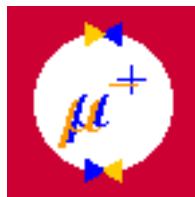


# Higgs Factory Physics

CP conserving part

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# Outline

- Introduction
- $h_{SM}$  and  $h^0$  resonances
  - resonance cross section
  - high precision measurements
  - radiative corrections
  - beam polarization
- Heavy scalar resonances ( $H^0$  and  $A^0$ )
  - widths and branching ratios
  - telling  $H^0$  from  $A^0$
  - overlapping resonances
- Charged Higgs bosons
- Conclusions

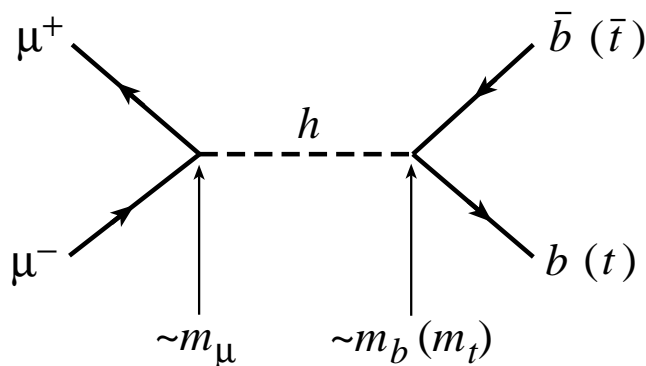
# Motivation

One of the key issues of future HEP experiments will be to pin down the exact mechanism of EWSM.

If the Higgs mechanism is Nature's choice one will want to determine masses, couplings, branching ratios, spin-0 character, CP-nature etc of (all) the Higgs boson(s) with high precision.

If there is more than one Higgs one needs to disentangle all the mass eigenstates and determine their properties.

A  $\mu^+\mu^-$  collider can essentially do all the physics that an  $e^+e^-$  collider of the same energy and luminosity can do. In addition:



Unique feature of the  $\mu C$ :  
Higgs production in the  $s$ -channel!

# The SM and MSSM Higgs bosons

**SM:** 1 Higgs doublet  $\rightarrow$  1 physical Higgs boson

If  $m_h < 2m_W$  then  $\Gamma^{\text{tot}} \lesssim 10$  MeV and the dominant decay mode is  $h_{SM} \rightarrow b\bar{b}$

**MSSM:** 2 doublets  $\rightarrow$  5 physical Higgs bosons

2 CP-even neutral scalars  $h^0, H^0$

1 CP-odd neutral scalar  $A^0$

2 charged scalars  $H^\pm$

Parameters:  $\tan\beta$  and  $m_A$

$$\begin{pmatrix} H^0 \\ h^0 \end{pmatrix} = \begin{pmatrix} \cos\alpha & \sin\alpha \\ -\sin\alpha & \cos\alpha \end{pmatrix} \begin{pmatrix} H_1^0 \\ H_2^0 \end{pmatrix}$$

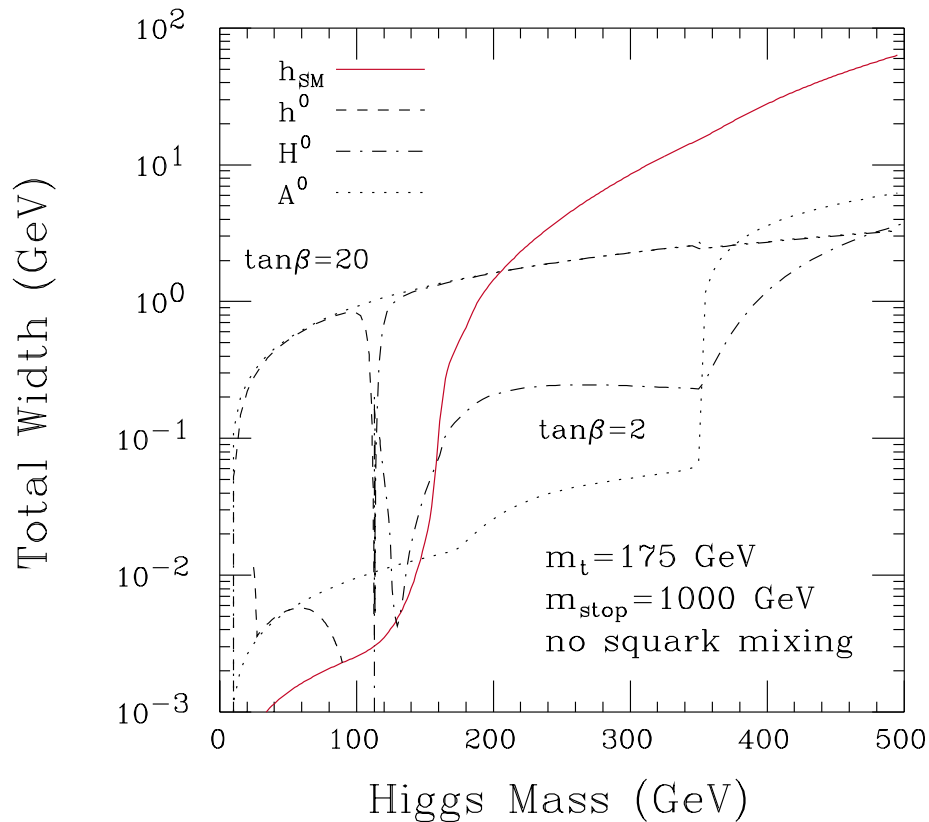
	$t$	$b, \tau$	$W, Z$
$h^0$	$\cos\alpha / \sin\beta$	$-\sin\alpha / \cos\beta$	$\sin(\beta - \alpha)$
$H^0$	$\sin\alpha / \sin\beta$	$\cos\alpha / \cos\beta$	$\cos(\beta - \alpha)$
$A^0$	$-i\gamma_5 \cot\beta$	$-i\gamma_5 \tan\beta$	0

Theoretical bound:  $m_{h^0} \lesssim 135$  GeV

For small  $\tan\beta$  and large  $m_A$ ,  $h^0$  is SM-like.

For large  $\tan\beta$ ,  $A^0$  and  $H^0$  are degenerate.

## Higgs Total Widths



Total width versus mass of the SM and MSSM Higgs bosons. SUSY decays are assumed to be absent.

Note that  $\Gamma^{\text{tot}} \lesssim 10$  MeV for a SM-like Higgs with  $m_h < 2m_W$ .

