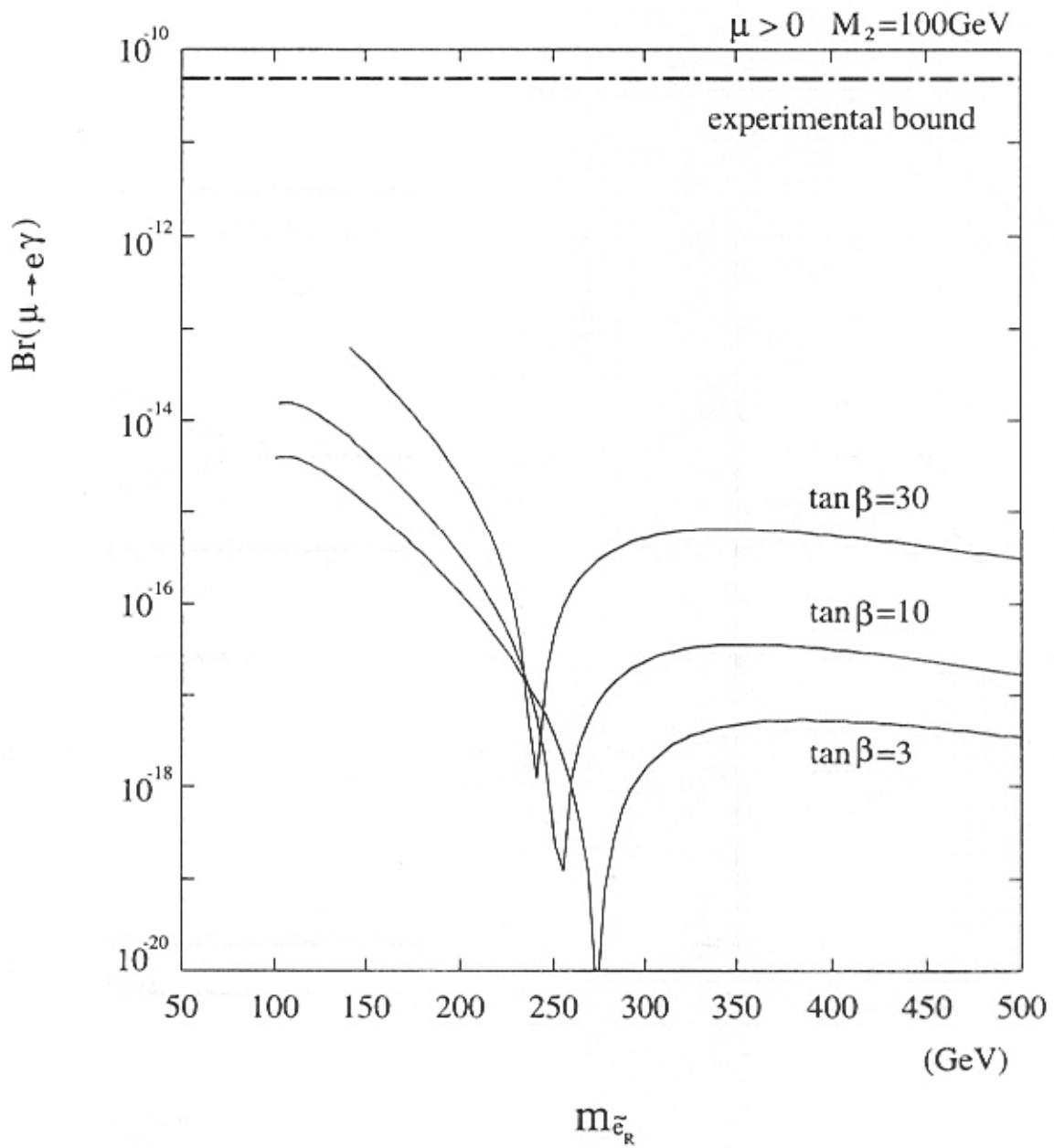
Because of λ_t effects \Rightarrow

$\Rightarrow 3^{\text{rd}}$ gen split from other 2

- Lepton violation mainly in right-handed sector

(chargino diagram suppressed)

SUSY GUT effect



HISANO et al.

Fig. 14

$\mu \rightarrow 3e$

- γ, Z penguins, box diagrams
- γ dominates (because of IR log):

$$\frac{\Gamma(\mu \rightarrow 3e)}{\Gamma(\mu \rightarrow e\gamma)} = 6 \times 10^{-3}$$

$\mu-e$ conversion

- If γ dominates

$$\frac{\Gamma(\mu-e \text{ conv})}{\Gamma(\mu \rightarrow e\gamma)} \approx 6 \times 10^{-3}$$

Not always true (because of
absence of logs)

R-parity violation

see talk by A. de Gouvea

- Effect from 4-fermion operators
($\mu \rightarrow 3e$ tree level, $\mu \rightarrow e\gamma$ loops)

- 3 cases

	$\mu \rightarrow e\gamma$	$\mu \rightarrow 3e$	$\mu - e$ conv.
1)	loop	tree	loop
2)	loop	loop	loop
3)	loop	loop	tree

Table 1: The ratios of branching ratios $\text{Br}(\mu^+ \rightarrow e^+ \gamma)/\text{Br}(\mu^+ \rightarrow e^+ e^- e^+)$ and $\text{R}(\mu^- \rightarrow e^- \text{ in Ti})/\text{Br}(\mu^+ \rightarrow e^+ e^- e^+)$, P -odd asymmetries A_P for $\mu^+ \rightarrow e^+ \gamma$, A_{P_1} and A_{P_2} for $\mu^+ \rightarrow e^+ e^- e^+$ are shown when the listed pair of Yukawa couplings is dominant. Case (1), (2), (3) refers to the representative classes of models discussed in Secs. 4.1, 4.2, and 4.3, respectively. Here, we assume $m_{\tilde{\nu}, \tilde{l}_R} = 100$ GeV and no mixing in the charged slepton mass matrix, and $m_{\tilde{q}} = 300$ GeV. We also show a typical result obtained for the MSSM with heavy right-handed neutrinos and R -parity conservation [7].

	$\frac{\text{Br}(\mu \rightarrow e\gamma)}{\text{Br}(\mu \rightarrow 3e)}$	$\frac{\text{R}(\mu \rightarrow e \text{ in Ti})}{\text{Br}(\mu \rightarrow 3e)}$	A_P	A_{P_1}	A_{P_2}	A_{P_1}/A_{P_2}
Case (1)						
$\lambda_{131}\lambda_{231}$	1×10^{-4}	2×10^{-3}	-100%	+19%	-15%	-1.3
$\lambda_{121}\lambda_{122}$	8×10^{-4}	7×10^{-3}	+100%	-19%	+15%	-1.3
$\lambda_{131}\lambda_{132}$	8×10^{-4}	5×10^{-3}	+100%	-19%	+15%	-1.3
Case (2)						
$\lambda_{132}\lambda_{232}$	1.2	18	-100%	-25%	-5%	5.6
$\lambda_{133}\lambda_{233}$	3.7	18	-100%	-25%	-4%	6.2
$\lambda_{231}\lambda_{232}$	3.6	18	+100%	+25%	+4%	6.2
$\lambda'_{122}\lambda'_{222}$	1.4	18	-100%	-25%	-4%	5.7
$\lambda'_{123}\lambda'_{223}$	2.2	18	-100%	-25%	-4%	5.9
Case (3)						
$\lambda'_{111}\lambda'_{211}$	0.4	3×10^2	-100%	-26%	-5%	5.4
$\lambda'_{112}\lambda'_{212}$	0.5	8×10^4	-100%	-26%	-5%	5.4
$\lambda'_{113}\lambda'_{213}$	0.7	1×10^5	-100%	-26%	-5%	5.5
$\lambda'_{121}\lambda'_{221}$	1.1	2×10^5	-100%	-26%	-5%	5.6
MSSM with ν_R	1.6×10^2	0.92	-100%	10%	17%	0.6

DE GOUVEA - LOLA - TOBE

CONCLUSIONS

- Rare μ processes complementary to high-energy searches
- Reveal new sources of χ beyond ν oscillations
- In supergravity models expected at experimental sensitivity level
- Information on susy mechanism
- $\mu \rightarrow eee$ could be discovery mode