[Barger, Berger, Gunion, Han '96]

# Resonant Higgs production

The effective cross section at  $\sqrt{s} = m_h$  results from convoluting the standard  $s$ -channel Breit–Wigner resonance cross section with a Gaussian energy distribution  $\sigma_E$  :

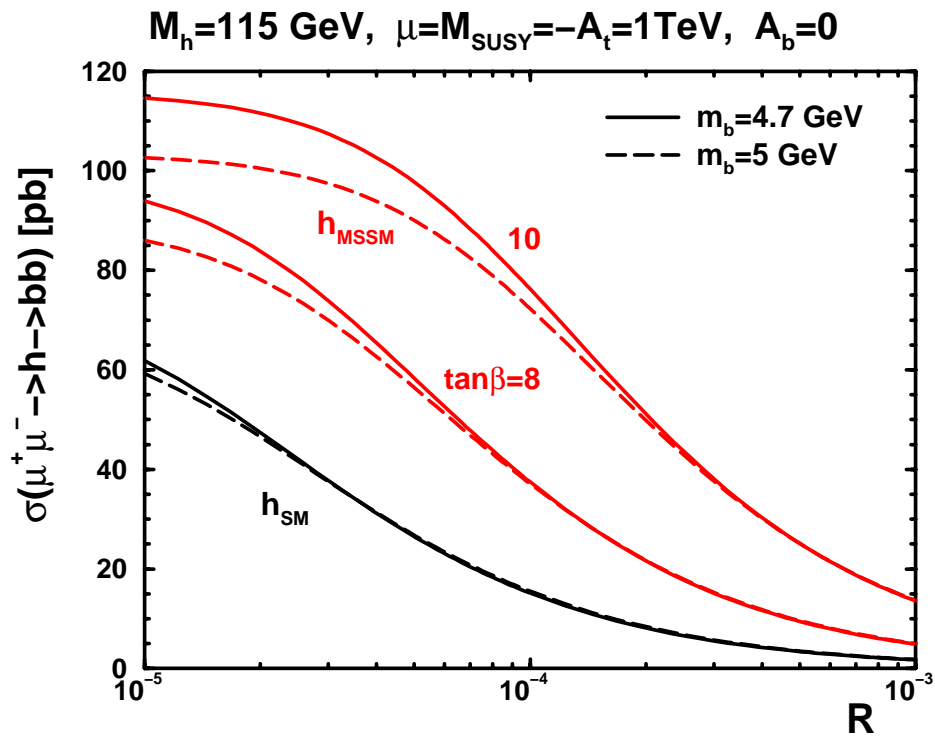
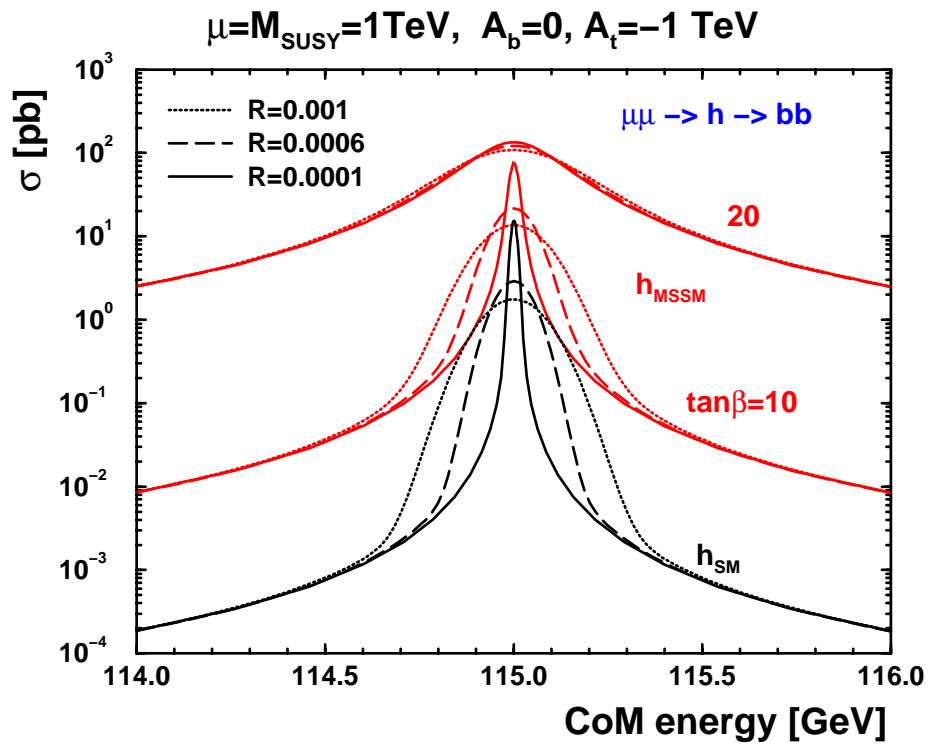
$$\bar{\sigma}_h \simeq \frac{4\pi}{m_h^2} \frac{B(h \rightarrow \mu^+ \mu^-) B(h \rightarrow X)}{\left[1 + \frac{8}{\pi} \left(\frac{\sigma_E}{\Gamma_h^{\text{tot}}}\right)^2\right]^{1/2}}.$$

The peak cross section is largest if  $\Gamma^{\text{tot}}$  is small and  $\sigma_E \sim \Gamma^{\text{tot}}$ . There are two important limits:

$$\sigma_E \ll \Gamma^{\text{tot}} \quad \Rightarrow \quad \bar{\sigma}_h = \frac{4\pi B(h \rightarrow \mu^+ \mu^-) B(h \rightarrow X)}{m_h^2}$$

$$\sigma_E \gg \Gamma^{\text{tot}} \quad \Rightarrow \quad \bar{\sigma}_h = \frac{\sqrt{2\pi^3} \Gamma(h \rightarrow \mu^+ \mu^-) B(h \rightarrow X)}{m_h^2 \sigma_E}$$

Often the beam energy resolution  $R = \sqrt{2} \sigma_E / \sqrt{s}$  is used instead of  $\sigma_E$ .



# Determining the properties of the resonance

Once  $m_h$  is approximately known, the  $\mu\text{C}$  can be run at  $\sqrt{s} = m_h$ .  $\rightarrow$  Allows to determine  $m_h < 2m_W$  of a SM-like Higgs to a fraction of MeV.

## Scanning: 3-point method

Measuring the ratio of the central peak cross section to the cross sections on the wings of the peak allows to determine  $\Gamma_h^{\text{tot}}$  to  $\mathcal{O}(10\%)$  if  $m_h \lesssim 130$  GeV. Requires an excellent energy resolution ( $\sigma_E < \Gamma$ ).

## Varying the beam energy resolution

The ratio of the peak cross sections for two different beam energy resolutions  $\sigma_E^{\text{min}} \ll \Gamma_h^{\text{tot}}$  and  $\sigma_E^{\text{max}} \gg \Gamma_h^{\text{tot}}$  is proportional to  $\Gamma_h^{\text{tot}}$ . Favourable method if  $\sigma_E < \Gamma$  leads to loss of  $\mathcal{L}$  and/or  $m_h \gtrsim 130$  GeV.

## Bremsstrahlung tail

If  $\sqrt{s} > m_h$  it is possible to search for a peak in the bremsstrahlung tail. This requires a good reconstruction of  $\sqrt{s}_{\text{eff}}$  from the final state momenta. Useful if  $m_h$  not known and essentially independent of  $R$ .

[Barger, Berger, Gunion, Han '96]

[Casalbuoni et al. '99]



# High precision measurements

of  $m_h$ ,  $\Gamma_h^{\text{tot}}$  and  $\sigma_{\text{peak}}$

- ⇒ distinguish between  $h_{SM}$  and  $h^0$  of the MSSM
- ⇒ determine the partial widths and associated couplings for all channels in which the Higgs can be observed:  $h \rightarrow b\bar{b}, \tau^+\tau^-, WW^*, ZZ^*$
- ⇒ fit  $(\tan\beta, m_A)$  with very good precision

[Janot, CERN 99-02]

Need to know theoretical predictions very precisely.  
Radiative corrections to the MSSM Higgs sector are important!

e.g. [Heinemeyer, Weiglein], [Carena, Garcia, Nierste, Wagner]

[Eberl, SK, Majerotto, Yamada]

★  $\sin\alpha_{\text{eff}} \rightarrow 0$ : suppression of  $\sigma(\mu^+\mu^- \rightarrow h^0)$

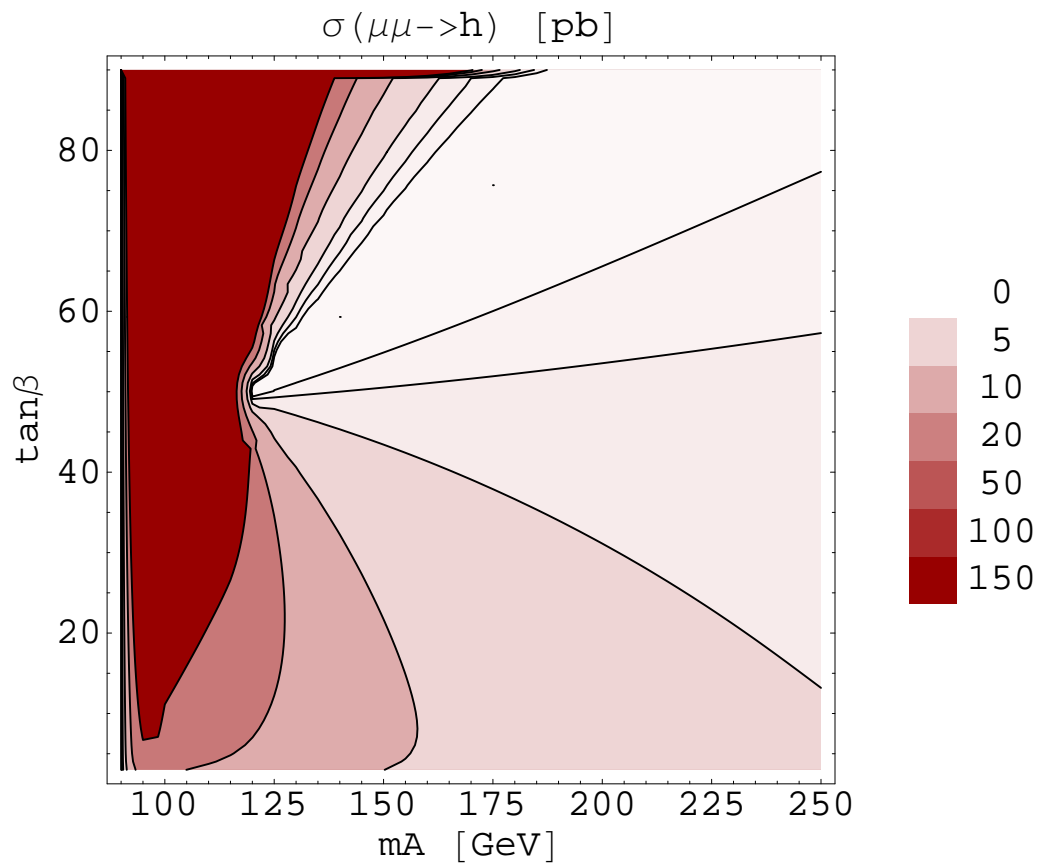
- $\sigma(\mu^+\mu^- \rightarrow H^0, A^0)$   $\tan\beta$  enhanced
- $H^0, A^0 \rightarrow b\bar{b}, \tau^+\tau^-$  dominate

★  $g_{hbb} \rightarrow 0$  due to  $\tan\beta$  enhanced SQCD corrections.

- No suppression of  $\sigma(\mu^+\mu^- \rightarrow h^0)$
- $h^0$  does not decay into  $b\bar{b}$
- $h^0 \rightarrow \tau^+\tau^-$  or  $WW^*$  observable

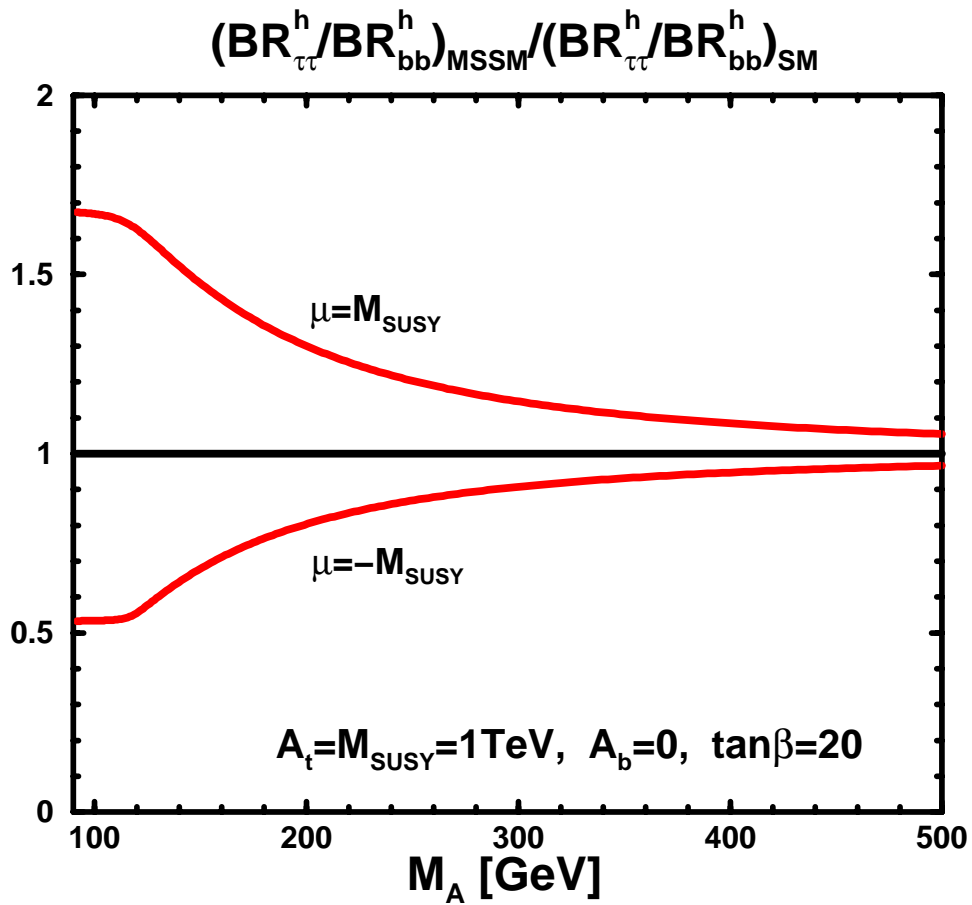
[Carena, Garcia, SK, Wagner, this WS]

[Talk by D. Gracia, 9 May 2000]



$$R = 10^{-4}, -A_t = \mu = M_{SUSY} = 1 \text{ TeV}$$

[talk by D. Gracia, 9 May 2000]



[talk by D. Gracia, 9 May 2000]

# The $\tau^+\tau^-$ signal

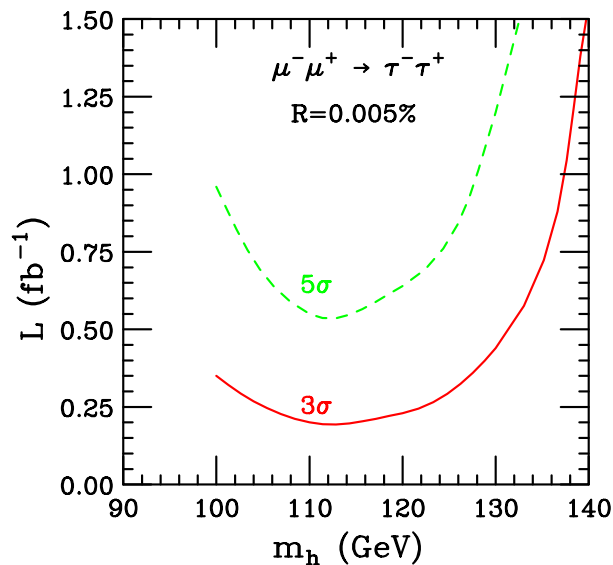
Allows to determine the the relative  $b$  and  $\tau$  Yukawa couplings and to test  $b - \tau$  unification of SUSY GUT theories.

## Higgs vs. $\gamma/Z$ exchange

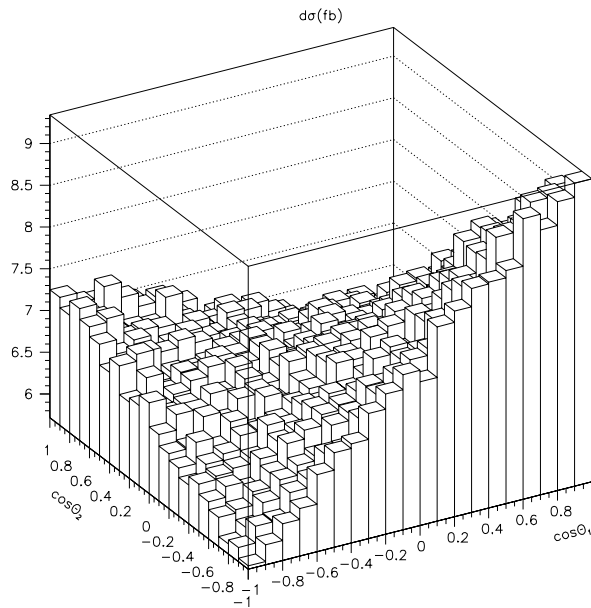
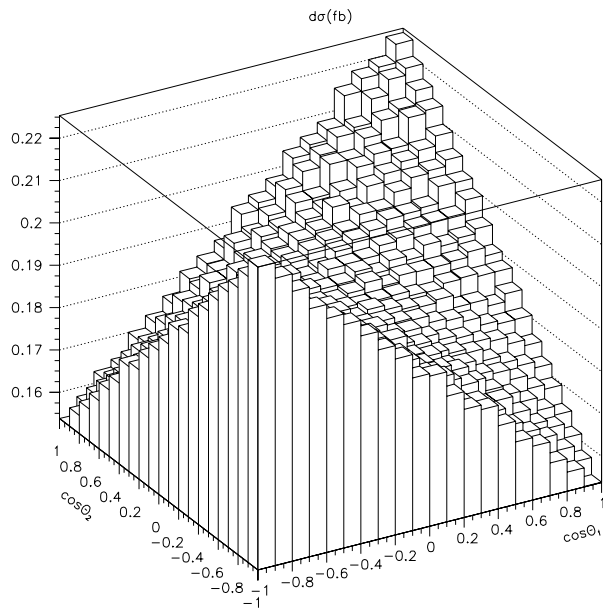
The Higgs exchange populates LL and RR helicity states of  $\mu^+\mu^-$  which lead to LL and RR combinations of  $\tau^+\tau^-$ . The differential cross section is isotropic in phase-space.

The SM background yields LR and RL combinations of  $\tau^+\tau^-$ . It shows a characteristic FB asymmetry in the scattering angle and a LR asymmetry in beam polarization.

Better beam energy resolution: significant enhancement of the signal for a narrow resonance, negligible effect on background.



[Barger, Han, Zhou '00]



Double differential distributions for  $\mu^+\mu^- \rightarrow \tau^+\tau^- \rightarrow \rho^-\nu_\tau\rho^+\bar{\nu}_\tau$  via Higgs exchange (upper fig.) and  $\gamma/Z$  exchange (lower fig.) for  $\sqrt{s} = m_h = 120$  GeV and  $R = 0.05\%$ . Initial  $\mu^\mp$  beam polarizations are  $P_- = P_+ = 0.25$ .

[Barger, Han, Zhou '00]

# $H^0$ and $A^0$

Prediction of  $m_A$  from high precision measurements at  $\sqrt{s} = m_{h^0} \rightarrow$  scan for the  $H^0$  and  $A^0$  resonances.

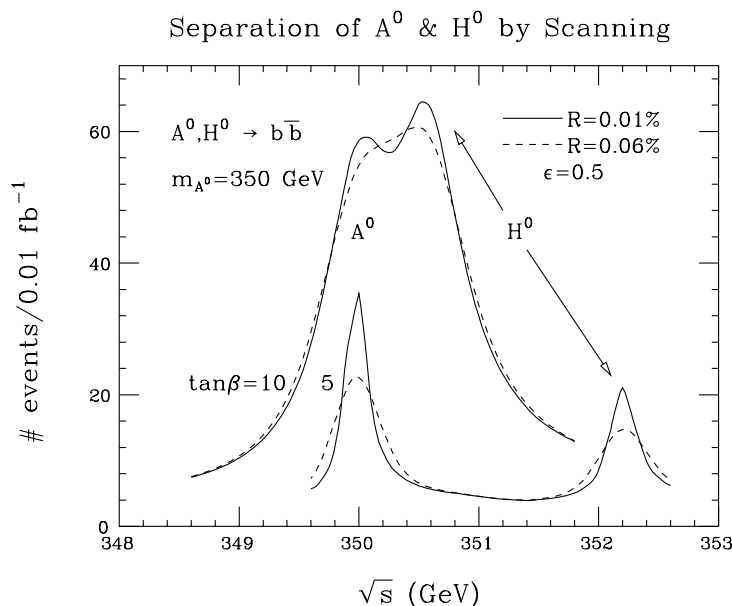
Once centered at  $\sqrt{s} = m_{H,A}$   
 $\rightarrow$  precision measurements of the  $H^0$  and  $A^0$  properties.

For large  $\tan \beta$  and/or large  $m_A$ ,  $H^0$  and  $A^0$  are (almost) degenerate and the two resonances (partly) overlap.

The high sensitivity on  $\tan \beta$  allows to determine  $\tan \beta$  with outstanding accuracy.

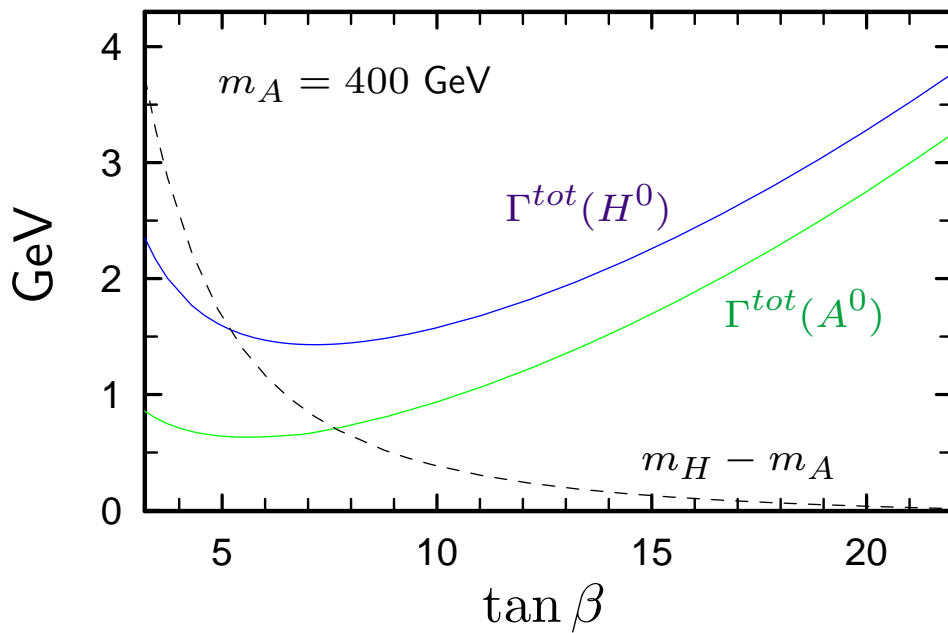
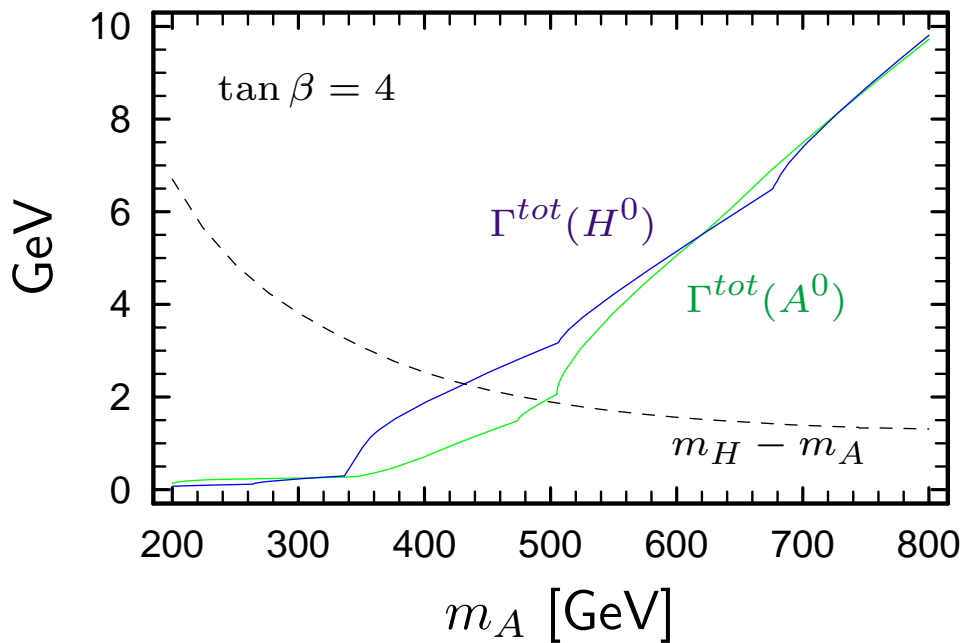
[Janot, CERN 99-02]

Stringent test of the model!



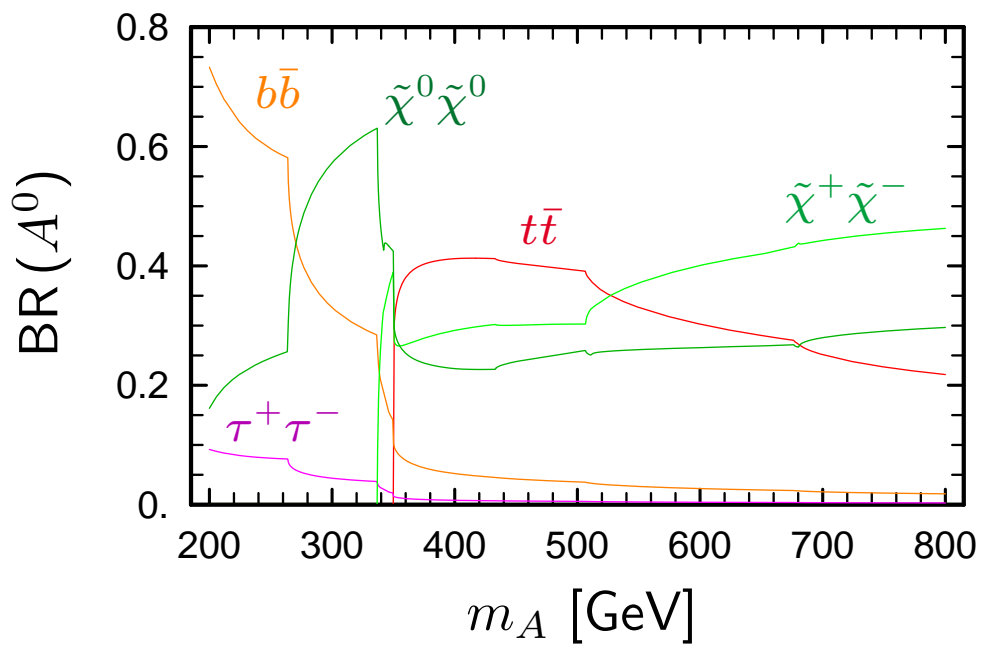
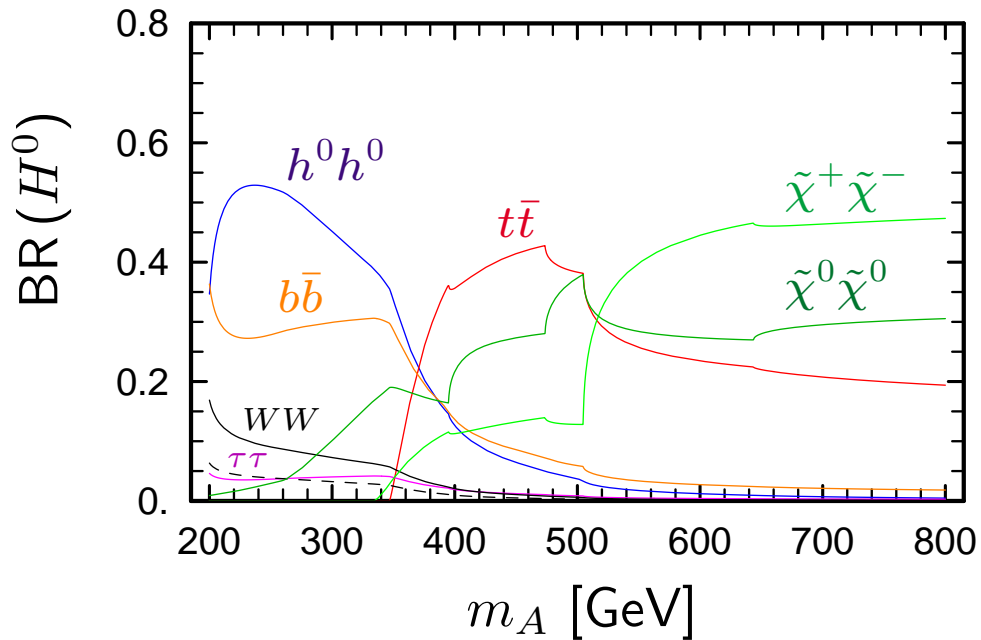
[Barger, Berger, Gunion, Han]

# $H^0$ and $A^0$ total widths



for  $M_2 = 200$  GeV,  $\mu = 300$  GeV,  $m_{\tilde{q}} \sim m_{\tilde{\ell}} \sim 800$  GeV

# Telling $H^0$ from $A^0$ : branching ratios

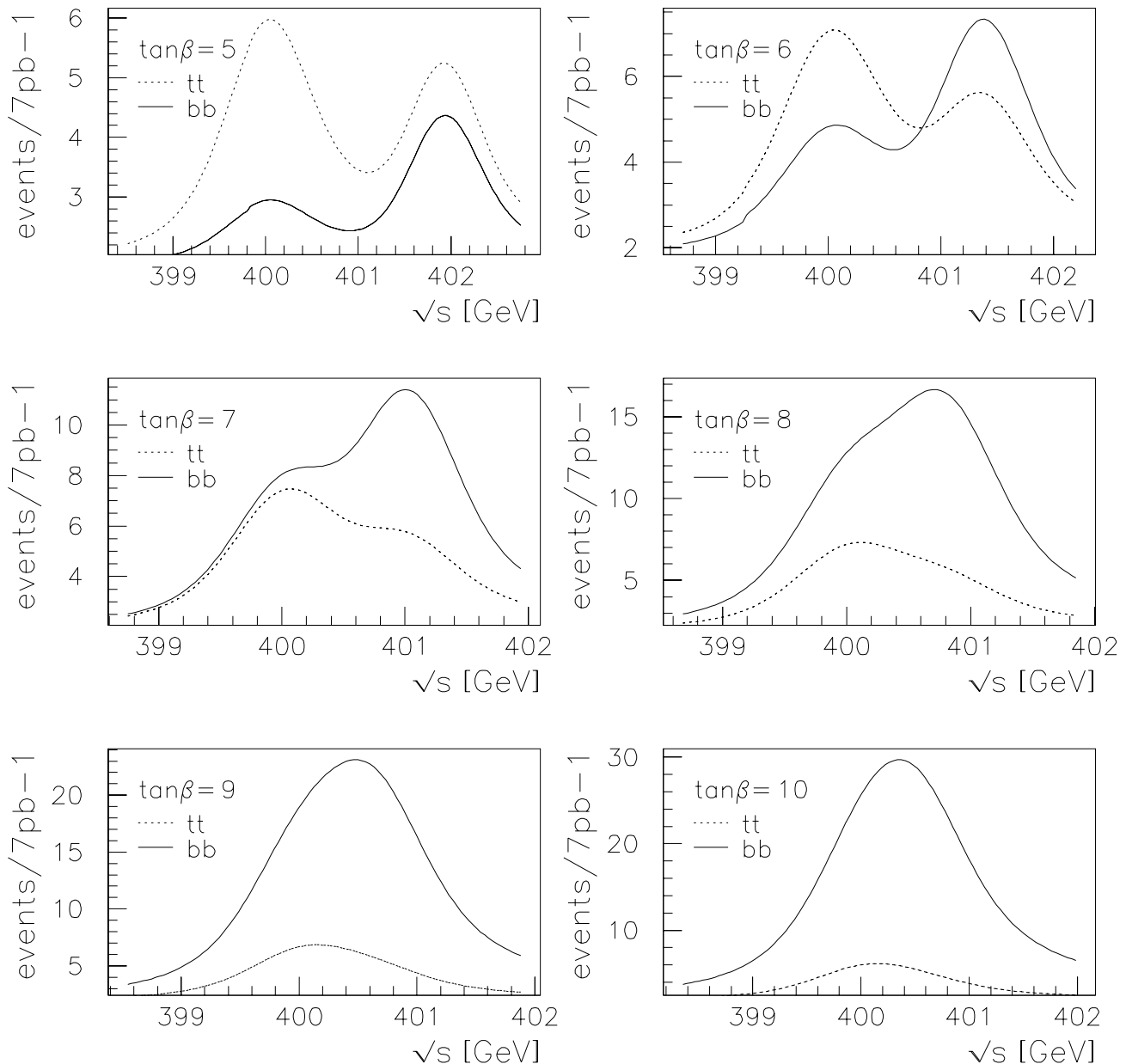


for  $\tan \beta = 4$ ,  $M_2 = 200$  GeV,  $\mu = 300$  GeV,  
 $m_{\tilde{q}} \sim m_{\tilde{\ell}} \sim 800$  GeV



# Telling $H^0$ from $A^0$ :

$$\mu^+ \mu^- \rightarrow H^0/A^0 \rightarrow b\bar{b}, t\bar{t}$$



Number of  $b\bar{b}$  (solid) and  $t\bar{t}$  (dashed) events per  $\mathcal{L} = 7 \text{ pb}^{-1}$  coming from  $\mu^+ \mu^- \rightarrow H^0 + A^0$  for  $m_A = 400 \text{ GeV}$ ,  $m_{\tilde{q}} = 1 \text{ TeV}$ , and no squark mixing.

[Grzadkowski, Gunion, Pliszka '00]

# $H^0 - A^0$ interference effects

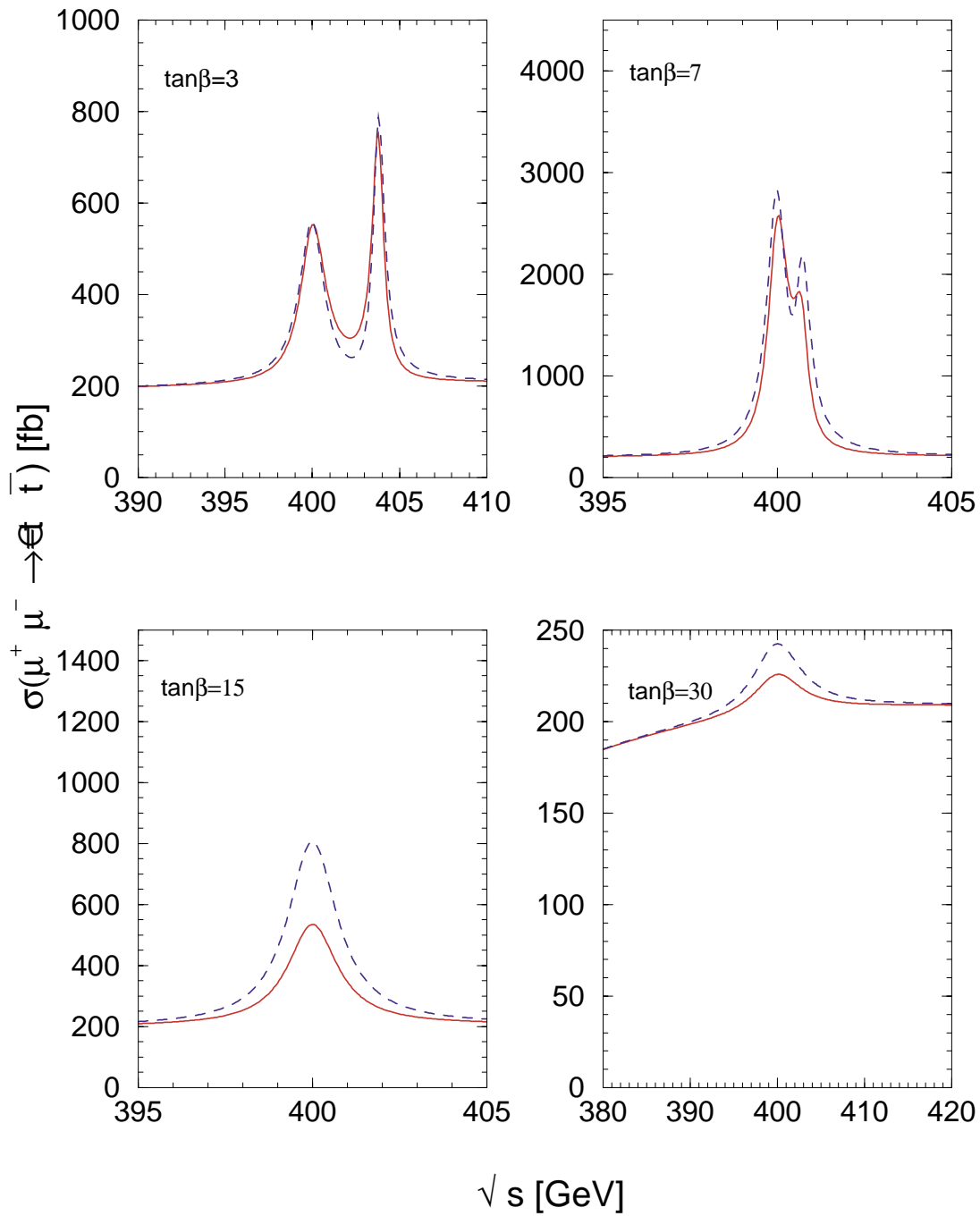
If the helicities of the initial and final state particles are fixed and  $m_H - m_A \lesssim \Gamma_{H,A}$ , the amplitudes of the  $H^0$  and  $A^0$  exchanges can sizably interfere. The asymmetry

$$\begin{aligned} A &= \frac{\sigma^{RRRR} + \sigma^{LLLL} - \sigma^{RRLl} - \sigma^{LLRR}}{\sigma^{RRRR} + \sigma^{LLLL} + \sigma^{RRLl} + \sigma^{LLRR}} \\ &= \frac{2\text{Re}[\mathcal{M}_H \cdot \mathcal{M}_A^*]}{|\mathcal{M}_H|^2 + |\mathcal{M}_A|^2} \end{aligned}$$

is a measure of the interference effect.

$A \neq 0$  means that two Higgs bosons with different CP-parities contribute to the resonance.

[Asakawa, Sugamoto, Watanabe '00]



Effective cross sections for  $\mu^+ \mu^- \rightarrow t\bar{t}$  for  $\tan\beta = 3, 7, 10, 30$ ,  $m_A = 400$  GeV and 60% beam polarization.

Red:  $\sigma(\mu_L^+ \mu_L^- \rightarrow t_L \bar{t}_L)$  or  $\sigma(\mu_R^+ \mu_R^- \rightarrow t_R \bar{t}_R)$ ,

Blue:  $\sigma(\mu_L^+ \mu_L^- \rightarrow t_R \bar{t}_R)$  or  $\sigma(\mu_R^+ \mu_R^- \rightarrow t_L \bar{t}_L)$

[Asakawa, Sugamoto, Watanabe '00]

# Charged Higgs

## Pair production

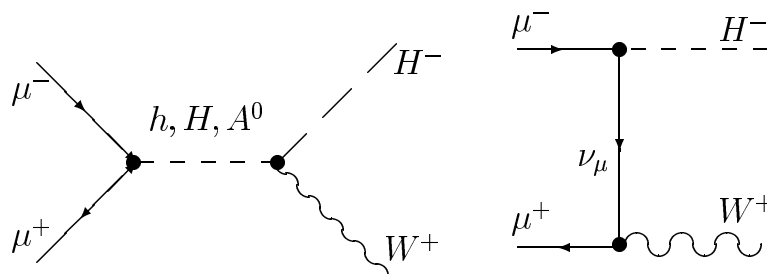
In the MSSM,  $H^0$ ,  $A^0$  and  $H^\pm$  are roughly degenerate if  $m_A > 200$  GeV.

$\Rightarrow$  main mechanism is  $\mu^+\mu^- \rightarrow \gamma/Z \rightarrow H^+H^-$

$\Rightarrow$  can probe up to  $m_{H^+} \lesssim \sqrt{s}/2$  identical to  $e^+e^-$

## Single production

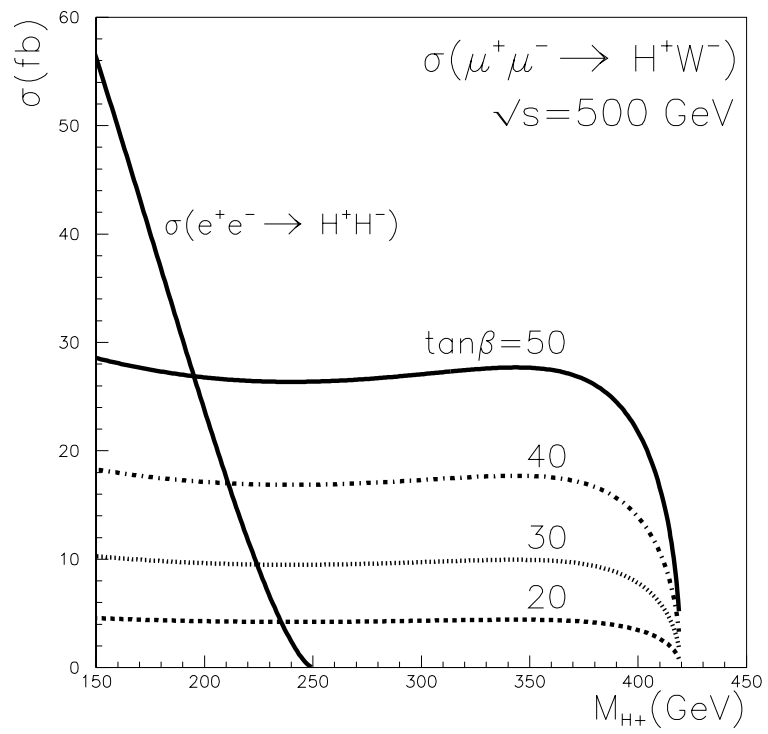
$\mu^+\mu^- \rightarrow H^\pm W^\mp$  proceeds via s-channel Higgs and t-channel neutrino exchange.



$\Rightarrow$  sensitive to the  $H^\pm \mu^\mp \nu_\mu$  Yukawa coupling

$\Rightarrow$  t-channel contribution can be large for large  $\tan \beta$

$\Rightarrow$  kinematical reach up to  $m_{H^+} \lesssim \sqrt{s} - m_W$



[Akeroyd, Arhrib, Dove '99]

# Conclusions

- At the  $\mu\text{C}$  the properties of the Higgs boson(s)  $h_{SM} (h^0, H^0, A^0)$ , i.e. mass, total and partial widths, spin, CP nature ....., may be determined with **outstanding accuracy**.  
e.g. for a SM-like Higgs boson with  $m_h < 2m_W$ :  
 $m_h, \Gamma_h$  to fractions of MeV!
- This allows to determine  **$\tan \beta$**  with high precision, even for high  $\tan \beta$ .
- Precise theoretical predictions are necessary (**radiative corrections** to  $h^0 \rightarrow b\bar{b}$  etc)
- Possibility for **scanning** and excellent **beam energy resolution** are essential.
- **Beam polarization** may be helpful to disentangle overlapping  $H^0$  and  $A^0$  resonances.
- A **charged Higgs** may be observed through  $\mu^+\mu^- \rightarrow H^\pm W^\mp$  with a kinematic reach of  $m_{H^\pm} \lesssim \sqrt{s} - m_W$ .